

The effects of digital elevation model resolution on the PyFLOWGO thermorheological lava flow model

Ian T W Flynn, Magdalena Oryaëlle Chevrel, David A Crown, Michael S

Ramsey

▶ To cite this version:

Ian T W Flynn, Magdalena Oryaëlle Chevrel, David A Crown, Michael S Ramsey. The effects of digital elevation model resolution on the PyFLOWGO thermorheological lava flow model. Environmental Modelling and Software, 2023, 167, 10.1016/j.envsoft.2023.105768. hal-04160976

HAL Id: hal-04160976 https://uca.hal.science/hal-04160976

Submitted on 13 Jul 2023

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution - NonCommercial - NoDerivatives 4.0 International License

1 2	The Effects of Digital Elevation Model Resolution on the PyFLOWGO Thermorheological Lava Flow Model
3	
4	Ian T. W. Flynn ¹ , Magdalena O. Chevrel ^{2,3,4} , David A. Crown ⁵ , and Michael S. Ramsey ¹
5 6	¹ Department of Geology and Environmental Science, University of Pittsburgh, Pittsburgh, PA, USA.
7 8	² Laboratoire Magmas et Volcans (LMV), Université Clermont Auvergne, CNRS, IRD, OPGC, 63000 Clermont-Ferrand, France.
9 10	³ Observatoire Volcanologique du Piton de la Fournaise, Institut de Physique du Globe de Paris, 97418 La Plaine des Cafres, France.
11	⁴ Université Paris Cité, Institut de Physique du Globe de Paris, CNRS, 75005 Paris, France.
12	⁵ Planetary Science Institute, Tucson, AZ, USA.
13	
14	Corresponding author: Ian Flynn (<u>itf2@pitt.edu</u>)
15	
16 17 18 19	
20	Highlights:
21	• We present a topographic sensitivity analysis for the PyFLOWGO lava flow model.
22	• Examined DEM resolutions were based on common Earth and planetary datasets.
23	• A model step size equal to or smaller than the DEM resolution should be used.
24	• DEM resolution has a quantifiable impact on the modeled flow length (up to 35%).
25	

26 Abstract (150/150 word limit)

27 Topography is a fundamental factor influencing the emplacement of lava flows. We assess the 28 impact of topographic resolution on the thermorheological PyFLOWGO model, specifically with 29 digital elevation model (DEM) resolutions commonly available for Earth and other planetary 30 bodies where flow modeling is relevant. We examined PvFLOWGO output parameters (e.g., 31 channel length, core temperature, and flow velocity) to assess model sensitivity to topography in 32 order to document model uncertainties and optimize future application. This study uses rheologic 33 and topographic data from the Tolbachik, Russia 2012-2013 eruption as model constraints. Using 34 moderate to lower resolution topographic data overestimates the channelized flow length by up to 35 35% due to differences in the distribution of slopes topographic variability at different resolutions 36 and resulting effects on the modeled lava velocity down channel. Determining the impact of 37 topography on thermorheological lava flow models such as PyFLOWGO is important to correctly 38 interpret the results for channelized flows.

- 39
- 40

41 Keywords: FLOWGO, Sensitivity analysis, Planetary science, Volcanology, Volcanic eruption,
42 Tolbachik, Topography, DEM

43

44 **1 Introduction**

45 The emplacement of a lava flow is controlled by a number of factors, such as the rheology 46 (i.e., lava viscosity, which depends on eruption temperature, composition, and degree of crystallization), the effusion rate, external environmental conditions (i.e., gravity, atmospheric 47 48 density, and temperature), and importantly, the topography over which it flows. Modeling lava 49 flow emplacement attempts to simplify these conditions to address specific volcanological 50 questions. For lava flows on Earth, modeling is commonly performed either once the flow is 51 emplaced in order to determine the rheological parameters or eruptive conditions (e.g., Harris & 52 Rowland, 2001; Ramsey et al., 2019; Rowland et al., 2005) or in a prognostic manner for hazard 53 response and assessment (e.g., Chevrel et al., 2022; Favalli et al., 2005, 2012; Harris & Rowland, 54 2015). For investigations of inactive/older flows on Earth and other planetary bodies, the goal is 55 typically to determine the eruption conditions and lava rheology necessary to produce the observed

flow length or area (e.g., Flynn et al., 2022; Ganci et al., 2020; Peters et al., 2021). No matter how

57 a lava flow model is applied, or the level of complexity included, topography is an essential dataset.

Therefore, understanding how the spatial resolution of a topographic dataset affects model resultsis critical.

60 For modeling recent terrestrial flows, it is common to have access to digital elevation 61 models (DEM) of the pre-flow surface ranging from moderate (~10-50 m/pixel) to high (≤ 10 62 m/pixel) resolution that are derived from photogrammetry, LIDAR, or InSAR datasets (Table 1) 63 (e.g., Chevrel et al., 2021; Kubanek et al., 2015; Richardson & Karlstrom, 2019). However, pre-64 flow topography is not available for investigations of older lava flows. Some planetary bodies may 65 have limited coverage of high to moderate resolution DEMs of a study region, whereas others are 66 limited to much lower resolution DEMs (Table 1). The resolution of planetary DEMs and lack of 67 pre-flow datasets have resulted in many studies using a constant slope to perform lava flow 68 modeling (e.g., Baloga & Glaze, 2008; Hiesinger et al., 2007; Peters et al., 2021). However, several 69 previous studies concluded that variations in local topography have a measurable impact on model 70 results of a lava flow's emplacement (Glaze & Baloga, 2007; Russo et al., 2022).

Planetary Body	Instrument	Spatial Resolution	Global Surface Coverage (%)	References
	ASTER ^a	30 m/pixel	100%	(Hirano et al., 2003)
Farth	SRTM ^b	30 m/pixel	100%	(Farr et al., 2007)
Larin	InSAR	12 m/pixel	~97%	(Rizzoli et al., 2017)
	ArcticDEM	2 m/pixel	~23%	(Takaku et al., 2020)
	MOLA ^c	463 m/pixel	100%	(Zuber et al., 1992)
	MOLA/HRSC ^d	200 m/pixel	100%	(Fergason et al., 2018)
Mars	HRSC	50 m/pixel	~44%	(Jaumann et al., 2007)
	CTX ^e	~20 m/pixel	~17%	(Breton et al., 2019)
	HiRISE ^f	~1-2 m/pixel	~0.4%	(Sutton et al., 2022)
Venus	Altimeter	10-20 km/pixel	98%	(Ford & Pettengill, 1992)
	SAR Stereo	1-2 km/pixel	20%	(Herrick et al., 2012)

71	Table 1: DEM	datasets c	commonly	available	for Earth,	Mars, and	Venus.
					,	,	

72 ^a Advanced Spaceborne Thermal Emission and Reflection radiometer

- 73 ^b Shuttle Radar Topography Mission
- 74 ^c Mars Orbiting Laser Altimeter
- 75 ^e Context Camera
- 76 ^f High Resolution Imaging Experiment
- 77

78 There are numerous lava flow emplacement models, and many have associated sensitivity 79 analyses to topography, including DOWNFLOW (Favalli et al., 2011), MAGFLOW (Bilotta et al., 80 2019), MULTIFLOW (Richardson & Karlstrom, 2019), and Q-LAVHA (Mossoux et al., 2016). 81 However, this has not been done for FLOWGO/PyFLOWGO (Chevrel et al., 2018; Harris & 82 Rowland, 2001). The focus of this study, therefore, is to investigate the impact of topographic data 83 resolution on the FLOWGO thermorheological model's output with specific focus on commonly 84 available DEM resolutions for Earth and other planetary bodies. We use a terrestrial study case 85 that was presented in Ramsey et al. (2019): the 2012-2013 Tolbachik eruption (Figure 1). It was chosen because Ramsey et al. (2019) already performed the FLOWGO modeling and provided the 86 87 input rheological parameters that best fit the lava flow.

88 1.1 The 2012-2013 Tolbachik Eruption

The Tolbachik volcanic complex is one of three active volcanoes (Klyuchevskoy, Bezymianny, and Tolbachik) that make up the Klyuchevskoy Volcano Group (KVG) in Kamchatka (Russia). Tolbachik is comprised of two stratovolcanoes, Ostry and Plosky Tolbachik, with multiple cones and lava flows to the south (Figure 1).



93

Figure 1. The Tolbachik volcanic complex comprised of Ostry and Plosky Tolbachik. To the immediate south of the
volcanic complex, are the three flow fields (shown in red) and two vents (red circles with black outline) formed during
the 2013 Tolbachik Fissure Eruption (TFE-50). Further south are three cones formed during the Great Tolbachik
Fissure Eruption (GTFE). The white dashed line indicates the path of the central channel used for the PyFLOWGO
model. Base image from Planets RapidEye Sensor (~5 m/pixel, visible), acquired on 18 June 2014.

99 Historically, the complex has produced eruptions throughout the Holocene and more recent 100 times (Churikova et al., 2015). The two most notable eruptions from the complex are the 1975-101 1976 Great Tolbachik Fissure Eruption (GTFE) and the 2012-2013 Tolbachik Fissure Eruption 102 (TFE-50), named after the 50th anniversary of the Institute of Volcanology and Seismology. During 103 the GTFE new monogenetic cones and several associated lava flows were emplaced along the 104 southern slope of Plosky Tolbachik (Figure 1) (Fedotov et al., 1984). However, most of the 105 deposited material is pyroclastic, infilling the area around the cones. The smaller TFE-50 eruption 106 produced mainly lava flows originating from vents that formed monogenetic cones closer to the 107 main volcanic edifice and along the same path that produced the GTFE (Churikova et al., 2015).

108During the TFE-50 eruption, which began on 27 November 2012, both Hawaiian and109Strombolian eruption styles occurred, producing basaltic trachyandesite lava flows (Belousov &

110 Belousova, 2017). The average effusion rate, measured with aerial photogrammetric surveys, early 111 in the eruption was $\sim 440 \text{ m}^3/\text{s}$, which gradually waned until the eruption ended on 5 September 112 2013 (Belousov & Belousova, 2017; Ramsey et al., 2019). At the end of the eruption three 113 prominent flow fields had formed, Vodopadnoye, Leningradskoye, and Toludskoye (Figure 1). 114 The Vodopadnoye flow field (area 6.17 km², volume 0.04 km³) originated from the Menyailov 115 vent and is comprised mostly of 'a'ā flows (Belousov et al., 2015; Belousov & Belousova, 2017). 116 Both the Leningradskoye (area 22.44 km², volume 0.35-0.39 km³) and Toludskoye (area 8.4 km², 117 volume 0.1 km³) flow fields originated from the Naboko vent (Belousov et al., 2015). The 118 Leningradskoye flow field contains mostly 'a'ā and the Toludskoye contains 'a'ā, pāhoehoe and 119 various transitional lava types (Belousov et al., 2015; Belousov & Belousova, 2017). The total 120 volume of lava produced from the TFE-50 eruption makes it one of the largest in history and one 121 of the most thermally radiant eruptions in the modern satellite era (Ramsey et al., 2019). This study 122 focuses specifically on the large, channelized lava flow that formed early in the eruption in the 123 Leningradskove flow field.

124 **2. FLOWGO model**

Lava flow modeling is a powerful tool for hazard mitigation and interpreting emplacement 125 126 processes as well as understanding the evolution of thermorheological properties of flowing lava. 127 One of the most extensive and widely utilized lava flow models is FLOWGO/PyFLOWGO (Table 128 2). The original FLOWGO model was recoded and updated in the Python scripting language to PyFLOWGO, which allows for improved iteration and customization (Chevrel et al., 2018). For 129 130 all modeling discussed throughout the rest of the manuscript, PyFLOWGO is used. As of 2023, 131 twenty-two peer-reviewed publications have used FLOWGO or PyFLOWGO to investigate both 132 active and inactive lava flows on Earth at a variety of locations. It has also been utilized to 133 investigate volcanism on four other planetary bodies (Table 2).

- 135
- 136 137
- 138
- 139

Study Locations	References
<u>Earth</u>	
Cameroon	(Wantim et al., 2013)
D.R. Congo	(Mossoux et al., 2016)
Galapagos	(Rowland et al., 2003)
Hawaiʻi	(Chevrel et al., 2018; Harris et al., 2022; Harris & Rowland, 2015, 2001; Mossoux et al., 2016; Riker et al., 2009; Robert et al., 2014; Rowland et al., 2005; Thompson & Ramsey, 2021)
Italy	(Harris et al., 2007, 2011; Wright et al., 2008)
Kamchatka	(Ramsey et al., 2019)
La Reunion	(Chevrel et al., 2018, 2022; Harris et al., 2016, 2019; Peltier et al., 2022; Rhéty et al., 2017)
<u>Planetary</u>	
Mars	(Flynn et al., 2022; Rowland et al., 2004)
Mercury	(Vetere et al., 2017)
Moon	(Lev et al., 2021)
Venus	(Flynn et al., 2023)

140 **Table 2**. Examples of studies employing FLOWGO/PyFLOWGO

141

142 FLOWGO, originally described in Harris and Rowland (2001) is a one-dimensional, 143 thermorheological model applicable to open channelized flows. It calculates the thermal budget 144 and resulting lava properties (i.e., core and surface temperature, and crystallinity) of a lava volume 145 down channel at each pre-defined interval step. At each step, the resulting depth-averaged viscosity 146 and velocity are obtained. The model is only applicable for cooling-limited flows and to the well-147 established channel region, and not the dispersed flow region that extends downslope beyond the 148 channel. For flows on Earth, the dispersed zone may be a region up to ~ 3 km beyond the end of 149 the channel (Dietterich & Cashman, 2014; Harris et al., 2022; Lipman & Banks, 1987). For 150 channelized flows on Mars, the dispersed zone may be up to ~49 km long (Flynn et al., 2022).

Thermal budgeting includes the radiative (Q_{rad}) heat loss from the flow surface, convective (Q_{conv}) heat loss to the atmosphere, conductive (Q_{cond}) heat loss to the channel walls and floor, and heat loss due to vaporization of precipitation (Q_{rain}) (where applicable). The heat gains are due to latent heat of crystallization (Q_{cryst}) and viscous dissipation (Q_{visc}) within the flowing lava. Under typical terrestrial conditions, heat loss from the modeled lava is dominated by radiative heat flux, which is a function of the temperature and effective emissivity of the lava's radiating surface (molten and crusted fractions) (Ramsey et al., 2019; Rowland et al., 2004).

158 PyFLOWGO makes five assumptions that define the model and where it is applicable. (1) 159 The lava flow velocity is defined by the effusion rate, which is held constant downflow, in a 160 channel with a defined depth and width (either estimated for an active flow or measured directly 161 on an older flow) on a given slope. (2) The lava flow must be confined to an open channel with no 162 continuous roofing or tube formation. (3) The vertical thermal structure of the lava is divided into 163 three layers: a cooler basal crust, a homogeneous high-temperature molten core, and a radiating 164 upper surface. (4) The model simulates the propagation of a channel-confined lava unhindered by the flow front or levee formation. (5) The flow is cooling- and not supply-limited. 165

As a cooling-limited flow slows down because of heat loss and increasing viscosity, it spreads laterally, commonly marking the end of the central channel, and will stop after it has cooled to an extent that its rheological behavior impedes forward motion (Chevrel et al., 2018). In practice, PyFLOWGO has one of three stopping conditions: (1) the modeled velocity reaches zero; (2) the modeled temperature of the flow core reaches the point of solidus; (3) the modeled yield strength of the flow core increases such that the flow is unable to advance. As the modeled velocity reaches zero the simulated channel width will increase substantially.

The main goal of this work is to investigate the effects of DEM resolution on 173 PyFLOWGO's results. The rheologic input parameters are the same as provided by Ramsey et al. 174 175 (2019) for the TFE-50 Leningradskoye channelized lava flow (Table 3), with the exception of the 176 lava's thermal emissivity module. As shown by Ramsey et al. (2019) and later by Thompson and 177 Ramsey (2021), PyFLOWGO is also sensitive to the assumed emissivity value chosen, with lava 178 flow runout distance varying by $\sim 6\%$. As part of this work, we also explore the effect of the three 179 different emissivity modules (where emissivity is considered constant, bimodal, and a function of 180 surface temperature) within PyFLOWGO and their effectiveness to reproduce the observed length 181 of a lava channel for the TFE-50 eruption. Between the three emissivity module options there is a 182 700 m (~6%) difference in modeled channel length. Full details of this investigation can be found 183 in the Supplemental Material. For the DEM analysis, we choose to use the variable emissivity 184 option because, similar to Thompson and Ramsey (2021), it appears to most accurately reproduce 185 a flow's emplacement compared to the other emissivity options in PyFLOWGO.

186 **3 Methods: Topographic Study**

187 Following the argument presented in Bilotta et al. (2019) for the MAGFLOW model, the 188 resolution of a DEM has both a direct and a secondary impact on modeling. The direct impact is 189 the resolution of the DEM, and the secondary impact is the model step size (i.e., how frequently 190 the model accounts for changes in topography). Both models (MAGFLOW and PyFLOWGO) 191 require topography and a step size. The model step size defines the distance (in meters) that the 192 simulated lava advances per each model iteration. PyFLOWGO allows the user to define a step 193 size that is independent of the DEM resolution. The influence of DEM resolution versus the model 194 step size is investigated using a convergence analysis (see section 3.2).

PyFLOWGO does not directly intake a DEM profile. It requires a slope transect that follows the path of the lava flow's central channel. For each DEM resolution, a slope map was created using ArcGIS v10.7 and the "Slope" tool.

198 **3.1 Topographic Data**

199 To assess the impact that DEM resolution has on any lava flow emplacement model, 200 numerous approaches are possible. For locations where multiple DEMs of different resolutions are 201 available, comparing the model outputs of each is possible (Stefanescu et al., 2012). The 202 generation of artificial terrain through Monte Carlo algorithms that control the variation and 203 amount of noise/error is another approach (Richardson & Karlstrom, 2019). For this analysis, a 204 deterministic approach similar to the method of Bilotta et al. (2019) was used. We used a high 205 resolution (5 m) DEM as the baseline and derived multiple lower-resolution DEMs (10, 15, 20, 206 30, 50, 100 and 200 m) for comparison. It is important to note, however, that a DEM degraded to 207 a lower resolution from a higher resolution DEM is not identical to a DEM produced at that same 208 spatial resolution. However, for this study, the smaller-scale differences between these two 209 approaches are not considered critical to the final model output.

The baseline topographic data pre-date the TFE-50 eruption and therefore represent the pre-flow topography. Colleagues (Viktor Dvigalo and Alexander Belousov) at the Institute of Volcanology and Seismology, Russia, generated the data necessary to produce the DEM using aerial images. The point cloud data provided were used to create the 5 m DEM with ArcGIS v10.7 and the "3D Analyst" toolbox, and the "Terrain to Raster" tool. This resolution was chosen because it is similar to the DEMs produced from CubeSat data and photogrammetry (i.e., Planet Labs) (Ghuffar, 2018). The moderate and low resolution DEMs represent common scales from other remote sensing data (Table 1). Lastly, for comparison we performed simulations on a constant slope that is the average value obtained on the 5 m DEM ($11.3^{\circ} \pm 0.11$) flow path transect. Using a constant slope is relevant because this approximation is commonly used for planetary lava flow modeling (e.g., Baloga & Glaze, 2008; Garry et al., 2007; Peters et al., 2021).

221 **3.2 Convergence Analysis**

222 A necessary step for assessing a model is a numerical convergence analysis. For 223 PyFLOWGO, a convergence analysis consists of varying the step size and assessing the value 224 returned for the variables of interest. Stabilization of the variable of interest within an acceptable 225 range determines whether the step size is sufficient. Step sizes were chosen to determine if there 226 is any relation between the employed step size and the resolution of the DEM. We therefore tested 227 step sizes of 1 m, 5 m, 10 m, 15 m, 30 m, 50 m, 100 m, and 200 m on the slope profiles extracted 228 from the 5 m reference DEM and from the lower resolution DEMs with pixel size of 15 m, 30 m, 229 200 m, as well as the constant slope profile. To assess the convergence analysis, the maximum 230 distance traveled by the channel and final lava core temperature are used. This convergence 231 analysis is similar to the one performed by Chevrel et al. (2018).

4 Results

4.1 Effects of DEM resolution on slope values

234 PyFLOWGO does not directly use a DEM to initiate the model but rather a 1D slope profile 235 that is derived from the DEM and drawn along the flow path. The elevation value of a pixel of the 236 DEM has a direct impact on the derived slope value, hence DEM resolution greatly matters (Chang 237 & Tsai, 1991). The focus of the analysis is on the change of slope values along the DEM transect 238 due to changing DEM resolutions. Statistics of the slope transects are shown in Table 4. As the 239 resolution of the DEM decreases (from 5 to 200 m pixel size), the average, maximum, standard 240 deviation, and variance of the slope decrease. A decreasing slope average from lower resolution 241 DEMs has been observed in previous studies (e.g., Chang & Tsai, 1991; Evans, 1980; Kienzle, 242 2004) and is well documented. The results here support these previous studies and reconfirm the 243 relationship between DEM resolution and derived slope values.

The slope values implemented in PyFLOWGO depend also on the step size (i.e., which effectively resamples the downflow slopes) so they are not always identical to the slope values derived from the topographic profile (see section 4.2). The resampled slope values nonetheless follow the same trend as DEM resolution decreases.

- 248
- 249
- 250
- 251

	5 m DEM Slope	10 m DEM Slope	15 m DEM Slope	20 m DEM Slope	30 m DEM Slope	50 m DEM Slope	100 m DEM Slope	200 m DEM Slope
Data Points (count)	3272	1640	1097	824	553	335	169	89
Average Slope (°)	11.4	11.4	7.70	7.01	6.39	5.91	5.60	5.60
Median Slope (°)	10.3	10.5	7.23	6.63	6.00	5.52	5.34	5.49
Minimum Slope (°)	1.19	3.03	1.16	0.69	1.00	1.49	2.20	2.43
Maximum Slope (°)	55.1	50.9	31.0	24.1	17.9	13.1	11.4	10.1
Standard Deviation (°)	6.07	5.09	3.65	3.27	2.87	2.41	2.01	1.87
Variance (°)	36.8	25.9	13.3	10.7	8.21	5.78	4.03	3.44

Table 4. Slope statistics from the channel transect for the eight DEM resolutions.

253

254 The distribution of slope values for each transect is a right skewed distribution (Figure 2a). 255 For the 15 m and lower resolution DEMs, as the DEM resolution decreases, the proportion of 256 higher slope values (>10°) significantly decreases (Figure 2b). These higher slope values are 257 averaged out as the DEM resolution decreases, whereas the proportion of moderate slope ($\leq 10^{\circ}$ 258 and $\geq 2^{\circ}$) values increases. As DEM resolution decreases, moderate resolution slopes become 259 dominant. This indicates that the higher slope values cover a proportionally smaller part of the 260 downslope transect than the moderate values. This trend is also reflected in the decreasing average 261 slope values (Table 4). In the transect used for this study, there is not a consistent relationship 262 between the proportion of moderate slopes and DEM resolution when considering the full range 263 of DEM resolutions.



265 Figure 2. (a) Distribution of DEM slope values for the eight DEM resolutions. (b) Slope values distributed into 266 three groups of low (<2°), moderate ($\leq 10^{\circ}$ and $\geq 2^{\circ}$), and high (>10°) values. Low slope (<2°) values are so few that 267 they do not appear on the graph.

268 **4.2 Convergence Analysis**

269 A convergence analysis was used to assess the impact of step size in relation to the DEM 270 resolution. Figure 3 shows how the final core temperature (K) and the final channelized flow 271 distance (km) vary with changing step size in the model.

272 As the step size decreases, the final core temperature generally decreases, stabilizing for a 273 step size of 5 m to 10 m. The final channelized flow length stabilizes at a step size of 10 m and 274 below for the DEM resolutions of 5 m, 15 m, and 30 m. However, for the 200 m and constant slope 275 a step size of 15 m can be used without significantly impacting the modeled channel length. Note 276 that the final channelized flow length does vary with DEM resolution (being higher for the 200 m 277 DEM than for the <30 m DEM) and will be discussed in section 4.3. The convergence analyses 278 for core temperature and channel length is consistent with Chevrel et al. (2018) that in most cases a step size of 10 m or less is preferred to ensure stabilization of the model. If a future study is 279 280 focused on core temperature, then a smaller step size may be needed. This may also be true for 281 other parameters (i.e., viscosity, crystal fraction, yield strength) and highlights the need for a 282 convergence analysis for any output parameter of interest. Other lava flow models that incorporate 283 a step size (i.e., MAGFLOW) have also determined a step size between 5 m and 10 m is optimal 284 (Bilotta et al., 2019). However, the smaller the step size, the longer the computation time, which 285 is also a function of the length of the lava flow modeled. If rapid results for hazard response are 286 required, the choice of step size may be a necessary consideration.





Figure 3. Convergence of the PyFLOWGO runs at 1, 5, 10, 15, 30, 50, 100, 200 m step size for the four different
 DEM derived slopes and the one constant slope (11.3°). The final channel length (bottom row) represents the distance
 the flow traveled once the velocity reaches zero.

288

293 If the step size is smaller than the resolution of the DEM, the model interpolates a profile 294 between the two points and calculates slope values for each step. If the model step size is larger 295 than the DEM resolution, the model averages over the slope values inside the step. Therefore, the 296 amount of topographic variability can also impact the choice of step size. If there is little 297 topographic variability (i.e., a smooth plain), then a larger step size could be used with potentially 298 minor impact on the model. However, if the topography is highly variable (i.e., valleys, obstacles, 299 etc.) then a smaller step size is required. To accurately and fully account for the topography present 300 in a transect, a step size equal to or smaller than the DEM resolution should be used. To allow for 301 a uniform comparison for the remainder of this manuscript, results using a 5 m step size are 302 presented for all DEM resolutions examined.

303 4.3 Modeled Channel Length

We define the baseline model using the pre-flow 5 m DEM and all rheological model inputs from Ramsey et al. (2019), excluding the variable emissivity module as discussed in the Supplemental Material. To initialize the model and match the observed flow length of 11.3 km, Ramsey et al. (2019) used an ASTER-derived 30 m DEM and an effusion rate of 278 m³/s. This initial effusion rate was taken from an estimation of the time averaged discharge rate (TADR) 309 obtained by the Middle Infrared Observation of Volcanic Activity (MIROVA) system (Coppola et 310 al., 2016). Here, using the new pre-flow 5 m DEM and variable emissivity module, we obtained 311 the desired channel length of 11.3 km for an effusion rate of 395 m^3/s . This value is slightly above 312 the estimation from MIROVA but is reasonable as it falls in the range determined for the early 313 phase of the eruption via field observations (aerial surveys) ($440 \text{ m}^3/\text{s}$), the MIROVA system (278) 314 m^{3}/s), and the TanDEM-X satellite (417 m^{3}/s) (Dvigalo et al., 2013; Kubanek et al., 2017; Ramsey 315 et al., 2019). The effusion rate of 395 m³/s is closer to the values of \sim 400 m³/s or more determined 316 by TanDEM-X and aero-photogrammetric observations that occurred during the first few days of 317 the eruption.

318 Varying the resolution of the DEM, all simulated flows traveled farther than the simulation 319 on the 5 m DEM for the same effusion rate (Figure 4). The simulation using the 10 m DEM resulted 320 in a 12.8 km flow (12% increase); the 15 m DEM resulted in a 12.5 km flow (10% increase); the 321 20 m DEM resulted in a 12.4 km flow (9% increase); the 30 m DEM resulted in a 11.6 km flow 322 (3% increase); the 50 m DEM resulted in a 11.5 km flow (1% increase); the 100 m DEM resulted 323 in a 13.1 km flow (14% increase); and the 200 m DEM resulted in a 16.2 km flow (35% increase). 324 The simulation on the constant slope the flow reached 17.0 km (40% increase) (Figure 4). All 325 model runs stopped because the flow velocity reached zero. Good model fits (<5% increase in flow 326 length) were obtained with the 5 m (baseline model), 30 m and 50 m DEMs. The 10 m, 15 m, 20 327 m, 100 m, 200 m, and constant slope had worse fits compared to the baseline model. Based on the 328 slope statistics in Table 4, specifically the decreasing trend in average slope values with decreasing 329 DEM resolution, the non-regular relationship between DEM resolution and modeled channel 330 length was not expected. Analyses of slope values at Tolbachik (Figure 2b) show that the 331 proportions of low, moderate, and high slopes do not systematically change with decreasing DEM 332 resolution and may have an effect on modeled channel length.

333 **4.4 Effusion Rate Variations**

Effusion rate is one input for PyFLOWGO (or any lava flow model) that greatly influences lava flow length but is subject to large uncertainty (Harris et al., 2007; Rowland et al., 2005). An effusion rate is typically calculated indirectly from satellite thermal data, or directly from observations made in the field, and used in the model to match a defined channel/flow length or area. To assess the relationship between effusion rate and the resolution of the DEM, PyFLOWGO was run iteratively with different effusion rates for all seven DEM resolutions plus the constant slope to match the 11.3 km channel length (Figure 5). All other input parameters remained
constant, including the 5 m step size, for all DEM resolutions. The 5 m DEM is the baseline model
as defined in section 4.3.

343 Figure 5 shows results for effusion rates for the eight DEM resolutions; these follow a non-344 regular trend, similar to the channel length results shown in Figure 4. Effusion rates similar to the 345 baseline model at Tolbachik were found for the 30 and 50 m DEMs, whereas significantly lower 346 values for the 10 m, 15 m, 30 m, 100 m and 200 m DEMs are needed to match the final channel 347 length. This pattern is attributed to the decrease in topographic variability of the Tolbachik slope 348 transect (Table 4 and Figure 2). For a low-resolution DEM (100 m and 200 m) or constant slope, 349 there is substantially less topographic variability expressed in the transect. A markedly smaller 350 effusion rate is necessary to reach the 11.3 km distance. With less topographic variability 351 influencing the modeled flow, a lower effusion rate can therefore produce a lava flow of the same 352 length. This could potentially lead to an underestimation of the effusion rate when using the model 353 with lower resolution DEMs (e.g., ≥ 100 m) to determine a flow's emplacement conditions.

For many terrestrial volcanic eruptions, effusion rates spike early then follows an 354 355 exponential decay (e.g., Bonny et al., 2018; Harris et al., 2000; Ramsey et al., 2019; Wadge, 1981; Wright et al., 2001). Most channelized lava flows are formed during this early period in the 356 357 eruption (Rowland et al., 2005). The average initial effusion rate determined for 27 - 29 November 358 2012 from field observations at Tolbachik (i.e., aerial surveys) was ~400 m³/s (Dvigalo et al., 359 2014; Kubanek et al., 2017). The observed flow length of 11.3 km occurred on 1 December 2012, 360 early in the eruption. Using the higher resolution topographic data required a higher effusion rate 361 to reach the same distance (Figure 5). In other words, the estimate of the effusion rate that produced 362 a given flow should improve with higher resolution topography.



363

Figure 4. Model runout distances at a constant effusion rate (395 m³/s) for eight DEM resolutions, and a constant slope. The black line represents lava velocity in the channel as a function of distance from the source. The red dotted line is the slope profile. The grey vertical line in the baseline model plot is the 11.3 km flow length observed on 1 December 2012, and the grey regions indicate the difference between the flow length of baseline model and the relevant model case. All model results shown here used a 5 m step size.



Figure 5. Required effusion rates as a function of DEM resolution to reach the 11.3 km channel length for the 5 m
(395 m³/s), 10 m (341 m³/s), 15 m (342 m³/s), 20 m (353 m³/s), 30 m (384 m³/s), 50 m (391 m³/s), 100 m (325 m³/s)
and 200 m (249 m³/s) model runs, and for the constant slope (11.3°) (248 m³/s). All model results shown here used a
5 m step size.

376

377 4.5 PyFLOWGO Velocity

378 PyFLOWGO accounts for the change in topography through a modified version of Jeffreys 379 equation to determine the flow velocity (Moore, 1987). To assess the lack of consistent channel 380 length and effusion rate trend with decreasing DEM resolution observed in Figure 4 and 5, we next 381 divided each modeled flow into three segments (proximal, medial, and distal) to compare changes 382 in flow velocity as a result of the DEM resolution in those segments (Table 5). This was intended 383 to explore how the distribution of slopes downflow might affect model results for different DEM 384 resolutions as the higher slopes are reduced/smoothed in lower resolution DEMs. Proximal 385 represents the first 10% of the channel length, medial the middle 65%, and distal the final 25%. 386 These percentages are similar to those used for terrestrial and Martian lava flows in prior studies 387 (Garry et al., 2007; Peitersen & Crown, 1999). The constant slope model run is not assessed 388 because variations in topography are not present.

389

Table 5: Average modeled velocity for the proximal, medial, and distal flow portions. The last two columns are the

	Modeled Channel Velocity (m/s)						
DEM Resolution	Proximal (first 10%)	Medial (middle 65%)	Distal (final 25%)	Average Over Channel Length	Median Over Channel Length		
5 m	1.68	1.07	0.27	0.92	0.76		
10 m	1.87	1.12	0.34	0.99	0.89		
15 m	1.95	1.12	0.30	0.99	0.85		
20 m	1.88	1.09	0.25	0.96	0.85		
30 m	1.69	1.01	0.25	0.88	0.72		
50 m	1.55	0.96	0.23	0.83	0.61		
100 m	1.75	1.08	0.22	0.93	0.74		
200 m	2.30	1.22	0.24	1.08	0.91		

392 average and median flow velocity over the entire modeled channel length.

393

394 There is a decrease in the average and median flow velocities for the 10 m to 50 m DEM 395 resolutions (Table 5). The same trend is not fully observed in the proximal, medial, or distal 396 regions. There is an increase in velocity in the 10, 15, and 20 m DEM results for the proximal, 397 medial, average, and median relative to the 5 m DEM results. For the distal region, the increase is 398 seen in the 10 and 15 m results and not for the 20 m DEM. These trends follow the lack of 399 consistent relationships with DEM resolution for channel length and effusion rate and are 400 attributed to the specific topographic characteristics of the Tolbachik slope transect that influences 401 flow velocity.

402 The decrease in flow velocity is attributed to the change in topographic variability at 403 different locations along the slope transect (Table 4 and Figure 4). The slope transect used for the 404 modeling contained large topographic changes that take up a proportionally smaller area than do 405 the small to moderate changes (Figure 2). As large topographic changes (and by extension large 406 slopes) are lost in the lower resolution DEMs, the flow is unable to maintain the same velocity to 407 allow it to reach the same length as those derived from using the higher resolution DEMs. For high 408 to moderate resolution DEMs (10 to 50 m), the fewer large slope changes in the transect leads to 409 a lower average flow velocity. However, for the low resolution DEMs (100 m and 200 m) and 410 constant slope there is an increase in both flow length and velocity in comparison to the moderate 411 resolution DEMs (Figure 4 and Table 5). With these lower resolution DEMs, the topography has

412 smoothed to the point where there is little to no variability left to influence the final length (Table 413 4 and Figure 2). Although there are not high slope values to increase velocity, there are also not 414 the corresponding decreases in slope that reduce velocity. The lower resolution DEMs can 415 maintain a higher velocity and thus a longer flow distance.

For the case shown here, topographic effects and the resulting changes in velocity of the modeled lava flow might be site specific to the Tolbachik volcanic complex. These results highlight the importance for future studies to examine the magnitude and distribution of slope elements at the scale of the DEM to assess how they may influence the modeling results.

420

421 **5 Discussion**

422 The resolution of the DEM used for PyFLOWGO modeling has a measurable impact on 423 the resulting channel length. These findings differ from Harris et al. (2016) who used two different 424 topographic datasets, a 30 m DEM from the SRTM and a 10 m DEM produced from LIDAR, to 425 compare the effect of different DEM resolutions on the FLOWGO model for a channelized lava 426 flow from the December 2010 eruption of Piton de la Fournaise (Harris et al., 2016). Their study 427 found that there is little difference between the two resolutions but did not elaborate on the details, 428 since the focus of the study was on comparing field measurements to model results and not a 429 detailed topographic sensitivity analysis. Comparing the results here for only the 30 m and 10 m 430 DEMs, the length difference is 1.16 km or 9.5%, a potentially significant difference for lava flow 431 hazard assessments and maps.

432 The changes in topographic variability related to the DEM resolutions and the effect on the 433 calculated velocity partially explains the trend in flow lengths (Figure 2, Figure 4, and Table 5). 434 However, we cannot rule out the possibility that the trend in channel length may be impacted by 435 specific aspects of the topography at Tolbachik. The slope profile used in the study shows large 436 variations near the proximal and distal end of the flow (Figure 4). These variations in slope are not 437 fully averaged out except in the 100 m and 200 m DEM (Figure 2). Previous studies have shown 438 that changes in topography at different points along a flow's emplacement can impact the final 439 flow length and morphology (Flynn et al., 2021; Gregg & Fink, 2000; Guest et al., 1987). 440 Assessing how different unique combinations of topographic variability impact lava flows 441 emplacement is outside the scope of this work but should be further investigated.

Results from the topographic sensitivity analysis indicate that using a higher resolution DEM requires a higher effusion rate to model the same channel length especially for regions with large pre flow slope variability. Moderate to low resolution DEMs will underestimate the modeled effusion rate in these same circumstances. The remainder of the discussion centers on the implications of using different DEM resolutions for modeling both active and inactive lava flows.

447 **5.1 Active Flows**

448 PyFLOWGO is increasingly used to make hazard assessments for new volcanic events 449 within minutes to hours of an eruption occurring (Chevrel et al., 2022; Harris et al., 2019; Peltier 450 et al., 2021, 2022). In these cases, lava flow composition (i.e., rheological parameters) is usually 451 determined based on past eruptions at that volcano. The two remaining inputs needed for the model 452 are the effusion rate and the topography. Effusion rate for active eruptions is commonly calculated 453 from repeat visible, thermal, or radar satellite data (Harris et al., 2007 and methods described 454 within). Common tools for determining effusion rates from satellite data are the MIROVA 455 (Coppola et al., 2016), HOTVOLC (Gouhier et al., 2016), and HOTSAT (Ganci et al., 2011) 456 monitoring systems and data from the TanDEM-X satellite (Kubanek et al., 2021). Our results 457 indicate that using the highest resolution DEM available, with an effusion rate from early in the 458 eruption, produces the best fit to the observed channel length (provided the model is calibrated to 459 that DEM resolution and chosen model step size as we show here). In an ideal situation, a high-460 resolution topographic dataset (i.e., 10 m DEM or better) is available coupled with effusion rate 461 measurements made as soon as possible at the start of the eruption. However, if a study uses a 462 moderate resolution DEM in combination with PyFLOWGO, an overestimate of the final channel 463 length is possible depending on the pre-flow topography.

464 For some volcanoes (e.g., Etna, Kīlauea, Piton de la Fournaise), a 5 m (or better) DEM may 465 be available. However, for many other volcanoes, especially those in remote locations, high 466 resolution DEMs are not readily available or feasible to acquire. In those cases, a moderate 467 resolution DEM (i.e., 30 m), such as the SRTM DEM or ASTER global DEM (GDEM) are freely 468 available and provide global coverage. However, the SRTM DEM provides a snapshot of 469 topography from February 2000, potentially missing important topographic changes since that 470 time (van Zyl, 2001). In contrast, version 3 of the ASTER GDEM is more current, but averages 471 together ASTER individual scene DEMs from 2000-2011. Averaging scenes together for the 472 GDEM does produce a more accurate DEM, devoid of clouds and other errors, but it also averages

any topographic change during that period. Alternatively, an ASTER individual scene DEM (30
m/pixel) could be used. However, as highlighted in Flynn & Ramsey (2020), these scenes can
contain substantial amounts of noise or interference from clouds and shadowing, despite being
more representative of recent topographic change.

477 The impact of noise (and/or rapidly changing topography) in a DEM could be reduced 478 using the "slope smoothing" function in PyFLOWGO. This function interpolates a line over the 479 DEM based on a set number of points, defined by an individual before the model starts. It is 480 important to note that, although using this function may reduce noise in a transect, it also removes 481 naturally occurring topographic features smaller than the smoothing function. As highlighted in 482 Harris et al. (2019) and Chevrel et al. (2022), calibration of PyFLOWGO for a given DEM 483 resolution and step size is mandatory before using it for any hazard assessment. This ensures that 484 the modeled lava flow distance for a given effusion rate is as accurate as possible.

485 **5.2 Inactive Flows**

486 PyFLOWGO can also be used to investigate the evolution of the thermorheological properties of already emplaced/inactive flows on Earth and other planetary bodies (cf. Table 2) 487 488 (e.g., Lev et al., 2021; Ramsey et al., 2019; Rowland et al., 2004). Morphological parameters of 489 terrestrial lava flows and rheological properties of the lava can be established through field 490 campaigns and sample analysis, respectively. However, for flows on other planetary bodies, 491 rheological conditions typically are assumed using an Earth analog or modeling (Chevrel et al., 492 2014). As discussed in Section 1, DEM resolution is limited for other planetary bodies, and pre-493 flow topography has not been available. Therefore, post-emplacement topography is assumed to 494 be a suitable proxy.

495 Comparing the results for the 200 m DEM (the same resolution as the MOLA/HRSC global 496 DEM for Mars) to the results for the constant slope, the modeled channel length difference is 850 497 m (5%). This is a potentially significant difference where attempting to reproduce very long (e.g., 498 100s of km) channelized lava flows observed on Mars or Venus. However, the difference in 499 effusion rate required to model a given flow using the 200 m DEM and constant slope scenarios is 500 negligible 0.4% (Figure 5). In order to apply PyFLOWGO to planetary lava flows the use of lower 501 resolution DEMs or a constant slope is commonly required and will introduce uncertainty into the 502 results. Results presented here quantify that uncertainty, which can aid future applications to 503 planetary lava flows.

A potentially important factor typically overlooked in studies that use a constant slope for lava flow modeling is the value chosen. As shown in Table 4, as the resolution of the DEM decreases the average slope value also decreases and becomes less representative of the local topography. Figure 6 shows that the change in measured slope value relates to the resolution of the topographic dataset using data commonly available on Mars (i.e., a CTX and MOLA/HRSC DEM).





Figure 6: (a) A CTX image (P02_001775_1593) of a channelized lava flow located south of Arsia Mons, Mars. The central channel has been filled with a secondary lava flow, which distinctly outlines its path. (b) CTX slope map of the same location in (a) and the black line indicating the location of the central channel. (c) MOLA/HRSC slope map, derived from the MOLA/HRSC DEM. (d) Histogram distribution of slope values along the black line in (b) and (c). The average value for the CTX and MOLA/HRSC slope transects were 3.92° and 0.14°, respectively.

518 Previous modeling of Martian lava flows has used a constant slope (i.e., the standard 519 rheologic approach described in Hiesinger et al., 2007). This value is usually derived from HRSC 520 or MOLA data (e.g., Hiesinger et al., 2007; Pasckert et al., 2012; Peters et al., 2021). As shown in 521 Table 4, Figure 2, and Figure 6, the higher resolution DEMs can provide a large range of slope 522 values dependent on the resolution of the topographic dataset. This range in slope values can have 523 a quantifiable effect on modeling results for effusion rate, viscosity, and yield strength (Russo et 524 al., 2022). However, using a constant slope derived from the regional topography may be the best 525 option if no pre-flow topography is available.

526 To assess the effects of the constant slope values we perform an additional model run using 527 the average slope value derived from the 200 m DEM (5.6°) (Table 4). We compare the 5.6° 528 constant slope model run to those from the 11.3° constant slope results. Our results show that the 529 differences between a simulation on a constant slope of 5.6° or 11.3° is only 960 m (5%). Given 530 the large (nearly two times) difference in average slope value, this is a relatively minor difference 531 in distance. Although using a constant slope for lava flow modeling is not optimal, given the 532 limitations of planetary datasets, errors related to this approximation are acceptable for a first order 533 estimation of the lava flow emplacement dynamics.

534 6 Conclusions

The main objective of this work was to investigate the effect of DEM resolution on PyFLOWGO modeling. We used the 11.3 km-long lava flow emplaced during the Tolbachik 2012-2013 eruption as a reference and the same PyFLOWGO rheologic input parameters as provided by Ramsey et al. (2019) with the exception of the emissivity model for that same flow. Our approach consisted of comparing PyFLOWGO results on DEMs of decreasing resolution (from 5 m to 200 m).

541 Using a convergence analysis, we emphasize the importance of choosing an appropriate 542 model step size to account for topography. In agreement with Chevrel et al. (2018) we show that 543 a step size of 10 m or smaller should be used for a DEM with resolutions between 5 and 200 m. 544 Choosing an appropriate model step size in relation to the DEM resolution is a necessary step to 545 ensure accurate model results.

The topographic sensitivity analysis results indicate that DEM resolution is an important parameter to consider with PyFLOWGO. Using a moderate to low resolution (~10 m to ~200 m) DEM overestimates the channelized flow length, as does using a constant slope equal to the

549 average slope value. In addition, assessing the level of topographic variability in a modeled lava 550 flows path is an important consideration. This information supports the fact that regardless of the 551 level of complexity in a lava flow model, topography and its accuracy are critical parameters. 552 Studies using PyFLOWGO for active lava flow emplacement should strive to use the most recent 553 pre-flow DEM, especially for cases where the topography is frequently changing. If moderate to 554 low resolution DEMs are the only available options, either the effusion rate will be underestimated, 555 or the final channel length overestimated. However, where applying PyFLOWGO to inactive lava 556 flows (on Earth or other planetary bodies), a moderate to low resolution DEM may be the only 557 option. Interpreting these model results should be done with the expectation of higher error rates 558 in either the effusion rate or modeled channel length.

With the wide range of applications for PyFLOWGO, across multiple planetary bodies, understanding the impact of topographic datasets resolution is important for accurate modeling results. The topographic sensitivity analysis presented here provides useful information that can be used to improve the application of PyFLOWGO for hazard assessments and investigation into the emplacement of channelized flows on Earth and other planetary bodies.

564

565 Acknowledgments and Data Availability Statement

566 This research was supported through the NASA Solar System Workings (SSW) program (grant 567 number: 80NSSC19K0547). The authors would like to thank Dave Hyman and an anonymous 568 reviewer for their insightful reviews. The authors would also like to thank Andy Harris for 569 constructive input regarding FLOWGO. Thank you to Viktor Dvigalo and Alexander Belousov 570 for providing the Tolbachik DEM and to Dan Berman for generating the CTX DEM. All Planet 571 data were supplied through their Education and Research program. The PyFLOWGO model is 572 available for download at https://github.com/pyflowgo. PyFLOWGO results can be found at Flynn 573 (2023). This is a Laboratory of Excellence ClerVolc contribution no°594.

574 **References**

- Baloga, S. M., & Glaze, L. S. (2008). A self-replication model for long channelized lava flows
 on the Mars plains. *Journal of Geophysical Research E: Planets*, *113*(5), 1–15.
 https://doi.org/10.1029/2007JE002954
- Belousov, A., & Belousova, M. (2017). Dynamics and viscosity of 'a'a and pahoehoe lava flows
 of the 2012–2013 eruption of Tolbachik volcano, Kamchatka (Russia). *Bulletin of Volcanology*, 80(1). https://doi.org/10.1007/s00445-017-1180-2
 - 24

- 581 Belousov, A., Belousova, M., Edwards, B., Volynets, A., & Melnikov, D. (2015). Overview of
- the precursors and dynamics of the 2012-13 basaltic fissure eruption of Tolbachik Volcano,
 Kamchatka, Russia. *Journal of Volcanology and Geothermal Research*, 307, 22–37.
 https://doi.org/10.1016/j.jvolgeores.2015.06.013
- Bilotta, G., Cappello, A., Hérault, A., & Del Negro, C. (2019). Influence of topographic data
 uncertainties and model resolution on the numerical simulation of lava flows. *Environmental Modelling and Software*, *112*(November 2018), 1–15.
- 588 <u>https://doi</u>.org/10.1016/j.envsoft.2018.11.001
- Bonny, E., Thordarson, T., Wright, R., Höskuldsson, A., & Jónsdóttir, I. (2018). The Volume of
 Lava Erupted During the 2014 to 2015 Eruption at Holuhraun, Iceland: A Comparison
 Between Satellite- and Ground-Based Measurements. *Journal of Geophysical Research:*Solid Earth, 123(7), 5412–5426. https://doi.org/10.1029/2017JB015008
- Breton, S., Quantin-Nataf, C., Bodin, T., Loizeau, D., Volat, M., & Lozac'h, L. (2019). Semiautomated crater depth measurements. *MethodsX*, 6(May), 2293–2304.
 https://doi.org/10.1016/j.mex.2019.08.007
- 596 Chang, K. T., & Tsai, B. W. (1991). The effect of dem resolution on slope and aspect mapping.
 597 *Cartography and Geographic Information Systems*, 18(1), 69–77.
 598 https://doi.org/10.1559/152304091783805626
- Chevrel, M. O., Baratoux, D., Hess, K. U., & Dingwell, D. B. (2014). Viscous flow behavior of
 tholeiitic and alkaline Fe-rich martian basalts. *Geochimica et Cosmochimica Acta*, *124*,
 348–365. https://doi.org/10.1016/j.gca.2013.08.026
- 602 Chevrel, M. O., Labroquere, J., Harris, A. J. L., & Rowland, S. K. (2018). PyFLOWGO : An
 603 open-source platform for simulation of channelized lava 25cience-rheological properties,
 604 *111*(November 2017), 167–180. https://doi.org/10.1016/j.cageo.2017.11.009
- 605 Chevrel, M. O., Favalli, M., Villeneuve, N., Harris, A. J. L., Fornaciai, A., Richter, N., et al.
 606 (2021). Lava flow hazard map of Piton de la Fournaise volcano. *Natural Hazards and Earth*607 *System Sciences*, 21(8), 2355–2377. https://doi.org/10.5194/nhess-21-2355-2021
- Chevrel, M. O., Harris, A., Peltier, A., Villeneuve, N., Coppola, D., Gouhier, M., & Drenne, S.
 (2022). Volcanic crisis management supported by near real-time lava flow hazard
 assessment at Piton de la Fournaise, La Réunion. *Volcanica*, 5(2), 313–334.
 https://doi.org/10.30909/vol.05.02.313334
- 612 Churikova, T. G., Gordeychik, B. N., Edwards, B. R., Ponomareva, V. v., & Zelenin, E. A.
- 613 (2015). The Tolbachik volcanic massif: A review of the petrology, volcanology and
 614 eruption history prior to the 2012-2013 eruption. *Journal of Volcanology and Geothermal*615 *Research*, 307, 3–21. https://doi.org/10.1016/j.jvolgeores.2015.10.016
- 615 *Research*, 507, 5–21. <u>https://doi</u>.org/10.1016/J.Jvolgeores.2013.10.016
 616 Coppola, D., Laiolo, M., Cigolini, C., Donne, D. D., & Ripepe, M. (2016). Enhanced volcanic
- hot-spot detection using MODIS IR data: results from the MIROVA system. *Geological Society, London, Special Publications, 426*(1), 181–205. https://doi.org/10.1144/SP426.5
- Dietterich, H. R., & Cashman, K. V. (2014). Channel networks within lava flows: Formation,
 evolution, and implications for flow behavior. *Journal of Geophysical Research: Earth Surface*, *119*, 1704–1724. https://doi.org/10.1002/2013JF002871.
- Dvigalo, V. N., Svirid, I. Yu., & Shevchenko, A. V. (2014). The first quantitative estimates of
 parameters for the tolbachik fissure eruption of 2012-2013 from aerophotogrammetric
 observations. *Journal of Volcanology and Seismology*, 8(5), 261–268.
- 625 <u>https://doi</u>.org/10.1134/S0742046314050029

- Evans, I. S. (1980). An integrated system of terrain analysis and slope mapping. *Zeitschrift Fur Geomorphologie*, *36*, 274–295.
- Farr, T. G., Rosen, P. A., Caro, E., Crippen, R., Duren, R., Hensley, S., et al. (2007). The shuttle
 radar topography mission. *Reviews of Geophysics*, 45(2).
- Favalli, M., Pareschi, M. T., Neri, A., & Isola, I. (2005). Forecasting lava flow paths by a
 stochastic approach. *Geophysical Research Letters*, *32*(3), 1–4.
 https://doi.org/10.1029/2004GL021718
- Favalli, M., Tarquini, S., & Fornaciai, A. (2011). Downflow code and lidar technology for lava
 flow analysis and hazard assessment at mount etna. *Annals of Geophysics*, 54(5), 552–566.
 https://doi.org/10.4401/ag-5339
- Favalli, M., Tarquini, S., Papale, P., Fornaciai, A., & Boschi, E. (2012). Lava flow hazard and
 risk at Mt. Cameroon volcano. *Bulletin of Volcanology*, *74*(2), 423–439.
 https://doi.org/10.1007/s00445-011-0540-6
- Fedotov, S. A., Flerov, G. B., & Chirkov, A. M. (1984). The 1975–1976 Large Tolbachik Fissure
 Eruption in Kamchatka. *26cience, Moscow (637 Pp.)*.
- Fergason, R. L., Hare, T. M., & Laura, J. (2018). HRSC and MOLA blended digital elevation
 model at 200m v2, astrogeology PDS annex. US Geological Survey.
- Flynn, Ian. T. W., Chevrel, Magdalena. O., & Ramsey, Michael. S. (2023). Adaptation of a
 thermorheological lava flow model for Venus conditions. *Journal of Geophysical Research: Planets*. https://doi.org/10.1029/2022JE007710
- Flynn, Ian. (2023). Data for: "The effects of DEM resolution on the PyFLOWGO
 thermorheological lava flow model" paper [Data set]. Zenodo.
 https://doi.org/10.5281/zenodo.8021357
- Flynn, I. T. W., Crown, D. A., & Ramsey, M. S. (2022). Determining Emplacement Conditions
 and Vent Locations for Channelized Lava Flows Southwest of Arsia Mons. *Journal of Geophysical Research: Planets*, *127*(11). https://doi.org/10.1029/2022JE007467
- Flynn, I T W., Crown, D. A., & Ramsey, M. S. (2021). The Effects of DEM Resolution on
 Planetary Thermo-Rheological Lava Flow Modeling. In *52nd Lunar and Planetary Science Conference* (p. 1305).
- Flynn, Ian T.W., & Ramsey, M. S. (2020). Pyroclastic density current hazard assessment and
 modeling uncertainties for Fuego volcano, Guatemala. *Remote Sensing*, 12(17).
 https://doi.org/10.3390/RS12172790
- Ford, P. G., & Pettengill, G. H. (1992). Venus topography and kilometer-scale slopes. *Journal of Geophysical Research*, 97(E8), 103–114. https://doi.org/10.1029/92je01085
- Ganci, G., Vicari, A., Fortuna, L., & del Negro, C. (2011). The HOTSAT volcano monitoring
 system based on combined use of SEVIRI and MODIS multispectral data. *Annals of Geophysics*, 54(5), 544–550. https://doi.org/10.4401/ag-5338
- Ganci, G., Cappello, A., Bilotta, G., & Del Negro, C. (2020). How the variety of satellite remote
 sensing data over volcanoes can assist hazard monitoring efforts: The 2011 eruption of
 Nabro volcano. *Remote Sensing of Environment*, 236(September 2019), 111426.
 https://doi.org/10.1016/j.rse.2019.111426
- 667 Garry, W. B., Zimbelman, J. R., & Gregg, T. K. P. (2007). Morphology and emplacement of a
 668 long channeled lava flow near Ascraeus Mons Volcano, Mars. *Journal of Geophysical*669 *Research E: Planets*, 112(8), 1–21. https://doi.org/10.1029/2006JE002803
- 670 Ghuffar, S. (2018). DEM generation from multi satellite Planetscope imagery. *Remote Sensing*,
- 671 *10*(9), 1–22. https://doi.org/10.3390/rs10091462

- Glaze, L. S., & Baloga, S. M. (2007). Topographic variability on Mars: Implications for lava
 flow modeling. *Journal of Geophysical Research E: Planets*, *112*(8), 1–9.
 https://doi.org/10.1029/2006JE002879
- Gouhier, M., Guéhenneux, Y., Labazuy, P., Cacault, P., Decriem, J., & Rivet, S. (2016).
 HOTVOLC: A web-based monitoring system for volcanic hot spots. *Geological Society*, *London, Special Publications*, 426(1), 223–241.
- 678 Gregg, T. K. P., & Fink, J. H. (2000). A laboratory investigation into the effects of slope on lava
 679 flow morphology. *Journal of Volcanology and Geothermal Research*, *96*(3–4), 145–159.
 680 https://doi.org/10.1016/S0377-0273(99)00148-1
- Guest, J. E., Kilburn, C. R. J., Pinkerton, H., & Duncan, A. M. (1987). The evolution of lava
 flow-fields: observations of the 1981 and 1983 eruptions of Mount Etna, Sicily. *Bulletin of Volcanology*, 49(3), 527–540.
- Harris, A, Murray, J. B., Aries, S. E., Davies, M. A., Flynn, L. P., Wooster, M. J., et al. (2000).
 Effusion rate trends at Etna and Krafla and their implications for eruptive mechanisms. *Journal of Volcanology and Geothermal Research*, 102(3–4), 237–269.
- 687 https://doi.org/10.1016/S0377-0273(00)00190-6
- Harris, A. J. L., Dehn, J., & Calvari, S. (2007). Lava effusion rate definition and measurement: A
 review. *Bulletin of Volcanology*, 70(1), 1–22. https://doi.org/10.1007/s00445-007-0120-y
- Harris, Andrew, & Rowland, S. K. (2015). FLOWGO 2012, An Updated Framework for
 Thermorheological Simulations of Channel-Contained Lava. *Hawaiian Volcanoes: From Source to Surface, Geophysical Monograph Series, 208, 457–481.*
- Harris, Andrew, & Rowland, Scott. K. (2001). FLOWGO: a kinematic Thermo-rheological
 model for lava cooling in a channel. *Bulletin of Volcanology*, *63*, 20–44.
- Harris, Andrew, Favalli, M., Mazzarini, F., & Pareschi, M. T. (2007). Best-fit results from
 application of a thermo-rheological model for channelized lava flow to high spatial
 resolution morphological data. *Geophysical Research Letters*, 34(1), 1–5.
 https://doi.org/10.1029/2006GL028126
- Harris, Andrew, Favalli, M., Wright, R., & Garbeil, H. (2011). Hazard assessment at Mount Etna using a hybrid lava flow inundation model and satellite-based land classification. *Natural Hazards*, 58(3), 1001–1027. https://doi.org/10.1007/s11069-010-9709-0
- Harris, Andrew, Rhéty, M., Gurioli, L., Villeneuve, N., & Paris, R. (2016). Simulating the
 thermorheological evolution of channel-contained lava: FLOWGO and its implementation
 in EXCEL. *Geological Society Special Publication*, 426(1), 313–336.
 https://doi.org/10.1144/SP426.9
- Harris, Andrew, Chevrel, M., Coppola, D., Ramsey, M., Hrysiewicz, A., Thivet, S., et al. (2019).
 Validation of an integrated satellite-data-driven response to an effusive crisis: the April–
 May 2018 eruption of Piton de la Fournaise. *Annals of GeophysicsAnnals of Geophysics*,
 61(Vol 61 (2018)). https://doi.org/10.4401/ag-7972
- Harris, Andrew., Rowland, S., & Chevrel, M. O. (2022). The anatomy of a channel-fed 'a'ā lava fow system. *Bulletin of Volcanology*.
- Herrick, R. R., Stahlke, D. L., & Sharpton, V. L. (2012). Fine-scale Venusian topography from
 Magellan stereo data. *Eos*, 93(12), 125–126. https://doi.org/10.1029/2012EO120002
- Hiesinger, H., Head, J., & Neukum, G. (2007). Young lava flows on the eastern flank of
- 715 Ascraeus Mons: Rheological properties derived from High Resolution Stereo
- 716 Camera(HRSC) images and Mars Orbiter Laser Altimeter(MOLA) data. *Journal of*
- 717 *Geophysical Research E: Planets*, *112*(5). https://doi.org/10.1029/2006JE002717

- Hirano, A., Welch, R., & Lang, H. (2003). Mapping from ASTER stereo image data: DEM
 validation and accuracy assessment. *ISPRS Journal of Photogrammetry and Remote*
- 720 Sensing, 57(5–6), 356–370. https://doi.org/10.1016/S0924-2716(02)00164-8
- Jaumann, R., Neukum, G., Behnke, T., Duxbury, T. C., Eichentopf, K., Flohrer, J., et al. (2007).
 The high-resolution stereo camera (HRSC) experiment on Mars Express: Instrument aspects and experiment conduct from interplanetary cruise through the nominal mission. *Planetary and Space Science*, 55(7–8), 928–952. https://doi.org/10.1016/j.pss.2006.12.003
- Kienzle, S. (2004). The effect of DEM raster resolution on first order, second order and compound terrain derivatives. *Transactions in GIS*, 8(1), 83–111.
- 727 https://doi.org/10.1111/j.1467-9671.2004.00169.x
- Kubanek, J., Richardson, J. A., Charbonnier, S. J., & Connor, L. J. (2015). Lava flow mapping
 and volume calculations for the 2012–2013 Tolbachik, Kamchatka, fissure eruption using
 bistatic TanDEM-X InSAR. *Bulletin of Volcanology*, 77(12), 1–13.
 https://doi.org/10.1007/s00445-015-0989-9
- Kubanek, J., Westerhaus, M., & Heck, B. (2017). TanDEM-X Time Series Analysis Reveals
 Lava Flow Volume and Effusion Rates of the 2012–2013 Tolbachik, Kamchatka Fissure
 Eruption. *Journal of Geophysical Research: Solid Earth*, *122*(10), 7754–7774.
 https://doi.org/10.1002/2017JB014309
- Kubanek, J., Poland, M. P., & Biggs, J. (2021). Applications of bistatic radar to volcano
 topography-a review of ten years of TanDEM-X. *IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing*, 14, 3282–3302.
 <u>https://doi.org/10.1109/JSTARS.2021.3055653</u>
- Lee, R. J., & Ramsey, M. S. (2016). What is the emissivity of active basaltic lava flows.
 Proceedings of the AGU Fall Meeting, San Francisco, CA, USA, 12–16.
- Lev, E., Hamilton, C. W., Voigt, J. R. C., Stadermann, A. C., Zhan, Y., & Neish, C. D. (2021).
 Emplacement conditions of lunar impact melt flows. *Icarus*, *369*(June).
 https://doi.org/10.1016/j.icarus.2021.114578
- Lipman, P. W., & Banks, N. (1987). A'a flow dynamics, 1984 Mauna Loa eruption. Volcanism *in Hawaii*, (May), 43.
- Moore, H. J. (1987). Preliminary estimates of the rheological properties of 1984 Mauna Loa
 lava. US Geol Surv Prof Pap, 1350(99), 1569–1588.
- Mossoux, S., Saey, M., Bartolini, S., Poppe, S., Canters, F., & Kervyn, M. (2016). Q-LAVHA: A
 flexible GIS plugin to simulate lava flows. *Computers and Geosciences*, 97(September),
 98–109. https://doi.org/10.1016/j.cageo.2016.09.003
- Pasckert, J. H., Hiesinger, H., & Reiss, D. (2012). Rheologies and ages of lava flows on Elysium
 Mons, Mars. *Icarus*, 219(1), 443–457. https://doi.org/10.1016/j.icarus.2012.03.014
- Peitersen, M., & Crown, D. A. (1999). Downflow width behavior of Martian and terrestrial lava
 flows. *Journal of Geophysical Research*, *104*, 8473–8488.
- Peltier, A., Ferrazzini, V., di Muro, A., Kowalski, P., Villeneuve, N., Richter, N., et al. (2021).
 Volcano crisis management at Piton de la Fournaise (La Réunion) during the COVID-19
 lockdown. *Seismological Society of America*, 92(1), 38–52.
- Peltier, A., Chevrel, M. O., Harris, A. J. L., & Villeneuve, N. (2022). Reappraisal of gap analysis
 for effusive crises at Piton de la Fournaise. *Journal of Applied Volcanology*, *11*(1), 1–17.
 https://doi.org/10.1186/s13617-021-00111-w
 - 28

- Peters, S. I., Christensen, P. R., & Clarke, A. B. (2021). Lava Flow Eruption Conditions in the
 Tharsis Volcanic Province on Mars. *Journal of Geophysical Research: Planets*, *126*(7).
 https://doi.org/10.1029/2020JE006791
- Ramsey, M. S., Chevrel, M. O., Coppola, D., & Harris, A. J. L. (2019). The influence of
 emissivity on the thermo-rheological modeling of the channelized lava flows at tolbachik
 volcano. *Annals of Geophysics*, 62(Special Issue), 44. https://doi.org/10.4401/ag-8077
- 768 Rhéty, M., Harris, A., Villeneuve, N., Gurioli, L., Médard, E., Chevrel, O., & Bachélery, P.
- (2017). A comparison of cooling-limited and volume-limited flow systems: Examples from
 channels in the Piton de la Fournaise April 2007 lava-flow field. *Geochemistry, Geophysics, Geosystems, 18*(9), 3270–3291. https://doi.org/10.1002/2017GC006839
- Richardson, P., & Karlstrom, L. (2019). The multi-scale influence of topography on lava flow
 morphology. *Bulletin of Volcanology*, *81*(4). https://doi.org/10.1007/s00445-019-1278-9
- Riker, J. M., Cashman, K. V., Kauahikaua, J. P., & Montierth, C. M. (2009). The length of
 channelized lava flows: Insight from the 1859 eruption of Mauna Loa Volcano, Hawai'i. *Journal of Volcanology and Geothermal Research*, 183(3–4), 139–156.
- 777 https://doi.org/10.1016/j.jvolgeores.2009.03.002
- Rizzoli, P., Martone, M., Gonzalez, C., Wecklich, C., Borla Tridon, D., Bräutigam, B., et al.
 (2017). Generation and performance assessment of the global TanDEM-X digital elevation
 model. *ISPRS Journal of Photogrammetry and Remote Sensing*, *132*, 119–139.
 https://doi.org/10.1016/j.isprsjprs.2017.08.008
- Robert, B., Harris, A., Gurioli, L., Médard, E., Sehlke, A., & Whittington, A. (2014). Textural
 and rheological evolution of basalt flowing down a lava channel. *Bulletin of Volcanology*,
 76(6), 1–21. https://doi.org/10.1007/s00445-014-0824-8
- Rowland, S. K., Harris, A. J. L., Wooster, M. J., Amelung, F., Garbeil, H., Wilson, L., &
 Mouginis-Mark, P. J. (2003). Volumetric characteristics of lava flows from interferometric
 radar and multispectral satellite data: The 1995 Fernandina and 1998 Cerro Azul eruptions
 in the western Galápagos. *Bulletin of Volcanology*, *65*(5), 311–330.
- 789 https://doi.org/10.1007/s00445-002-0262-x
- Rowland, S. K., Harris, A. J. L., & Garbeil, H. (2004). Effects of Martian conditions on
 numerically modeled, cooling-limited, channelized lava flows. *Journal of Geophysical Research E: Planets*, 109(10), 1–16. https://doi.org/10.1029/2004JE002288
- Rowland, S. K., Garbeil, H., & Harris, A. J. L. (2005). Lengths and hazards from channel-fed
 lava flows on Mauna Loa, Hawai'i, determined from thermal and downslope modeling with
 FLOWGO. *Bulletin of Volcanology*, 67(7), 634–647. https://doi.org/10.1007/s00445-0040399-x
- Russo, F. P., Flynn, I. T. W., & Ramsey, M. S. (2022). The Impact of Slope Variability on the
 Modeling of Martian Lava Flows. *LPI Contributions*, 2678, 1410.
- Stefanescu, E. R., Bursik, M., & Patra, A. K. (2012). Effect of digital elevation model on MohrCoulomb geophysical flow model output. *Natural Hazards*, 62(2), 635–656.
 https://doi.org/10.1007/s11069-012-0103-y
- Sutton, S. S., Chojnacki, M., Mcewen, A. S., Kirk, R. L., Dundas, C. M., Schaefer, E. I., et al.
 (2022). Revealing Active Mars with HiRISE Digital Terrain Models. *Remote Sensing*,
 14(2403), 1–40.
- Takaku, J., Tadono, T., Doutsu, M., Ohgushi, F., & Kai, H. (2020). Updates of aw3d30' alos
 global digital surface model with other open access datasets. In *International Archives of the Photogrammetry, Remote Sensing and Spatial Information Sciences ISPRS Archives*

808	(Vol. 43, pp. 183–190). International Society for Photogrammetry and Remote Sensing.
809	https://doi.org/10.5194/isprs-archives-XLIII-B4-2020-183-2020
810	Thompson, J. O., & Ramsey, M. S. (2021). The influence of variable emissivity on lava flow
811	propagation modeling. Bulletin of Volcanology, 83(6), 1–19.
812	https://doi.org/10.1007/s00445-021-01462-3
813	Vetere, F., Rossi, S., Namur, O., Morgavi, D., Misiti, V., Mancinelli, P., et al. (2017).
814	Experimental constraints on the rheology, eruption, and emplacement dynamics of analog
815	lavas comparable to Mercury's northern volcanic plains. Journal of Geophysical Research:
816	Planets, 122(7), 1522–1538. https://doi.org/10.1002/2016JE005181
817	Wadge, G. (1981). The variation of magma discharge during basaltic eruptions. Journal of
818	Volcanology and Geothermal Research, 11(2), 139–168.
819	https://doi.org/https://doi.org/10.1016/0377-0273(81)90020-2
820	Wantim, M. N., Kervyn, M., Ernst, G. G. J., del Marmol, M. A., Suh, C. E., & Jacobs, P. (2013).
821	Numerical experiments on the dynamics of channelised lava flows at Mount Cameroon
822	volcano with the FLOWGO thermo-rheological model. Journal of Volcanology and
823	Geothermal Research, 253, 35–53. https://doi.org/10.1016/j.jvolgeores.2012.12.003
824	Wright, R., Blake, S., Harris, A. J. L., & Rothery, D. A. (2001). A simple explanation for the
825	space-based calculation of lava eruption rates. <i>Earth and Planetary Science Letters</i> , 192(2),
826	223–233. https://doi.org/10.1016/S0012-821X(01)00443-5
827	Wright, R., Garbeil, H., & Harris, A. J. L. (2008). Using infrared satellite data to drive a thermo-
828	rheological/stochastic lava flow emplacement model: A method for near-real-time volcanic
829	hazard assessment. Geophysical Research Letters, 35(19).
830	https://doi.org/10.1029/2008GL035228
831	Zuber, M. I., Smith, D. E., Solomon, S. C., Munleman, D. O., Head, J. W., Garvin, J. B.,
832	Absnire, J. B., & Bufton, J. L. (1992). The Mars Observer laser altimeter investigation.
833 924	Journal of Geophysical Research, 97(E5), 7781–7797. https://doi.org/10.1029/92JE00541
034 025	val Zyl, J. J. (2001). The Shuttle Radar Topography Mission (SRTM). a dieaktinough in temote songing of topography. Acta Astronaution. 48(5, 12), 550, 565
836	sensing of topography. Acta Astronautica, 46(3–12), 339–303.
830	
838	
839	
840	
841	
842	
843	
844	
845	
846	
847	
848	
849	
850	
051	
851	
851 852	

855	Table 3. PyFLOWGO input models, modules, and parameters that were used to simulate the 11.3 km channelized
856	Leningradskoye lava flow from 1 December 2012 (e.g., Ramsey et al., 2019). The * next to step size indicates that
857	this parameter was varied for a part of this study. For a full breakdown of abbreviations in the table see Chevrel et al.
858	(2018).

Models	Selection	References
Crystallization Rate	basic	Harris and Rowland (2001)
Melt Viscosity	vft	Giordano et al. 2008)
Relative Viscosity	er	Einstein-Roscoe model from
		Chevrel et al. (2018)
Yield Strength	ryerson	Ryerson et al. (1988)
Crust Temperature	constant	Harris and Rowland (2001)
Effective Crust Cover	basic	Harris and Rowland (2001)
Vesicle Fraction	constant	Harris and Rowland (2001)
Heat Budget Modules	Selection	References
Radiation	yes	Harris and Rowland (2001)
		and Ramsey et al. (2019)
Conduction	yes	Harris and Rowland (2001)
Convection	yes	Harris and Rowland (2001)
Rain	no	Harris and Rowland (2001)
Viscous Heating	no	Harris and Rowland (2001)
Initial Input Parameters	Value	References
Step Size*	10 m	Harris and Rowland (2001)
Effusion Rate*	278 - 400 $m^3 s^{-1}$	MIROVA (this study)
Width	30 m	Ramsey et al. (2019)
Depth	6.1 m	Ramsey et al. (2019)
Gravity	9.81 ms ⁻²	

Eruption Temperature	1355.15 K	Plechov et al. (2015)
Crystal Fraction	25%	Plechov et al. (2015)
Dense Rock Equivalent	2630 kg m ³	Plechov et al. (2015)
Density		
Vesicle Fraction	0.06	Plechov et al. (2015)
Stefan-Boltzmann constant	5.60E-08	
Emissivity Crust	0.95	Ramsey et al. (2019)
Emissivity Uncrusted	0.6	Lee & Ramsey, (2016)
Basal Temperature	773.15 K	Harris and Rowland (2001)
Distance from Core to	19%	Harris and Rowland (2001)
Base		
Wind Speed	5 ms ⁻¹	Harris and Rowland (2001)
Air Friction Factor	0.0036	Harris and Rowland (2001)
Air Temperautre	273.15 K	Harris and Rowland (2001)
Air Density	0.4412 kg m ⁻³	Harris and Rowland (2001)
Air Specific Heat Capacity	1099 J kg ⁻¹ K ⁻¹	Harris and Rowland (2001)
Buffer	140 °C	Harris and Rowland (2001)
Crust Cover Fraction	0.9	Ramsey et al. (2019)
Velocity Dependency of	-0.16	Ramsey et al. (2019)
Crust		
Crust Temperature	773.15 K	Belousov et al. (2015)
a vft	-4.55 Pa s	Volynets et al. (2015)
b vft	6887.303 J mol ⁻¹	Volynets et al. (2015)
c vft	527.44 K	Volynets et al. (2015)
Crystal Growth	0.37	Ramsey et al. (2019)
Solid Temperature	1253.15 K	Ramsey et al. (2019)
Latent heat of	350000 K kg ⁻¹	Harris and Rowland (2001)
Crystallization		

860			
861			
862			
863			
864			
865			
866			
867			
868			
869			