



**HAL**  
open science

## The Application of Ni–Ti SMA Wires in the External Prestressing of Concrete Hollow Cylinders

Aleksandra Dębska, Piotr Gwoździwicz, Andrzej Seruga, Xavier Balandraud, Jean-François Destrebecq

► **To cite this version:**

Aleksandra Dębska, Piotr Gwoździwicz, Andrzej Seruga, Xavier Balandraud, Jean-François Destrebecq. The Application of Ni–Ti SMA Wires in the External Prestressing of Concrete Hollow Cylinders. *Materials*, 2021, 14 (6), pp.1354. 10.3390/ma14061354 . hal-03474781

**HAL Id: hal-03474781**

**<https://uca.hal.science/hal-03474781v1>**

Submitted on 10 Dec 2021

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution 4.0 International License

1 Article

# 2 The Application of Ni-Ti SMA Wires in the External Prestress- 3 ing of Concrete Hollow Cylinders

4 Aleksandra Dębska<sup>1</sup>, Piotr Gwoździewicz<sup>2</sup>, Andrzej Seruga<sup>2</sup>, Xavier Balandraud<sup>3</sup>, Jean-Francois Destrebecq<sup>3</sup>5  
6 <sup>1</sup> Aldebud Aleksandra Dębska, ul. Zyndrama z Maszkowic 11, 30-689 Kraków, Poland; aleksan-  
7 dra.debska@wp.pl8 <sup>2</sup> Cracow University of Technology, ul. Warszawska 24, 31-155 Krakow, Poland; pgwozdziejwicz@pk.edu.pl;  
9 aseruga@pk.edu.pl10 <sup>3</sup> Université Clermont Auvergne, CNRS, SIGMA Clermont, Institut Pascal, F-63000 Clermont-Ferrand, France;  
11 xavier.balandraud@sigma-clermont.fr; j-francois.destrebecq@uca.fr

12 \* Correspondence: pgwozdziejwicz@pk.edu.pl

13 **Abstract:** An innovative method for prestressing structural elements through the use of shape  
14 memory alloys (SMAs) is gaining increasing attention in research as this method does not require  
15 the use of mechanical anchorages for tendons. The activation of the memory effect by means of  
16 temperature variations (Joule effect) in effect produces high stresses in SMA components attached  
17 to concrete components as reported in the literature. This paper presents the work performed for  
18 the purpose of prestressing concrete hollow cylinders with the use of nickel-titanium (Ni-Ti) SMA  
19 wires. In the tests, a variety of hollow cylinders were made using the same concrete mix, with the  
20 same wall thickness (20 mm) but with different external diameters (200 mm, 250 mm and 300 mm).  
21 Their prestressing was achieved by the means of Ni-Ti SMA wires of different diameters (1 mm,  
22 2 mm and 3 mm) wrapped around the cylinders. Longitudinal and circumferential strain during  
23 the thermal activation of the SMA wires by Joule heating was measured using gauges located on  
24 the internal surface of the hollow cylinders. The experimental protocol, recorded observations and  
25 discussion of the effectiveness of the prestressing of concrete elements as a function of the test  
26 parameters are included in the text in detail. Comments on the conditions for effective prestressing  
27 of concrete cylinders with SMA wires are proposed in the conclusions of the paper.

28 **Keywords:** shape memory alloy; prestressing force; confinement; civil engineering; nickel-titanium  
29

30  
31 **Citation:** Dębska, A.; Gwoździewicz, P.; Seruga, A.; Balandraud, X.; Destrebecq, J.-F. Application of Ni-Ti SMA wires to external prestressing of concrete hollow cylinders. *Materials* **2021**, *14*, x. <https://doi.org/10.3390/xxxxx>

32 Received: date  
33 Accepted: date  
34 Published: date

35 **Publisher's Note:** MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



36 **Copyright:** © 2021 by the authors. Submitted for possible open access publication under the terms and conditions of the Creative Commons Attribution (CC BY) license (<http://creativecommons.org/licenses/by/4.0/>).

## 37 1. Introduction

38 Technology relating to the prestressing of structures is widely known in civil engineering and is used mainly in the construction of bridges, tanks, industrial structures and public buildings. At the current level of development of this method, prestressing techniques with conventional steel tendons (wires, strands and bars) and tendons formed from composites developed in the last thirty years [1–3] are used. For the application of any of the proposed methods, it is necessary to use specific tensioning equipment usually in the form of hydraulic jacks as well as appropriate types of anchorages for the given tendon type. For many years, steel tendons have been used for the building of new structures and for strengthening of existing constructions. In recent times, new methods of structural strengthening have been developed for historical monuments, based on composite tapes and textiles, often made with carbon fibers as the principal component.

43 The use of shape memory alloys (SMAs) as another innovative technology used in  
44 the field of structural strengthening is an increasingly popular subject for considerations  
45 and developments. SMAs belong to the group of smart (intelligent) materials. Martensitic  
46 transformations triggered by temperature and stress occur in these metallic alloys. At  
47 zero stress, a SMA is in the austenite (A) phase at “high” temperatures and it is in the  
48 martensite (M) phase at “low” temperatures. The A→M and M→A transformations also  
49 occur at constant “high” ambient temperatures upon mechanical loading and unloading,  
50 respectively. For various use of the SMA materials, as for example the microactuators,  
51 good understanding of the phase transformations and of the role of influencing param-  
52 eters is important [4]. Whatever the type of activation (thermal or mechanical), a hysteresis  
53 of transformation is observed, making modelling and the use of SMAs complex tasks in  
54 engineering applications. The most famous property of SMAs promising for the applica-  
55 tions in civil engineering is the ability to regain the remembered geometry under thermal  
56 activation, referred to as the one-way shape memory effect [5–7]. Such geometry varia-  
57 tions when properly steered may indeed be used for the generation of forces in structural  
58 elements.

59 Nickel-titanium (Ni-Ti) and more generally Ni-Ti-based alloys are the most fre-  
60 quently used SMAs in engineering applications, especially in the form of wires. In Ref. [8]  
61 for instance, it is reported that during the return of SMA material to its original shape  
62 from the deformed form, stress reaching even 800 MPa can be generated in the specimen  
63 in which strain is blocked. This conclusion is promising in the context of the future ap-  
64 plication of properly prepared material for the needs of force introduction in structural  
65 members – such pioneering applications are described in Refs. [9–13]. More detailed ap-  
66 proach to the martensitic transformation of Ni-Ti alloys includes also the presence of the  
67 “R” phase during the cooling process, important for cyclic use of the material [14]. The  
68 introduction of prestressing with the use of this method usually as a single operation  
69 may be performed without the need for hydraulic pulling equipment at the place of pre-  
70 stressing, and it may therefore be used also in the locations where access is difficult.

71 The confinement of plain concrete cylinders using wound SMA wires is one of the  
72 proposed applications in civil engineering to create a state of compression; see for ex-  
73 ample Refs. [15–21]. The present paper describes the work performed for the purpose of  
74 prestressing hollow cylinders, which allows measurement of the strains on the inner  
75 surface while the SMA wire is wound on the outer surface. In the tests, hollow cylinders  
76 were made of the same concrete mix, with the same wall thickness (20 mm) but different  
77 external diameters (200 mm, 250 mm and 300 mm). Their prestressing was achieved by  
78 the means of Ni-Ti SMA wires of different diameters (1 mm, 2 mm and 3 mm) wrapped  
79 around the cylinders. Longitudinal and circumferential strains were measured using  
80 gauges located on the inner surface of the hollow cylinders during thermal activation of  
81 the SMA wires by Joule heating. Following the testing plan composed of a series of  
82 one-way, simple prestressing operations the observations were focused on the effective-  
83 ness of the technique and did not include full analysis of the potential degradation of the  
84 SMA wires during the electrothermal working cycles as it is described in [22]. The ex-  
85 perimental protocol, recorded observations and discussion of the effectiveness of pre-  
86 stressing of concrete elements as a function of the test parameters are included in detail in  
87 the text. A description of the conditions for the effective prestressing of concrete pipes  
88 with SMA wires is proposed in the conclusions of the paper.

## 89 2. Properties of the SMA wires used

90 Ni-Ti SMA wires were used in the present work to generate prestress states in con-  
91 crete samples. Three wires with the different diameters (1 mm, 2 mm and 3 mm) were  
92 selected. Their chemical compositions were Ni<sub>55.44</sub>Ti (wt.%) for the 1 mm wire and  
93 Ni<sub>55.84</sub>Ti (wt.%) for the other two diameters of the wires. Table 1 presents the values of  
94 the four transformation temperatures for each wires diameter: austenite-start ( $A_s$ ), aus-  
95 tenite-finish ( $A_f$ ), martensite-start ( $M_s$ ) and martensite-finish ( $M_f$ ). Values were obtained

by means of dilatometric testing. Detailed information on the SMA wires properties testing can be found in Refs. [21, 23, 24]. They are the principal informations needed for proper control of the phase transformation progress in SMA under varying temperature. It can be noted that  $M_s$  is negative and lower than  $A_s$  for the three wires. This property is not generic for SMAs. We selected this property for our SMA wires in order to have an ambient temperature  $T_{amb}$  between  $M_s$  et  $A_s$ . The inequality  $M_s < T_{amb} < A_s$ . is a key point of the study. Note that by construction, the thermal hysteresis is high compared to most of SMA wires. As a consequence also, the SMA wires can be “initialised” to the austenitic state by heating above  $A_f$  followed by a return to an ambient temperature higher than  $M_s$  [21, 23]. Next, as a result of loading and further unloading of the austenitic SMA wire at the ambient temperature, a residual strain is generated in the wire. This residual strain is related to the transformation of the austenite into so-called oriented martensite upon loading (this is distinguished from the self-accommodating martensite, which is created by cooling and is not associated to a macroscopic strain). In these circumstances, the blocking of wire deformation and increasing its temperature above  $A_f$  leads to the generation of stress in the wire. This phenomenon is described in detail in, for example, Ref. [20]. For the mechanical characterisation of each of the three SMA wires, a 20 kN Zwick 1455 laboratory testing machine was used to measure various mechanical parameters at 15°C, starting from the austenitic state at zero stress: apparent Young modulus ( $E_{SMA}$ ) of the austenite, critical stress ( $\sigma_{cr}$ ) at which the  $A \rightarrow M$  transformation starts, as well as the maximal stress ( $\sigma_{max}$ ) and residual strain ( $\epsilon_{res}$ ) during the load-unload cycle to a maximum deformation of 6%. Finally, the residual stress ( $\sigma_{res}$ ) at the blocked residual strain upon heating was measured. The mechanical properties of the three types of Ni-Ti wires used in the tests are shown in Table 1 besides the transformation temperature values. Details can be found in Ref. [24].

**Table 1.** Properties of the three SMA wires: transformation temperatures and mechanical properties from [21, 23]

SMA wire diameter	Transformation temperatures at zero stress	Mechanical characteristics for a load-unload test at 6% maximum strain at 15°C, followed by heating at fixed residual strain $\epsilon_{res}$								
		$M_f$	$M_s$	$A_s$	$A_f$	$E_{SMA}$	$\sigma_{cr}$	$\sigma_{max}$	$\epsilon_{res}$	$\sigma_{res}$
		[°C]	[°C]	[°C]	[°C]	[GPa]	[MPa]	[MPa]	[%]	[MPa]
$\phi$ 1 mm		-51	-7	14	22	34.7	244	269	5.1	202
$\phi$ 2 mm		-66	-11	2	13	21.7	314	309	4.6	248
$\phi$ 3 mm		-51	-30	1	10	15.5	340	349	3.0	179

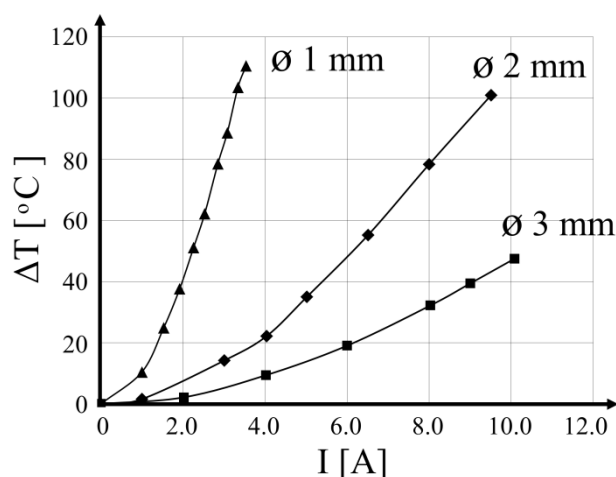
fect was used for heating the SMA wires. Heating tests were performed on 200-mm-long wire specimens. Two parameters were recorded under different current intensities  $I$  [A]: voltage  $U$  [V] and stabilized temperature variation  $\Delta T$  [°C] using an infrared thermal camera (see Ref. [25] for details about the boundary conditions). Figure 1 shows the  $\Delta T - I$  diagrams, which can be used for the purpose of defining the current value needed for the heating of the Ni-Ti wires to a given temperature. The equations for each diameter are as follows:

$$\Delta T_{\phi 1 \text{ mm}} = 7.646 I^2 + 5.047 I \quad (1)$$

$$\Delta T_{\phi 2 \text{ mm}} = 0.689 I^2 + 2.400 I \quad (2)$$

$$\Delta T_{\phi 3 \text{ mm}} = 0.401 I^2 + 0.729 I \quad (3)$$

Prestressing of structural member is generally a single operation. In the consequence the tests were focused on the behavior of the specimens during heating process of the SMA wire and the effectiveness of such technique and the cooling process was the finishing part for every test. Some influences, for example the generation of the “R” phase during cooling of the wire which influences the wire resistance at this phase (as reported in [14]) were not considered. Following the same argument, also considerations regarding the degradation of the material in consequence of cyclic heating as described for instance in [22] was not included in the scope of the work.



**Figure. 1** Temperature change  $\Delta T$  vs. electric current  $I$  relations in the three 200-mm-long SMA Ni-Ti wires

### 3. Description and preparation of the concrete samples

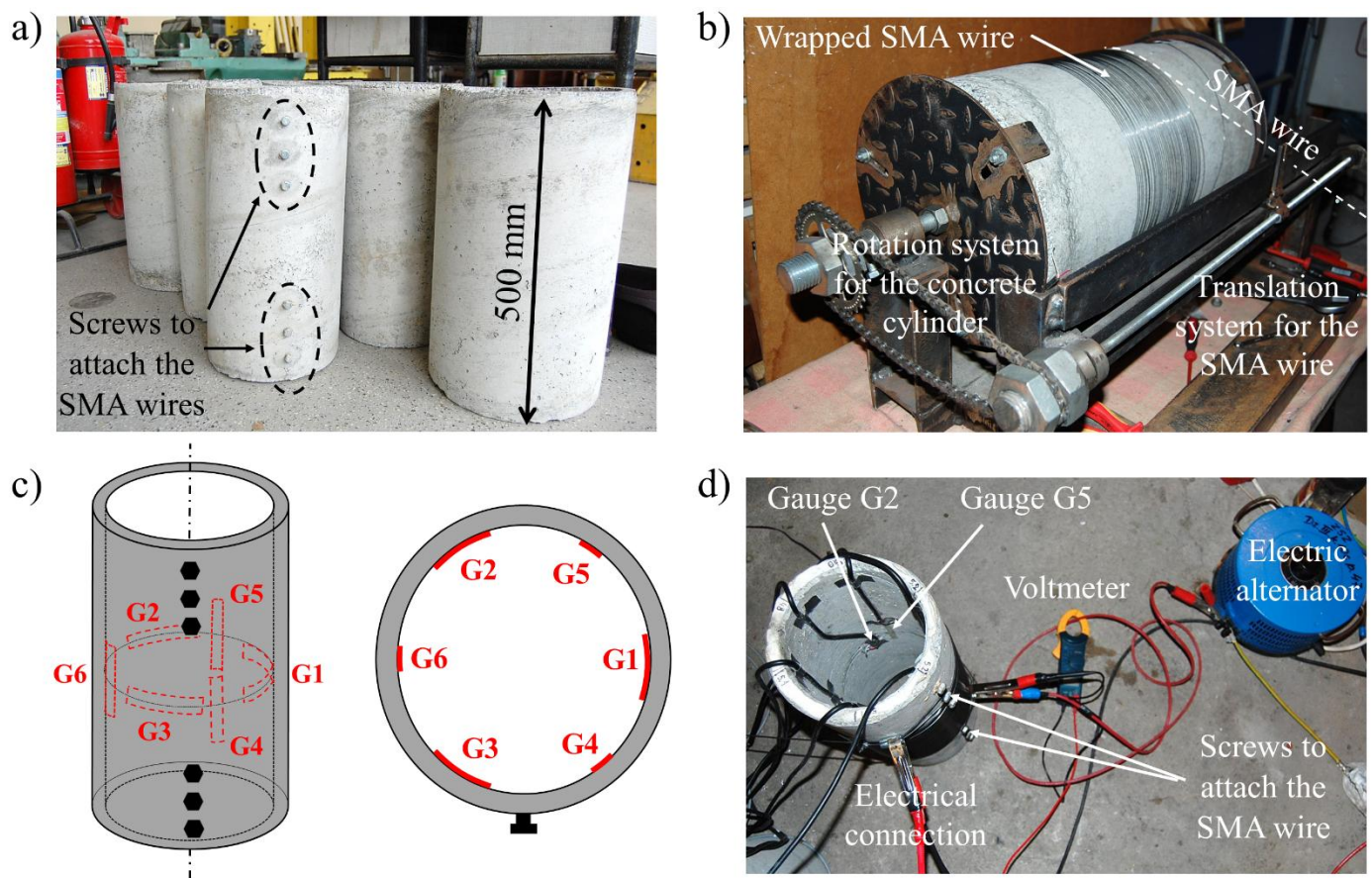
In the plan of this research, it was decided that the tests would be performed on three series of 500-mm-long concrete hollow cylinders, each comprised of three pieces with external diameters of 200 mm, 250 mm and 300 mm (see Fig. 2a). The measured values of wall thickness for the 200-mm cylinder were between 20.1 mm and 20.8 mm. They were between 22.1 mm and 22.9 mm for the 250-mm cylinder, and between 20.5 mm and 20.9 mm for the 300-mm cylinder. The variation coefficients  $\nu$  of the mean wall thickness were between 3.7% and 9.6%.

All hollow cylinders were made of concrete composed of basalt gravel, the size of which was between 2 mm and 8 mm and CEM I 32.5 R Portland cement. The composition of the concrete mix per  $\text{m}^3$  was: 353.4 kg cement, 1,202.6 kg basalt gravel, 560 kg river sand, 213 w/c ratio of water, which was equal to 0.6. At the time of casting the test elements, several concrete specimens were collected for simultaneous verification of the mechanical properties of the material at the time of testing of the hollow cylinders. The dimensions of the material specimens were a diameter of 150 mm and a length of 300 mm for the plain cylinders, and the cubes were 150×150×150 mm. After seven days, the molds were disassembled and the concrete hollow cylinders (as well as the concrete specimens for material tests, see below) were protected with PE foil for a period of twenty-eight days. For the sake of the estimation of the volumetric weight of concrete, all specimens were weighted and measured. The mean concrete weight obtained was 2,465  $\text{kg}/\text{m}^3$  with a coefficient of variation  $\nu$  of 1.1%. The mean concrete compressive strength measured on the cubic specimens was  $f_{c,\text{cub}} = 51$  MPa ( $\nu = 8.1\%$ ). The mean value measured on the cylinders was  $f_{c,\text{cyl}} = 43$  MPa ( $\nu = 8.1\%$ ). The mean value of concrete elasticity modulus under compression measured at the level of 0.4  $f_{c,\text{cyl}}$  was  $E_c = 36,240$  MPa ( $\nu = 0.8\%$ ). On two cylindrical concrete specimens, the widened program of the test for the elasticity modulus was additionally performed with measurements taken at five levels of loading: 0.2, 0.3, 0.4, 0.5 and 0.6 of  $f_{c,\text{cyl}}$ . The test procedure followed the provisions given by

Instytut Techniki Budowlanej (Building Research Institute, Warszawa) [26]. The variations of concrete elasticity modulus following the force level are reported in Table 2. The mean value of concrete tensile strength under axial loading determined in the tests was 4.4 MPa ( $\nu = 1.0\%$ ). The mean value of the concrete tensile strength determined in the splitting tests was 4.1 MPa with ( $\nu = 2.1\%$ ).

**Table 2** Modulus of elasticity of concrete versus the level of loading

Sample no	Modulus of elasticity $E_c$ [MPa]				
	0.2 $f_{c,cyl}$	0.3 $f_{c,cyl}$	0.4 $f_{c,cyl}$	0.5 $f_{c,cyl}$	0.6 $f_{c,cyl}$
1	38 240	37 860	36 170	35 300	34 100
2	39 130	37 100	36 000	34 820	33 870



**Figure 2.** Test details: a) photo of concrete test samples (hollow cylinders) after demolding, with anchoring bolts visible on one sample; b) hand wire-winding machine; c) location of the strain gauges on the internal surface of the concrete cylinders; d) photo of the Joule effect setting for the prestressing of the hollow cylinder

#### 4. Procedure for the creation of prestress states in concrete hollow cylinders with use of SMA wires

The procedure presented below refers to the external prestressing of concrete cylinders with shape memory wires. The prestressing process is based on the thermal activation of the shape memory effect in the SMA wires. Heating of the material to a temperature exceeding the value of  $A_s$  is performed with the use of electric power. The prestressing procedure for every concrete cylinder is composed of the following four steps:

207  
208  
209  
210  
211  
212  
213  
214  
215  
216  
217  
218  
219  
220  
221  
222  
223  
224  
225  
226  
227  
228  
229  
230  
231  
232  
233  
234  
235  
236  
237  
238  
239  
240  
241  
242  
243  
244  
245  
246  
247  
248  
249  
250  
251  
252  
253

#### Step I – wire preparation for testing

- The wire is subjected to heating until a temperature exceeding the value of  $A_f$  is obtained for the purpose of initialisation in austenite phase.
- The wire is cooled to the ambient temperature. Let us recall that the ambient temperature is higher than  $M_s$ . In consequence, transformation to martensite does not occur, the material austenitic state is preserved. At this time, anchoring loops are formed on the wire ends.
- For part of the testing, controlled predeformation (residual strain) is applied to the SMA wire with the relevant pulling equipment.

#### Step II – winding and anchoring of SMA wires

- The concrete specimen is installed in the specially designed winding apparatus shown in Fig. 2b.
- The SMA wire loop is attached to the anchoring bolt on the external surface of the hollow cylinder and the wire is wound on the surface.
- During the whole winding process, the ambient temperature is kept constant and the SMA wire is protected from any temperature increase, especially from contact with hands.
- After winding, the wire end loop is fixed to the anchorage bolt.

#### Step III – connection of the measurement equipment

- The following equipment is connected to the HBM QuantumX MX840A measuring amplifier with the use of shielded cables:
  - the strain gauges installed on the internal surface of two hollow concrete cylinders – the tested cylinder and a reference cylinder (Fig. 2c);
  - two temperature sensors, one for measuring temperature of the SMA wire  $T_{ext}$  and one for the internal surface of the concrete cylinder  $T_{int}$ .
- An ammeter and voltmeter are used for monitoring the current parameters during the test.

#### Step IV – heating and cooling of the tested element

- At the initiation of the test, the SMA wire is connected to an electric current. Appropriate current source was used in dependence on the electric resistance of the SMA wire. The temperature increase in the SMA wire is controlled.
- After achieving the required temperature of the wire, the electrical current is disconnected and the temperature decrease is observed until it returns to the ambient temperature.

### **5. Standard features of the experimental procedure**

#### *5.1. Set-up of the specimens and the measurement equipment*

All tests in the research program were performed at the ambient temperature selected with consideration to the austenite start ( $A_s$ ) temperature for the given type of wire, which should not be exceeded. Part of the research program was therefore performed outdoors during winter. Low ambient temperatures and protection of the SMA wire from heating were an important advantage of this time of year.

The concrete deformation of every concrete cylinder was measured with strain gauges, which were installed at the mid-height of the inner surface of the hollow cylinders. Each of the specimens was equipped with six gauges: three in the longitudinal direction of the

tube (vertically) and three in the circumferential direction, placed alternately along the internal circumference of the element. The gauges are denoted as follows and their positions are shown in Fig. 2c:

- circumferential gauges – G1, G2 and G3;
- vertical gauges – G4, G5 and G6.

Temperature compensation was used due to the influence of temperature during prestressing of the tubes. Following the principles of the strain measurement theory, the gauges were connected in the Wheatstone's half-bridge system. During the tests, the following parameters were identified: ambient temperature ( $T_a$ ), temperature of the pipe internal surface ( $T_{int}$ ) and temperature of the SMA wire wound on the pipe ( $T_{ext}$ ).

### 5.2. Application of electrical current for prestressing of concrete hollow cylinders

The testing stand was installed in a location where temperature varied between  $-1^\circ\text{C}$  and  $+10^\circ\text{C}$ . During all tests, the procedure described in Section 4 was used. The electrical current energy was transferred into thermal energy, which is reflected by the temperature increase in the wire through Joule's law:

$$P = I^2 R = \frac{U^2}{R} \quad (4)$$

where  $P$  is the electric power [W] and  $R$  is the conductor resistance [ $\Omega$ ]. Table 3 shows the values of the parameters required for fulfilling the condition of the temperature increase in the wire at  $60^\circ\text{C}$  above the ambient temperature. Current density was calculated using equations (1), (2) and (3), and the resistance value was measured. Appropriate equipment for generating the direct current was used. Resistance variations during the cooling period of the SMA wire ("R" phase generation as described for instance in [22]) as well as influence of the wire re-use on its resistance were not considered.

**Table 3** Parameters required for performing the SMA wire heating tests with direct current

Wire diameter	L [m]	$\Delta T$ [ $^\circ\text{C}$ ]	R [ $\Omega$ ]	I [A]	P [W]	U [V]
$\varnothing$ 1 mm	40	60	41.6	2.5	260	104
$\varnothing$ 2 mm	80	60	20.8	7	1,041	147
$\varnothing$ 3 mm	80	60	9.3	13	1,562	120

### 5.3. Equations for the analysis of the combined effect of prestressing and thermal dilatation on concrete strain in hollow cylinders

The influence of thermal deformation of concrete under conditions of the heating and cooling of the shape memory wire is considered. An analytical model is composed for the determination of forces acting in the SMA wire on the basis of measured deformation. It is assumed that the concrete circumferential strain measured with the strain gauges  $\varepsilon_c$  is linearly composed of the elastic strain provoked by prestressing with the SMA wire  $\varepsilon_{c,SMA}$  and the thermal strain  $\varepsilon_t$ :

$$\varepsilon_c = \varepsilon_{c,SMA} + \varepsilon_t \quad (5)$$



Based on the assumption that the material properties of concrete are constant in time and are independent of temperature, thermal strain in concrete is expressed as:

$$\varepsilon_t = \alpha_t \Delta T \quad (6)$$

where  $\Delta T$  is the temperature variation and  $\alpha_t$  is the coefficient of thermal expansion for concrete ( $\alpha_t = 10 \cdot 10^{-6}/^\circ\text{C}$ ).

Following the assumption of the mechanical isotropy of concrete, thermal isotropy is also assumed. Additionally, the temperature influence for any direction of deformation is separately considered in a linear manner. Therefore, the constitutive relations between stress and strain are written in the following form, accounting for thermal deformation in accordance with a cylindrical coordinates system:

$$\begin{cases} \varepsilon_r = E^{-1}[\sigma_r - \nu(\sigma_c + \sigma_z)] + \alpha_t \Delta T \\ \varepsilon_c = E^{-1}[\sigma_c - \nu(\sigma_z + \sigma_r)] + \alpha_t \Delta T \\ \varepsilon_z = E^{-1}[\sigma_z - \nu(\sigma_r + \sigma_c)] + \alpha_t \Delta T \end{cases} \quad (7)$$

with:

$\varepsilon_r, \sigma_r$  – strain and stress in radial direction,

$\varepsilon_c, \sigma_c$  – strain and stress in circumferential direction,

$\varepsilon_z, \sigma_z$  – strain and stress in longitudinal direction.

Using the Lamé-Clapeyron approach for a thin cylindrical shell subjected to a radial uniform pressure  $p$ , it is possible to express the stress tensor  $\sigma$ :

$$[\sigma] = \begin{bmatrix} \sigma_r & 0 & 0 \\ 0 & \sigma_c & 0 \\ 0 & 0 & \sigma_z \end{bmatrix} \quad (8)$$

with

$$\begin{cases} \sigma_r = -\frac{p r_2^2}{r_2^2 - r_1^2} \left(1 - \frac{r_1^2}{r^2}\right) \\ \sigma_c = -\frac{p r_2^2}{r_2^2 - r_1^2} \left(1 + \frac{r_1^2}{r^2}\right) \\ \sigma_z = 0 \end{cases}$$

where  $r$  is the radial distance from the centroid of the concrete hollow cylinder, and  $r_1$  and  $r_2$  are the internal and external radii of the concrete hollow cylinder, respectively. It is possible to express the strain tensor  $\varepsilon$  as follows:

$$[\varepsilon] = \begin{bmatrix} \varepsilon_r & 0 & 0 \\ 0 & \varepsilon_c & 0 \\ 0 & 0 & \varepsilon_z \end{bmatrix} \quad (9)$$

with

$$\begin{cases} \varepsilon_r = -\frac{1}{2\mu} \frac{p r_2^2}{r_2^2 - r_1^2} \left(\frac{\lambda + 2\mu}{3\lambda + 2\mu} - \frac{r_1^2}{r^2}\right) + \alpha_t \Delta T \\ \varepsilon_c = -\frac{1}{2\mu} \frac{p r_2^2}{r_2^2 - r_1^2} \left(\frac{\lambda + 2\mu}{3\lambda + 2\mu} + \frac{r_1^2}{r^2}\right) + \alpha_t \Delta T \\ \varepsilon_z = \frac{\lambda}{\mu(3\lambda + 2\mu)} \frac{p r_2^2}{r_2^2 - r_1^2} + \alpha_t \Delta T \end{cases}$$

where parameters  $\mu$  and  $\lambda$  are classically expressed as functions of Young's modulus  $E$  and Poisson's ratio  $\nu$  of concrete as follows:

$$\begin{cases} \mu = \frac{E}{2(1-\nu)} \\ \lambda = \frac{\nu E}{(1+\nu)(1-2\nu)} \end{cases}$$

Based on the local equilibrium of the cylindrical shell, the pressure  $p$  applied by the SMA wires on the external surface of the hollow cylinder is expressed in the following formula (7):

$$p = \frac{\pi d^2 \sigma_{SMA}}{2 e (2r_2 + d)} \geq 0 \quad (10)$$

where  $\sigma_{SMA}$  is longitudinal stress in the SMA wire,  $d$  is the diameter of the SMA wire and  $e$  is the axial spacing of the SMA wire (pitch) wound on the concrete hollow cylinder.

## 6. Results of the performed tests

### 6.1. Results obtained from tests of concrete hollow cylinders prestressed with SMA wire without preliminary deformation

Nineteen tests were successfully performed on concrete hollow cylinders prestressed with wound SMA wires that were not pretensioned and not preliminary deformed (not predeformed). Information on the number of tests performed for the various SMA wire diameters used and the various diameters of concrete specimens is presented in Table 4. For practical reasons, lengths of Ni-Ti wires measuring 28.80 m were prepared for this purpose.

**Table 4.** Number of tests performed on concrete hollow cylinders with use of SMA wires without preliminary deformation

Wire diameter	External pipe diameter		
	200 mm	250 mm	300 mm
∅ 1 mm	4 tests	1 test	2 tests
∅ 2 mm	4 tests	1 test	2 tests
∅ 3 mm	2 tests	1 test	2 tests

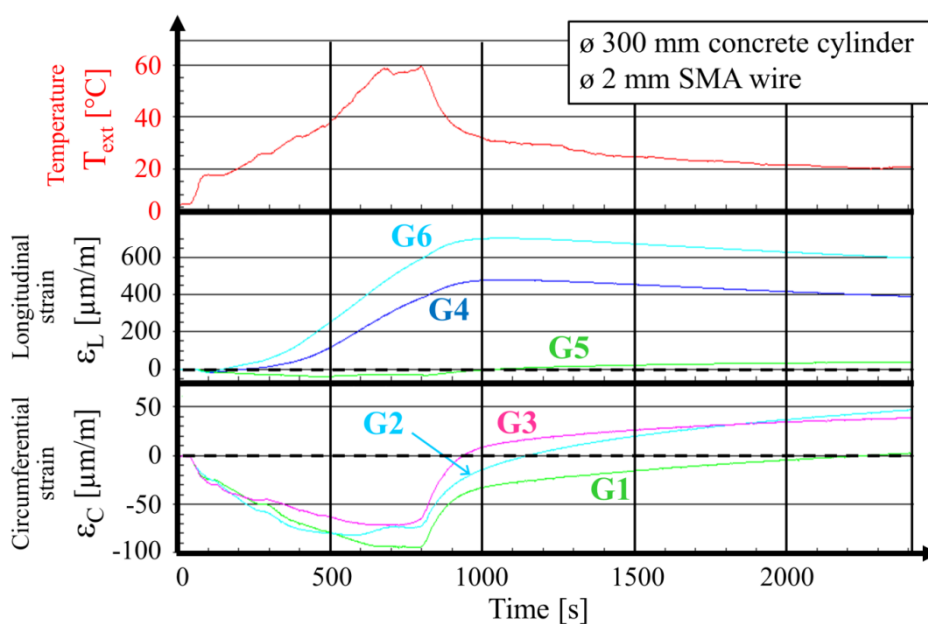
Figure 3 presents example results of the measurements which were recorded during the heating and cooling process of the specimen composed of a concrete cylinder with a diameter of 300 mm wound with Ni-Ti wire with a diameter of 2 mm. Three diagrams were prepared as a time function: a diagram of the wound wire temperature, a diagram of the vertical concrete deformation and a diagram of the circumferential concrete deformation. The temperature of the internal surface of the cylinder  $T_{int}$  and ambient temperature  $T_a$  were also measured.

For the first testing phase (heating), the temperature increases up to +60°C. With a wire temperature increase of 20°C (200 s after current connection), the initiation of an increase in strain is observed in the longitudinal direction of the hollow cylinder. It is worth noting that the result of the thermal dilatation of concrete is included in all measurements of the vertical (longitudinal) and circumferential strain gauges. The duration of the electric current flow through the wound wires was 800 s. It may be observed in the concrete deformation diagrams that, during the initial 200 s of the heating period, the vertical (longitudinal) concrete strain is not significant while the circumferential compressive concrete strain increase is substantial and reaches a level of -50  $\mu\text{m}/\text{m}$ . The increase of concrete strain in the circumferential direction provides evidence of the martensite transformation in the SMA wire and is consequently also evidence of concrete

364 prestressing. After 800 s of heating (when the maximal wire temperature of 60°C is  
 365 reached) the mean circumferential compressive strain in the concrete was at a level of  
 366 around -85  $\mu\text{m}/\text{m}$ , and the mean strain in the longitudinal direction was around 333  
 367  $\mu\text{m}/\text{m}$  (at this moment, the temperature of the concrete is lower than the wire tempera-  
 368 ture).

369 After disconnecting the electrical current, SMA wire quickly loses its temperature  
 370 while concrete retains its heat for much longer. During the cooling period, compressive  
 371 strain in concrete is progressively lost. The maximal observed main longitudinal strain  
 372 increase in the concrete was around 400  $\mu\text{m}/\text{m}$  after 1,000 s (SMA temperature  $T_{\text{ext}} =$   
 373 32°C). It is understood that concrete temperature is higher than wire temperature. After  
 374 1,300 s, the mean circumferential strain in concrete is approaching zero and with further  
 375 time, the strain becomes positive. The explanation for such a development is that the re-  
 376 sidual strain in the wire decreases to zero. After 2,400 s, the wire temperature is 20°C, the  
 377 mean longitudinal strain in concrete is 333  $\mu\text{m}/\text{m}$  and the mean circumferential concrete  
 378 strain is 30  $\mu\text{m}/\text{m}$ .

379 Based on the results, it can be concluded that the prestressing effect obtained with  
 380 the SMA wire without preliminary deformation is not stable over time. A comment can  
 381 be made about the heating phase. Before winding the SMA wire, it was in the austenite  
 382 state; however, a low quantity of the oriented martensite probably appeared due to the  
 383 curvature of the wire when installed on the external surface of the concrete hollow cyl-  
 384 nder. During the temperature increase above the  $A_f$  value, the shape memory effect was  
 385 activated, thus generating a (relatively low) circumferential compressive strain increase  
 386 in concrete. A similar effect was previously reported in Ref. [16] for plain concrete cyl-  
 387 inders. The loss of effect upon cooling can be explained by the appearance of oriented  
 388 and self-accommodating martensite. In any case, in spite of the number of tests, the ob-  
 389 served effect is found to be not sufficient for the permanent prestressing of the concrete  
 390 hollow cylinders. Based on this, it was decided to perform further tests exclusively with  
 391 the preliminary deformation of SMA wires and to resign from the presentation of re-  
 392 maining results captured during tests with use of wires that were not predeformed.



394  
 395 **Figure 3.** Measurements of wire temperature  $T_{\text{ext}}$ , longitudinal strain  $\varepsilon_L$  and circumferential strain  $\varepsilon_C$  of concrete during the process  
 396 of testing 300-mm-diameter hollow cylinder wound with 2-mm-diameter SMA wire without predeformation (circumferential

gauges – G1, G2 and G3; longitudinal gauges – G4, G5 and G6). Note that gauge G5 was not working for all tests without predeformation.

## 6.2. Concrete hollow cylinders prestressed with the preliminary deformed SMA wire

### 6.2.1. Experimental setup

In the next step of the testing program, the effectiveness of the prestressing of concrete hollow cylinders with predeformed Ni-Ti coil was verified. Ni-Ti wires measuring 28.80 m in length were prepared for this purpose.

The experiments were performed with the use of all nine concrete hollow cylinders (three hollow cylinders for each of the wire diameters). Eighteen tests were performed. During the preparation of every test, the SMA wire was predeformed and was then wound over the external surface of the hollow cylinder. After every test, the SMA wire was unwound and was then heated above  $A_f$  in order to retrieve the austenite state; it was then predeformed and wound again on a hollow cylinder. As a consequence of the differences between the diameters of the hollow cylinders, the number of possible windings with the wire of a constant length varied and were as follows for each of the hollow cylinders:

- For the hollow cylinder with an external diameter of 200 mm, there were forty-five windings of the wire placed in the central strip of the hollow cylinder surface, which amounted to a width of approximately 0.17 m.
- For the hollow cylinder with an external diameter of 250 mm, there were thirty-eight windings of the wire placed in the central strip of the hollow cylinder surface, which amounted to a width of approximately 0.15 m.
- For the hollow cylinder with an external diameter of 300 mm, there were thirty-two windings of the wire placed in the central strip of the hollow cylinder surface, which amounted to a width of approximately 0.13 m.

The pitch of the spiral coil was independent of the winding precision. The nominal pitch was 4 mm. As with the test without predeformation, the following parameters were recorded during the tests: ambient temperature ( $T_a$ ), temperature of the internal surface of the hollow cylinder ( $T_{int}$ ) and temperature of the wire wound on the hollow cylinder ( $T_{ext}$ ).

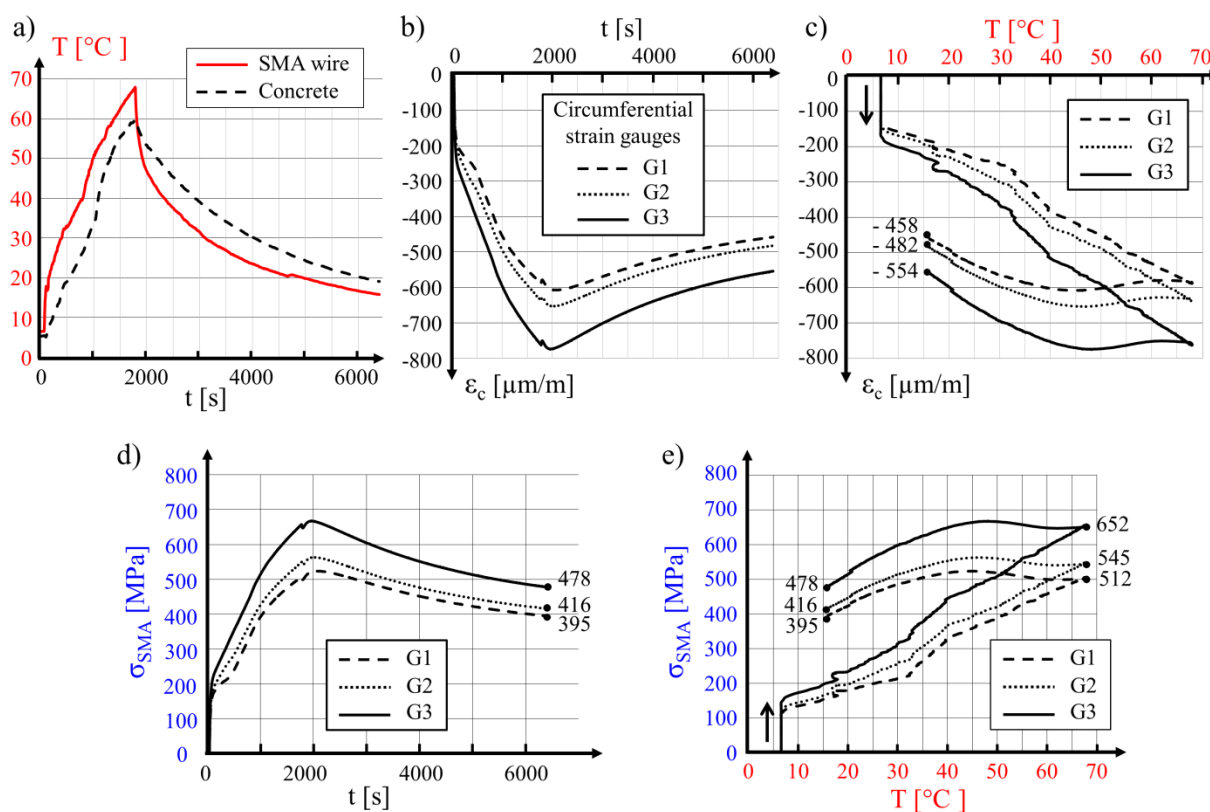
All tests of this series were performed following the same procedure. In contrast to the tests described in Section 6.1, all the SMA wires were predeformed before winding, as explained in Section 4. The initial elongation of the wires was set at two levels: 3% and 6%. The measurement equipment was connected to the tested cylinder and to the reference cylinder, and the hollow cylinder prestressing was performed using a flow of electrical current through the SMA material winds as is presented in Fig. 2d.

### 6.2.2. Test results and stresses calculated in the SMA

As explained in Section 5.1, variation of concrete strain in the circumferential direction (three strain gauges) and in longitudinal direction (three strain gauges) as well as the temperature of the wire and that of the internal hollow cylinder surface were monitored and recorded during each test. The measured values are presented as diagrams of strain and temperature, both in relation to time. Figure 4 presents example diagrams determined during the prestressing tests performed on the 300-mm-diameter concrete hollow cylinder with 2-mm SMA wire. The main features shown on the diagrams are discussed below. Detailed results for the same specimen are included in Table 8, No. 16. Variations of the temperature during the whole test are presented in Fig. 4a. Temperature increase activated the martensite-to-austenite transformation. Let us recap that the start and finish transformation temperatures at zero stress are  $A_s = 2^\circ\text{C}$  and  $A_f = 13^\circ\text{C}$ , respectively (see

Table 1). As a consequence, transformation starts nearly instantaneously after the initiation of the flow of electrical current. This phenomenon can be seen in Fig. 4b and Fig. 4c. The circumferential strain in concrete resulting from the clamping of the Ni-Ti wire around the hollow cylinder starts with a sharp increase at a wire temperature of 7°C (Fig. 4c). Following further temperature increases, growth of the compressive strain in concrete is registered. After reaching 67°C in the tested wire, the current is disconnected. The moment of current disconnecting may be found in the diagram showing the relationship between the circumferential strain in concrete and time (Fig. 4b) in the form of a small discontinuity in any line of captured values. A decrease of the wire temperature to a level of 40°C does not substantially influence the circumferential strain generated in concrete (Fig. 4c). Further cooling of the specimen to the ambient temperature provokes a partial loss of the generated concrete deformation.

Based on the concrete strain evolution shown in Fig. 4b and Fig. 4c, and on account of Eq. (8) to (10) presented above, diagrams of stress development in the 2 mm Ni-Ti wire were built as functions of time and temperature. In Fig. 4d, an instantaneous stress increase to the level of 200 MPa may be observed, which results from a quick activation of the shape memory effect. Further increases of the wire temperature allows the progress of the transformation of oriented martensite into austenite. This progress provokes a further increase of stress in the SMA wire. A partial loss of the wire stress initially generated during heating time is observed after a decrease of its temperature to below 40°C (Fig. 4e).



**Figure 4.** Results recorded during testing of the 300-mm hollow cylinder prestressed with predeformed 2-mm Ni-Ti wire: a) temperature of the wire and the concrete surface over time; b) variations of circumferential concrete strains over time; c) variation of circumferential strain over concrete in relation to wire temperature; d) stress in Ni-Ti wire in relation to time; e) stress in Ni-Ti wire as a function of temperature.

Analysis of the recorded measurements leads to the conclusion that during cooling time, nearly 24% of the maximal stress obtained in the test for the material is lost. Such a loss is a consequence of the thermo-mechanical properties of the shape memory alloy used and may be qualified as a non-standardized initial loss of the prestressing force. A decrease of the residual stress in the prestressing wire was estimated at 6.5% while accounting for the influence of temperature variations on concrete deformation.

## 7. Analysis of test results

### 7.1. Discussion of the results from tests and analysis

The registered results of the tests were used for the determination of prestressing effectiveness. Measurements were taken at the final stage of the tests of the eighteen concrete hollow cylinders, including concrete strain in circumferential and longitudinal directions, temperatures of the surrounding air  $T_a$ , of the wire  $T_{ext}$  and of the internal surface of the hollow cylinder  $T_{int}$  are included in Table 6. Additionally, the stress values are analytically determined.

The following parameters were used for the calculations of stress and force in the SMA wires:  $E_c$  (elasticity modulus for concrete, equal to 36 GPa),  $T_{ext}$  (SMA wire temperature measured in the final step of the test),  $T_{int}$  (temperature of the internal surface of the concrete hollow cylinder measured in the final step of the test),  $T_a$  (ambient temperature of the test) and  $\epsilon_c$  (circumferential strain in the concrete measured with the strain gauges in the final step of the test). With the use of Eq. (8) to (10), after excluding the thermal dilatation of the concrete, the following quantities were calculated for every concrete hollow cylinder prestressed with the SMA wires:

- $p$  – pressure [MPa];
- $\sigma_{c,SMA}$  – circumferential compression stress in concrete at the residual state [MPa];
- $\sigma_{res}$  – stress in shape memory wire at the residual state [MPa];
- $F_{SMA}$  – force in SMA wire remaining after prestress execution [N].

The mean values of the circumferential stress in concrete caused by the prestressing wire action ( $\sigma_{c,SMA}$ ) and mean values of the residual stress in the prestressing wire  $\sigma_{res}$  calculated on the basis of measurements are included in Table 6..

**Table 6.** Results of measurements and calculation of mean forces in SMA wires wound on the concrete cylinders

No	$\Delta L/L$ [%]	$T_a$ [°C]	$T_{ext}$ [°C]	$T_{int}$ [°C]	$\epsilon_{c1}$ [10 <sup>-6</sup> ]	$\epsilon_{c2}$ [10 <sup>-6</sup> ]	$\epsilon_{c3}$ [10 <sup>-6</sup> ]	$\epsilon_{c,av}$ [10 <sup>-6</sup> ]	$\epsilon_t$ $\Delta T$ [10 <sup>-6</sup> ]	$\alpha$	$\epsilon_{c,SMA}$ [10 <sup>-6</sup> ]	$p$ [MPa]	$\sigma_{c,SMA}$ [MPa]	$\sigma_{res}$ [MPa]	$F_{SMA}$ [N]
<b>Pipe <math>\varnothing</math> 200 mm – SMA wire <math>\varnothing</math> 1 mm</b>															
1	3	-3	13.3	22.5	-155.9	-143.2	-151.9	<b>-150.3</b>	-91.8		-58.5	0.38	-2.1	194.2	152.5
<b>Pipe <math>\varnothing</math> 200 mm – SMA wire <math>\varnothing</math> 2 mm</b>															
2	3	4	20.1	27.4	-420.6	-450.2	-488.0	<b>-452.9</b>	-72.6		-308.3	2.46	-13.8	317.1	995.7
3	3	-1	20.3	26.0	-615.7	-486.9	-537.2	<b>-546.6</b>	-57.0		-483.6	3.17	-17.6	408.2	1,281.8
4	3	3	52.9	41.1	-388.8	-754.6	-420.3	<b>-521.2</b>	117.8		-639.0	3.38	-18.8	435.5	1,367.4
5	3	2	20.4	26.2	-537.7	-486.9	-615.8	<b>-546.8</b>	-57.8		-489.0	3.17	-17.6	407.7	1,280.2
6	3	7	21.2	30.1	-298.9	-383.8	-319.8	<b>-334.2</b>	-89.0		-245.2	1.59	-8.8	204.4	641.8
<b>Pipe <math>\varnothing</math> 200 mm – SMA wire <math>\varnothing</math> 3 mm</b>															
7	3	3	14.5	19.9	-727.1	-662.5	-467.3	<b>-618.9</b>	-54.5		-564.4	3.66	-20.3	210.2	1,485.0
8	3	4	24.6	38.8	-724.9	-458.1	-683.6	<b>-607.2</b>	-141.0		-466.2	3.02	-16.8	173.5	1,225.7

Pipe $\varnothing$ 250 mm – SMA wire $\varnothing$ 1 mm														
9	4	-1	19.6	24.9	-137.5	-135.3	-129.9	<b>-134.3</b>	-52.7	-81.6	0.43	-2.9	276.4	217.0
Pipe $\varnothing$ 250 mm – SMA wire $\varnothing$ 2 mm														
10	3	4	24.1	37.0	-344.5	-	-415.9	<b>-380.2</b>	-129.0	-251.2	1.33	-9.0	213.7	670.9
11	4	0	20.2	25.0	-295.7	-412.5	-341.4	<b>-349.9</b>	-47.8	-302.1	1.6	-10.9	256.9	806.7
Pipe $\varnothing$ 250 mm – SMA wire $\varnothing$ 3 mm														
12	4	-1	19.6	24.9	-514.3	-683.3	-549.0	<b>-582.2</b>	-52.7	-529.5	2.81	-19.1	201.0	1,419.9
13	4	10	28.1	33.1	-173.1	-139.6	-	<b>-156.4</b>	-49.9	-106.5	0.56	-3.8	40.4	284.4
Pipe $\varnothing$ 300 mm – SMA wire $\varnothing$ 1 mm														
14	4	0	29.6	31.9	-108.5	-105.4	-114.4	<b>-109.5</b>	-22.4	-87.1	0.39	-3.1	229.1	234.8
Pipe $\varnothing$ 300 mm – SMA wire $\varnothing$ 2 mm														
15	3	-2	23.0	23.1	-597.2	-760.5	-574.6	<b>-644.1</b>	-1.7	-642.4	2.88	-23.1	533.6	1,738.3
16	4	-1	15.8	19.0	-482.3	-554.4	-458.0	<b>-498.2</b>	-32.4	-465.8	2.09	-17.9	429.3	1,348.1
Pipe $\varnothing$ 300 mm – SMA wire $\varnothing$ 3 mm														
17	3	1	28.4	30.3	-153.8	-172.8	-177.8	<b>-168.1</b>	-18.1	-150.0	0.67	-5.4	57.7	407.3
18	4	9	25.8	5.1	-200.6	-266.1	-178.2	<b>-215.0</b>	206.6	-421.6	1.89	-15.2	162.0	1,144.5

The effective force in the SMA wire depends on its diameter. It can be observed also that for a part of the cylinders prestressed with the wire with a diameter of 3 mm (No 13 and 17) the force in SMA wire is much lower than for the remaining specimens of the same type (No 12 and 18, respectively). Such lower effectiveness is mainly related to the difficulty in blocking the wire ends at the beginning of the test. Additional influence may be related to degradation of the SMA wire by the flow of electrical current. The value of the electric current equal to 13 A used in these tests is much above the value influencing the properties of SMA wires, as reported for example in [22]. A summary of the detailed results is presented in Tables 7 and 8. For all types of specimens, defined by the hollow cylinder diameter and wire diameter, the mean values of the principal results are included. The mean values of the circumferential concrete strain and stress as well as the estimated force in the SMA wire at the residual state (after activation of the shape memory effect and cooling to the ambient temperature) are summarized.

**Table 7.** Mean values  $\sigma_{c,SMA}$  of circumferential compression stress in concrete resulting from prestressing with SMA wire at the residual state

	Mean circumferential compression stress in concrete resulting from prestressing with SMA wire		
	$\varnothing$ 1 mm	$\varnothing$ 2 mm	$\varnothing$ 3 mm
	Pipe $\varnothing$ 200 mm	2 MPa	16 MPa
Pipe $\varnothing$ 250 mm	3 MPa	10 MPa	11 MPa
Pipe $\varnothing$ 300 mm	3 MPa	20 MPa	10 MPa

**Table 8.** Mean values  $\sigma_{res}$  of residual stress in SMA wire at the residual state

	Mean residual stress in SMA wire $\sigma_{res}$		
	$\varnothing$ 1 mm	$\varnothing$ 2 mm	$\varnothing$ 3 mm
Pipe $\varnothing$ 200 mm	194 MPa	378 MPa	192 MPa

Pipe $\varnothing$ 250 mm	276 MPa	235 MPa	120 MPa
Pipe $\varnothing$ 300 mm	299 MPa	478 MPa	110 MPa
Average	256.3 MPa	363.7 MPa	140.7 MPa

526

527

### 7.2. The influence of preliminary wire deformation on prestressing effectiveness

528

529

530

531

532

533

534

535

536

537

538

539

540

541

542

543

544

545

546

547

548

549

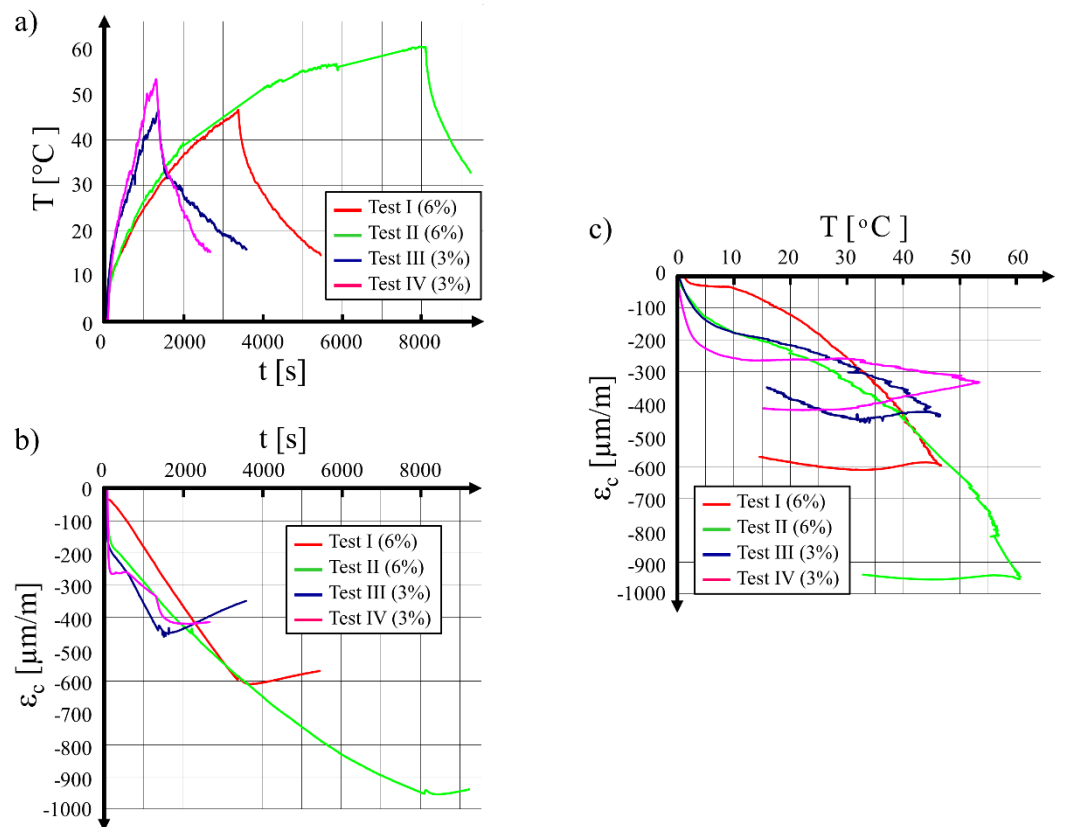
For the investigation of the relationship between the value of the initial predeformation of the wire and the level of prestressing obtained in the concrete hollow cylinders, four specimens with external diameters of 250 mm prestressed with Ni-Ti wire with a diameter of 2 mm were tested. The initial predeformation was at two different values (6% and 3%); there were two cylinders for each predeformation value. Tests I and II refer to the initial predeformation of 6%, while tests III and IV refer to the 3% predeformation.

After the initial predeformation, the wire was wound on the hollow cylinder and was connected to the electrical current. A diagram of wire temperature variations over time during the heating and cooling periods is presented in Fig. 5a for the four tests. It may be observed that after connecting the electrical power, the wire predeformed to 3% heated much faster than the wire predeformed to 6%. The time needed for heating the wires to 45°C for tests I and II is 3,000 s, which is three times more than the time needed for the heating of specimens III and IV.

Variations of the circumferential concrete strain as a function of SMA wire heating time for the four tests are shown in Fig. 5b. It is observed that the strain increase in the first 1,500 s of heating is similar for all four tests. Afterwards, the concrete strain in tests III and IV decreases as an effect of the wire cooling, while for tests I and II, the concrete strain increases during the whole period of heating of the longer wire.

Variations of the concrete strain in the circumferential direction related to temperature for the four tests described above are presented in Fig. 5c. For the sake of comparison, all concrete strain values were captured for the SMA wire temperature of 45°C.





**Figure 5.** Results captured during tests with Ni-Ti wire with a diameter of 2 mm wound on the 250-mm-diameter pipeof: a) wire temperature variations over time during electric heating, then cooling; b) variations of circumferential concrete strain over time; c) variations of circumferential concrete strain as a function of temperature. Note that measurements for test II were stopped before the specimen was cooled to the ambient temperature

- Test I (initial predeformation 6%), -545  $\mu\text{m}/\text{m}$ ;
- Test II (initial predeformation 6%), -547  $\mu\text{m}/\text{m}$ ;
- Test III (initial predeformation 3%), -428  $\mu\text{m}/\text{m}$ ;
- Test IV (initial predeformation 3%), -305  $\mu\text{m}/\text{m}$ .

The results collected during the tests performed allow the following conclusions to be formulated:

- SMA wire predeformed to a higher initial strain value needs a longer duration of electrical current flow to reach the expected temperature. In the case of wire with a diameter of 2 mm and predeformed to 6%, the time needed to reach a temperature of 45°C is three times longer than the time needed to heat the same wire predeformed to 3%.
- As a consequence of the longer heating time required for the wire predeformed to 6%, the concrete hollow cylinder is also heated more and this provokes an additional thermal deformation of the concrete.
- At a wire temperature of 45°C, the circumferential strain of the concrete in the hollow cylinder prestressed with the wire predeformed to 6% is around 50% higher than the strain in the concrete hollow cylinder with the wire predeformed to 3%; the

576 measured concrete strain includes the influence of prestressing with the SMA wire  
577 and the thermal deformation of the concrete.

- 578 • It can be seen in Fig. 5c that for the hollow cylinder prestressed with wire subjected  
579 to 6% predeformation, a higher final strain is preserved after cooling, and this means  
580 that the residual stress ( $\sigma_{res}$ ) in this wire is higher than in the case of a wire  
581 predeformed to 3%.

## 582 8. Comments on tests conditions

### 583 8.1. Conditions for performing the prestressing of concrete hollow cylinders with the use of SMA 584 wires activated with an electrical current

585 During the tests, attention was paid to the proper registration of the concrete strain  
586 and the temperature of the internal surface of the hollow cylinders as well as that of the  
587 wire. The results were used for the determination of the final stress in the concrete hollow  
588 cylinders in the circumferential direction and the residual stress  $\sigma_{res}$  in the wound wire. A  
589 constant pitch of the wound wires of 4 mm was successfully achieved in order to exclude  
590 any risk of electrical short circuit. Nevertheless, the following potential imperfections of  
591 the tests were observed:

- 592 1. Limited space between the wires eliminated the possibility to install temperature  
593 sensors on the external surface of the hollow cylinders. For the needs of analysis, it  
594 was assumed that the external surface temperature was equal to the temperature of  
595 the wound wire – such an assumption is rather rough as contact between the wires  
596 and the concrete is not uniform.
- 597 2. As a consequence of the above point, the external concrete surface was not heated  
598 evenly.
- 599 3. During the execution of the prestressing of the hollow cylinders, their position was  
600 vertical and this could have inhibited the ventilation and cooling of the internal  
601 surface.

602 The speed of increase of the wire temperature under the influence of current flow  
603 depends on the type of wire as well as its diameter. Together with the temperature of the  
604 wires, the temperature of the concrete cylinders also increased. The progress of these  
605 variations depends on the current parameters, the wire impedance, the wire and cylinder  
606 thermal capacity and the ambient temperature. Diagrams of the temperature increase of  
607 the wire and concrete above the initial level registered during prestressing of the hollow  
608 cylinders are presented in Fig. 6. In each case, after reaching the required temperature  
609 level, the electrical current was disconnected and the temperature of the wire and con-  
610 crete decreased.  $\Delta T$  is the increase of temperature of the internal surface of the hollow  
611 cylinder and of the wire from their initial levels. Every temperature measurement was  
612 started before connection of the SMA wire to the current source.

613 The temperature variation of the Ni-Ti wire with a diameter of 1 mm is the most  
614 rapid of all wire diameters. The maximal value of the wire temperature is reached after 6  
615 to 10 mins of heating. At the same time, the temperature of the internal surface of the  
616 concrete remains low (10°C to 30°C), so the temperature gradient between the SMA wire  
617 and the internal concrete surface may reach around 75°C after 3 mins of heating (as is the  
618 case for the hollow cylinder with a diameter of 250 mm). After 5 mins, this gradient drops  
619 to 30°C. For all specimens, the temperature of the wire decreases quickly after the end of  
620 heating, while the temperature of concrete after reaching its maximum decreases less  
621 quickly. For the hollow cylinders with a diameter of 200 mm, the temperature of the  
622 concrete 7 mins after the test is higher than the temperature of the wire. This may be ex-  
623 plained by the lowest thermal capacity of the 200-mm concrete cylinder from all speci-  
624 mens. For hollow cylinders of 250 mm and 300 mm prestressed with the 1-mm-diameter  
625 wire, the temperature of the wire and of the concrete become equal after 20 mins, while

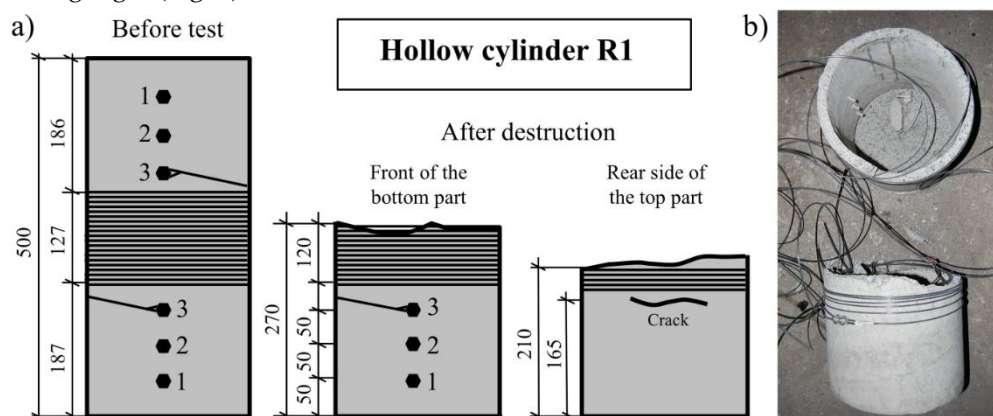
for the 200-mm cylinder, the concrete temperature is higher for a much longer period of time.

Prestressing of the concrete hollow cylinders with SMA wires with diameters of 2 mm and 3 mm requires a substantially longer heating time as under the effect of lower electrical impedance of the material, less heat is released. A heating time of 20 to 30 mins also results in a systematic increase of temperature of the internal surface of the hollow cylinder. The temperature gradient during the heating time does not exceed 25°C (Fig. 6b and Fig. 6c). At the moment when the current was disconnected, a sudden drop of wire temperature in the range of 20°C is observed followed by further cooling. Measurements of the concrete surface temperature do not reveal any instantaneous drop of temperature. It shows that the progress of the cooling of the concrete is slow and the temperature measured on the internal surface of the hollow cylinder is at most 20°C higher than the wire temperature for the whole time until the end of the test. A similar observation is observed for the cylinders of 250 mm and 300 mm as for the 200-mm cylinder prestressed with 1 mm wire – the concrete temperature is decreasing slowly and wire temperature is lower during cooling time. This is understood as the influence of the thermal capacity of the parts of the specimen.

### 8.2. The failure of two hollow cylinders during the tests

During the execution of the entire testing program, two failures of concrete hollow cylinders occurred, as is typical for a new direction of research – two hollow cylinders (R1 and R2), each with an external diameter of 300 mm, broke during prestressing. In the first case, hollow cylinder R1 (Fig. 6) was subjected to prestressing with Ni-Ti wire with a diameter of 3 mm which was predeformed to the initial deformation level of 6%. After winding the wire over the hollow cylinder, the prestressing operation commenced. Direct electrical current with density  $I = 15$  A and voltage  $U = 50.8$  V was used in this case. The whole test took only 350 s (including 280 s of heating time). During this time, the wire temperature increased by  $\Delta T = 9.0^\circ\text{C}$  (quantity of the released heat  $Q = 213$  kJ).

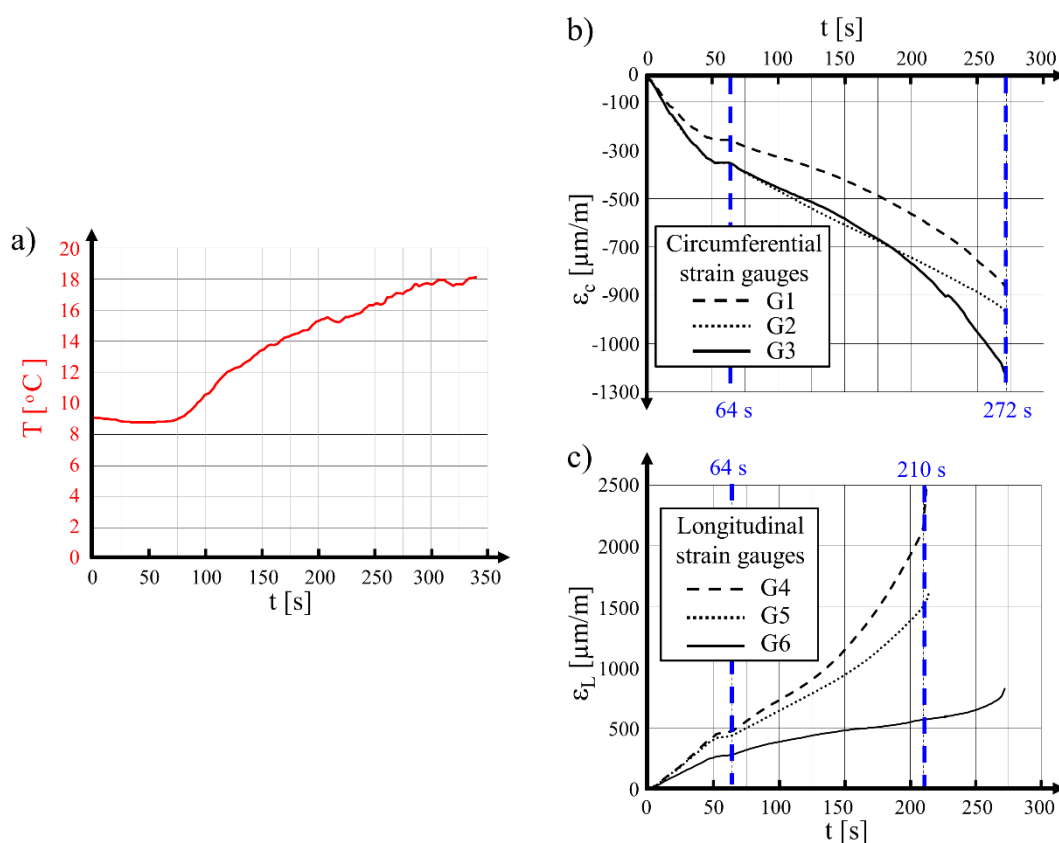
The wire temperature increase in relation to time and variations of concrete strain on the internal surface of the hollow cylinder in the longitudinal and circumferential directions are shown in Fig. 7. Analysis of the concrete strain variations presented in Fig. 7b and in Fig. 7c allows us to state that at 64 s from the start of the test, when the electric current was connected, the concrete strain starts to grow linearly until 125 s and further more intensive strain increase in the longitudinal direction captured by strain gauges G5 and G4 is observed. The two strain gauges G5 and G4 were damaged nearly simultaneously after 210 s of the test, reaching strain at the levels of 1,500 and 2,100  $\mu\text{m}/\text{m}$  respectively (Fig. 7c). This means that at the location of the strain gauges, concrete cracking appeared in the circumferential direction, perpendicular to the longitudinal direction of the strain gauges (Fig. 6).



665 **Figure 6.** R1 hollow cylinder before and after its destruction: a) drawing of the specimen before  
 666 destruction, front of the bottom part and rear side of the bottom part after destruction; b) photo of  
 667 the R1 specimen after its destruction  
 668

669 During further execution of the test program, concrete strains recorded with the  
 670 strain gauges installed in the circumferential direction linearly increased up to 250 s. Af-  
 671 ter this moment, a significant increase of the strains registered by gauges G1 and G3 is  
 672 observed. Destruction of all strain gauges in the circumferential direction and in one  
 673 longitudinal direction (G6) occurred simultaneously at 275 s. The upper part of the hol-  
 674 low cylinder separated from the lower part with a bang and was thrown to a height of  
 675 around 1.5 m. Loosened coils of the Ni-Ti wire absorbed its kinetic energy and the sepa-  
 676 rated part fell to the floor. The Ni-Ti wire was neither broken nor damaged (Fig. 6b).  
 677 In the other case, the hollow cylinder R2 was destroyed during prestressing with the same  
 678 diameter of Ni-Ti wire (3 mm). The specimen was prepared according to the procedure  
 679 described in 4. Wire predeformed to 3% was wound on the hollow cylinder. An electrical  
 680 current with a density of  $I = 20$  A and a voltage of  $U = 70$  V was connected. The temper-  
 681 ature variations over time measured for the wire and for the internal surface of the hol-  
 682 low cylinder (Table 6, No. 18) are presented in Fig. 8a.

683 Analysis of the presented diagrams leads to the conclusion that the wire was quickly  
 684 heated to a temperature of  $38.7^{\circ}\text{C}$ , while on the internal surface of the concrete hollow  
 685 cylinder, the temperature was nearly stable for a period of 100 s and remained at a level  
 686 of  $+5^{\circ}\text{C}$ . After 136 s from the start of the test, the difference between temperatures on the  
 687 external and internal surfaces of the hollow cylinder was  $32^{\circ}\text{C}$ . At this time, the hollow  
 688 cylinder burst was observed 0.21 m from the bottom. The final temperatures of the wire  
 689 and concrete were  $26^{\circ}\text{C}$  and  $5^{\circ}\text{C}$ , respectively.  
 690

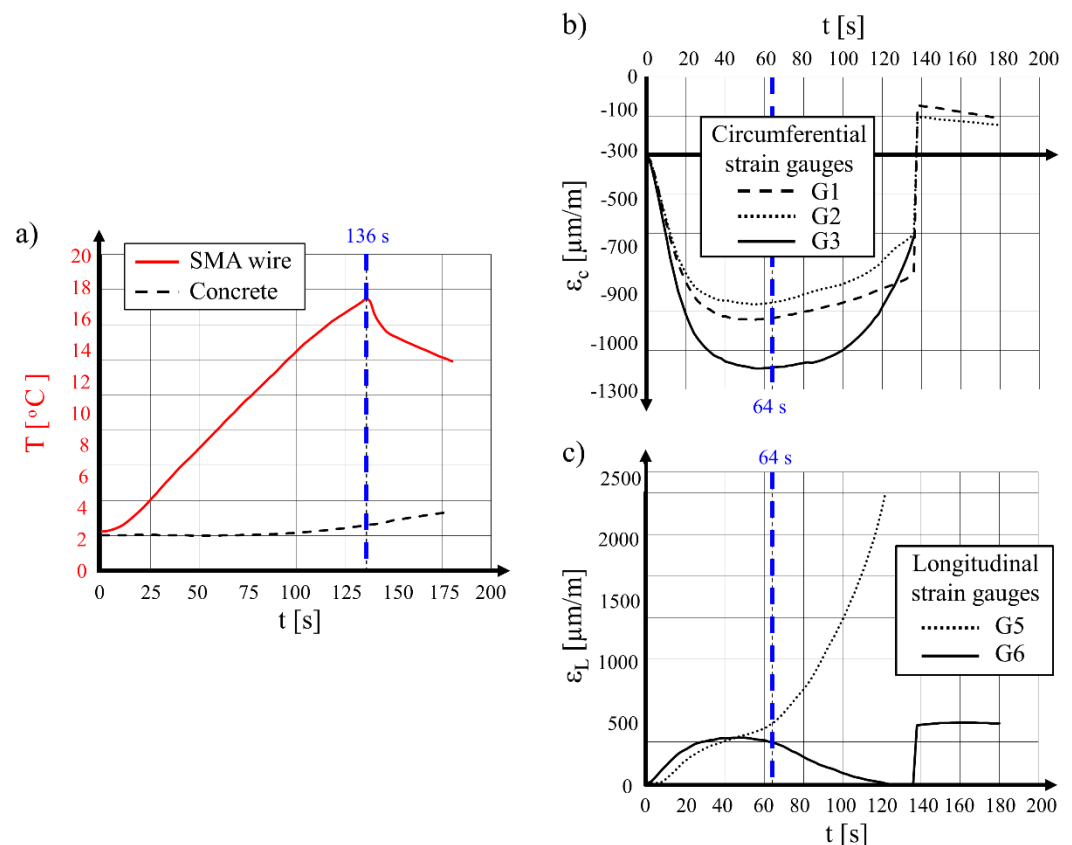


692 **Figure 7.** Results recorded during testing of the 300-mm hollow cylinder prestressed with 3-mm  
 693 SMA wire – specimen R1: a) temperature over time for the Ni-Ti wire; b) circumferential strain for  
 694 concrete; c) longitudinal strain for concrete

695  
 696 A careful analysis of the strain development in concrete in both measured directions  
 697 shown in Figs. 8b and 8c brings clear information that an important moment in the test  
 698 was occurred after 64 s of wire heating. At this time, the circumferential strain reaches its  
 699 maximal value and the longitudinal strain starts to rapidly increase or decrease.

700 The above described conditions are characteristic of the moment of creation of the  
 701 circumferential cracks, perpendicular to the longitudinal direction of the hollow cylinder.  
 702 The temperature difference (gradient) between the external and internal surfaces of the  
 703 concrete at 64 s is 16°C. Considering the value of concrete elasticity modulus at the level  
 704 of 36 GPa, this gives a tensile stress in concrete of 5.9 MPa. The estimated value is higher  
 705 than the concrete tensile resistance in the axial load, and is 4.4 MPa on the basis of labor-  
 706 atory tests.

707 To conclude, it is expressed that hollow cylinder failures were provoked by stress  
 708 exceeding concrete tensile resistance. Thermal actions generated at the time of cylinders  
 709 prestressing, together with load applied to hollow cylinders by means of wound wire  
 710 with prestressing force activated within it, were the cause of the damage.  
 711  
 712



713 **Figure 8.** Results recorded during testing of the 300-mm hollow cylinder prestressed with 3-mm  
 714 SMA wire – specimen R2: a) temperature variations of the wire and of the concrete specimen inter-  
 715 nal surface over time; b) strain variations of concrete in the circumferential direction over time;;  
 716 c) strain variations of concrete in the longitudinal direction over time

## 9. Conclusions

As a result of the performed research, following conclusions can be drawn:

- Cylindrical concrete elements may be effectively prestressed with use of initially predeformed wire formed from shape memory alloy (SMA), in which prestressing is activated in the method of heating the wires with a flow of electrical current.
- Values of the circumferential compressive stress in concrete  $\sigma_c$  as well as values of permanent stress in the SMA wires  $\sigma_{res}$  depend on the type and diameter of the wire, the initial predeformation value and the hollow cylinder diameter and thickness.
- Prestressing of the concrete hollow cylinders with SMA wires with a higher level of initial deformation (6%) is more effective as it brings higher values of circumferential compression stress in concrete  $\sigma_c$  as well as higher values of permanent stress in the prestressing wire  $\sigma_{res}$  than for the specimens with wire predeformation of 3%.
- The performed testing program showed that activation of the shape memory effect in the wires with use of a flow of electrical current is effective in practical usage. The selection of the Ni-Ti wire diameter should relate to the conditions of the prestressing execution. It should be noted that wire predeformed to 6% requires a much longer action of electrical current than wires predeformed to 3%. Longer heating of SMA wires also results in the heating of concrete and this may lead to thermal deformation of the concrete.
- Too much heat in the wire may result in a high thermal gradient in the hollow cylinder wall which consequently may provoke high tensile stress in concrete; such conditions may provoke exceeding of the concrete tensile strength and ultimately, the failure of the hollow cylinder. Overheating may also damage the SMA wire.

**Author Contributions:** Conceptualisation, A.S. and J.-F.D.; methodology, P.G., A.D.; software, A.S.; validation, A.D., A.S. and X.B.; formal analysis, A.D.; investigation, A.D.; resources, J.F.D. and P.G.; data curation, A.D.; writing—original draft preparation, A.D., X.B. and P.G.; writing—review and editing, P.G. and X.B.; visualisation, P.G. and X.B.; supervision, J.-F.D. and A.S. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research received no external funding

**Institutional Review Board Statement:** Not applicable

**Informed Consent Statement:** Not applicable

**Data Availability Statement:** The data presented in this study are available on request from the corresponding author

**Conflicts of Interest:** The authors declare no conflict of interest

## References

1. Abdel Baky, H.; Kotynia, R.; Neale, K.W. Nonlinear FE analysis of RC beams strengthened in flexure with NSM CFRP systems. Proceedings of the Sixth International Conference Analytical Models and New Concepts in Concrete and Masonry Structures (AMCM 2008), Łódź, Poland, 9–11 June 2008.
2. Kotynia, R.; Walendziak, R.; Stoecklin, I.; Meier, U. RC slabs strengthened with prestressed and gradually anchored CFRP strips under cyclic loading. Proceedings of the Sixth International Conference Analytical Models and New Concepts in Concrete and Masonry Structures (AMCM 2008), Łódź, Poland, 9–11 June 2008.
3. Kotynia, R. Shear strengthening of RC beams with polymer composites. Associate Professor Thesis, University of Łódź, Poland, 2011.
4. Otsuka, K.; Ren, X. Physical metallurgy of Ti-Ni-based shape memory alloys. *Prog. Mater. Sci.* **2005**, *50*, 511–678.
5. Otsuka, K.; Wayman, C.M. *Shape memory materials*; Cambridge University Press: Cambridge, UK, 1999.
6. Lexcellent, C. *Shape-memory alloys handbook*; ISTE & Wiley: London, UK & Hoboken, NJ, USA, 2013.
7. Ziółkowski, A. *Pseudoelasticity of shape memory alloys: theory and experimental studies*; Butterworth-Heinemann: Oxford, UK, 2015.
8. Kaszuwara, W. Stopy z pamięcią kształtu. *Inżynieria Materiałowa / Materials Engineering*, R. XXV, nr 2, 61–64, 2004.
9. El-Tawil, S.; Ortega-Rosales, J. Prestressing concrete using shape memory alloy tendons. *ACI Struct. J.* **2004**, *101*, 846–851.

- 770 10. Janke, L.; Czaderski, C.; Motavalli, M.; Ruth, J. Applications of shape memory alloys in civil engineering structures – Over-  
771 view, limits and new ideas. *Mater. Struct.* **2005**, *38*, 576–592.
- 772 11. Krstulovic-Opara, N.; Naaman, A.E. Self-Stressing Fiber Composites. *ACI Struct. J.* **2000**, *97*, 335–345.
- 773 12. Krstulovic-Opara, N.; Thiedeman, P.D. Active confinement of concrete members with self- stressing composites. *ACI Mater. J.*  
774 **2000**, *97*, 297–308.
- 775 13. Moser, K.; Bergamini, A.; Christen, R.; Czaderski, C. Feasibility of concrete prestressed by shape memory alloy short fibers.  
776 *Mater. Struct.* **2005**, *38*, 593–600.
- 777 14. Costanza, G.; Paoloni, S.; Tata, M.E. IR thermography and resistivity investigations on Ni-Ti Shape Memory Alloy. In *Materials*  
778 *and Applications for Sensors and Transducers III*, Proceedings of the 3rd International Conference on Materials and Applications  
779 for Sensors and Transducers (IC-MAST), Prague, Czech Republic, Sept 13-17, 2013; Hristoforou, E., Vlachos, D.S., Eds.; Trans  
780 Tech Publications Ltd: Durnten-Zurich, Switzerland, 2014. Key Engineering Materials, Vol. 605, pp. 23–26.
- 781 15. Choi, E.; Chung, Y.S.; Cho, B.S.; Nam, T.H. Confining concrete cylinders using shape memory alloy wires. *Eur. Phys. J.-Spec.*  
782 *Top.* **2008**, *158*, 255–259.
- 783 16. Destrebecq, J.F.; Balandraud, X. Interaction between concrete cylinders and shape-memory wires in the achievement of active  
784 confinement. In *Materials with complex behaviour: modelling, simulation, testing, and applications. Advanced Structured Materials;*  
785 *Ochsner, A.; DaSilva, L.F.M.; Altenbach, H., Eds.; Springer-Verlag Berlin Heidelberg: Berlin, Germany, 2010; Volume 3, pp.*  
786 *19–34. [https://doi.org/10.1007/978-3-642-12667-3\\_2](https://doi.org/10.1007/978-3-642-12667-3_2)*
- 787 17. Choi, E.; Park, S.H.; Cho, B.S.; Hui, D. Lateral reinforcement of welded SMA rings for reinforced concrete columns. *J. Alloy*  
788 *Compd.* **2013**, *577* (Suppl. 1), S756–S759.
- 789 18. Tran, H.; Balandraud, X.; Destrebecq, J.F. Curvature effect on the mechanical behaviour of a martensitic shape-memory-alloy  
790 wire for applications in civil engineering. *Smart Mater. Struct.* **2015**, *24*, 025025.
- 791 19. Pan, S.; Yue, R.; Hui, H.; Fan, S. Lateral cyclic behavior of bridge columns confined with pre-stressed shape memory alloy  
792 wires. *J. Asian Archit. Build.* **2020**. <https://doi.org/10.1080/13467581.2020.1818568>
- 793 20. Hong, C.K.; Qian, H.; Song, G.B. Uniaxial compressive behavior of concrete columns confined with superelastic shape memory  
794 alloy wires. *Materials* **2020**, *13*, 1227.
- 795 21. Tran, H.; Balandraud, X.; Destrebecq, J.F. Improvement of the mechanical performances of concrete cylinders confined actively  
796 or passively by means of SMA wire. *Arch. Civ. Mech. Eng.* **2015**, *15*, 292–299.
- 797 22. Debska, A. Utilisation d’alliages à mémoire de forme pour la création d’effets de précontrainte dans des composants en béton.  
798 (in French; Use of shape memory alloys for the creation of prestressing effects in concrete components), PhD thesis, Université  
799 Blaise Pascal - Clermont-Ferrand II, France, 2014.
- 800 23. Debska, A.; Gwozdziwicz, P.; Seruga, A.; Balandraud, X.; Destrebecq, J.F. Prestress state evolution during thermal activation  
801 of memory effect in concrete beams strengthened with external SMA wires. *Arch. Civ. Mech. Eng.* **2020**, *20*, 142.
- 802 24. Debska, A.; Balandraud, X.; Destrebecq, J.F.; Gwozdziwicz, P.; Seruga, A. Influence of thermal boundary effects on the process  
803 of creating recovery stresses in a SMA wire activated by Joule heating. *J. Mater. Eng. Perform.* **2017**, *26*, 3336–3346.
- 804 25. Wang, ZG; Zu, XT; Feng, XD; Zhu, S; Bao, JW; Wang, LM. Characteristics of two-way shape memory TiNi springs driven by  
805 electrical current. *Mater. Des.* **2004**, *25*, 699–703.
- 806 26. Instrukcja Instytutu Techniki Budowlanej. Laboratoria Budowlane. Praca zbiorowa (in Polish; Instruction of Institut Techniki  
807 Budowlanej. Construction Laboratories), Instytut Techniki Budowlanej Warszawa 1971, s.1–196, Poland.
- 808
- 809