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► To cite this version:

Quoc Anh Tran, Bastien Chevalier, Pierre Breul. Spectral Analysis of the Response of Coarse Granular Material to Dynamic Penetration Test Modelled with DEM. *International Journal of Geosynthetics and Ground Engineering*, 2018, 4, pp.22. 10.1007/s40891-018-0139-5 . hal-01885925

HAL Id: hal-01885925

<https://uca.hal.science/hal-01885925>

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Spectral analysis of the response of coarse granular material to dynamic penetration test modelled with DEM

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Abstract

Dynamic penetration tests are often used to determine the strength properties of surface soils. The paper presents a study on the use of spectral analysis on dynamic cone penetration tests results, modelled with Discrete Element Method. This method is applied to assess the effect of the variation of the grain size distribution of the soil on test results. A two-dimensional discrete model is used to reproduce cone penetration tests in dynamic conditions: the tip of the penetrometer is driven in the material by successive impacts of a hammer on the penetrometer. For each impact of the hammer, a curve of the load applied by the tip on the soil is obtained versus the penetration distance of the tip. The curves of the load vs. penetration traditionally used to calculate the tip resistance of the soil are analyzed with Discrete Fourier transform in order to investigate curve's shape. The effect of the variation of the grain size distribution of the soil on these curves is investigated, i.e. average particle diameter and span of particle size distribution. It was found out that the grain size distribution influences tip resistance but also the shape and oscillation modes of the curve of the stress-penetration curve. Based on these indicators, the exploitation of the load-displacement curve obtained with dynamic penetration tests could be enlarged to determine other properties of the soils.

Keywords: dynamic cone penetration, discrete element method, granular material, particle size distribution, Discrete Fourier Transform.

1. Introduction

In the practice of geotechnical engineering, the use of in situ testing is widespread. Among existing testing techniques, lightweight dynamic penetration testing device such as Panda penetrometer is used to characterize mechanical properties of surface soils [1,2]. Based on recent technological improvements, this device is able to record the curve of the tip stress or tip force versus the tip penetration distance for each impact of the hammer on the penetrometer [3,4]. This curve, referred to as load-penetration curve, provides information on dynamic tip resistance but also on additional mechanical parameters involved during the driving of the tip [3,5,6]. Cone penetration test is a blind testing technique, because there is no sampling of the different layers of soils that are cut across. It would be very interesting to be able to get information about the nature of the soils, from the actual measurements recorded by the device. The present paper proposes to study the effect of the particle size distribution on the load vs. penetration distance measured at the tip. Numerical modelling using Discrete Element Method

was chosen so that we have a strict control on the parameters of the particle size distribution (PSD).

The numerical model of penetration tests using Discrete Element Method (DEM) used to reproduce the penetration tests in dynamic conditions is the same model as the one presented in [7]. Many authors have modeled cone penetration tests before with DEM in 2D [8-15] and in 3D [3,16-20]. However, most of them modelled the penetration in static conditions, i.e. with a constant velocity of the tip, and very few focused on penetration tests in dynamic conditions, i.e. with impacts [6,7,19].

At the macroscopic scale, the tip resistance quantifies the mechanical response of the granular material to the driving of the tip (Fig.1). At the scale of the contacts or of the particles, the shapes of the load-penetration curves are analyzed in terms of both frequency and amplitude of signal oscillation by using Discrete Fourier Transform (DFT). Figure 2 shows an example of the load penetration curve. The objective of the study is to evaluate the effect of the PSD on the load-penetration curves, based on DFT analysis. Two parameters were tested: the average particle diameter, D_{50} and the span of the PSD given as the ratio of maximal particle diameter D_{max} to minimal diameter D_{min} .

At first, we will present the numerical model and parameters used to reproduce the dynamic penetration test as well as the method used to analyze the load-penetration curve with DFT. Finally, the influence of the particle size distribution is discussed.

2. Numerical model

Discrete Element Method in two dimensions is used with Itasca software PFC^{2D} [21]. Dense assemblies of disks are generated without gravity and without friction in a container of 0.60 m in width and of 0.45 m in height (Fig.3). The lateral walls of the container are fixed. A study of boundary conditions with different sample sizes on this numerical model was conducted by Tran et al. [14] and revealed that for a container width larger than 0.60 m, there is no effect of the lateral walls on the tip resistance anymore. A linear contact model is used along with a Coulomb friction criterion after the generation process. The normal contact stiffness of 1.25×10^8 N/m is chosen in order to assess the assumption of rigid particles during penetration tests [22-24]. The tangential contact stiffness has been set to 0.75 of normal contact stiffness.

The samples are generated without friction and without gravity in order to reach a random close packing volume fraction, corresponding to the minimal void ratio of the considered PSD. After

sample generation, gravity is applied to the system as well as a confining vertical stress of 40 kPa. The confining stress is applied on the top face of the container to simulate an overlaying layer of material and to prevent the effects of free surface to be observed [1].

The penetration tests were performed with a frictionless rod of width $D_{rod}=14$ mm linked to a tip of width $D_{tip}=16$ mm at its bottom edge which has a friction coefficient μ_{tip} of 0.3 [19]. First, the rod is driven with constant velocity until a depth of 0.15 m is reached inside the granular material. Then, the rod is released and stabilized under its own weight. Finally, series of five successive impacts are produced in the sample with a hammer represented by an additional disk hitting the top of the rod (Fig.3). The mass of the impacting cylinder is equal to the rod mass. The impacting velocity at the impact is equal to $1,25 \text{ m.s}^{-1}$ in order to obtain an average penetration distance that is representative of experimental tests. The description of the model and the effect of the impact velocity are addressed by Tran et al. in [7]. Table 1 summarizes the main parameters of the model.

Table 2 summarizes the parameters of the five granular materials studied, with two types of PSD. The first distribution type (I) keeps constant the ratio between maximal and minimal particle diameters $D_{max}/D_{min} = 2$, and particle number varies from 10 000 to 160 000 making the average diameter D_{50} varying (Fig.4 a). The second distribution type (II) keeps constant maximal diameter $D_{max} = 7.02$ mm and the ratio between maximal and minimal particle diameters D_{max}/D_{min} varies from 2 to 10 (Fig.4 b). All the samples were tested with their maximal volume fraction (ϕ_{max}) and with a particle friction coefficient equal to 1.0.

For each type of granular material, the testing process was repeated on three different samples corresponding to the same sample conditions but with different initial particle arrangements.

The following section explains how the load-penetration curves obtained from dynamic cone penetration tests were analyzed in the frequency domain by using *DFT*.

3. Investigation of load - penetration curve

3.1. Macroscopic exploitation for the tip resistance

Tip force F_d is defined as the vertical component of the force applied by the granular material on the tip as it drives in the granular with a penetration distance s . Figure 5 shows examples of load-penetration curves $F_d = f(s)$ obtained for 3 impacts with the numerical model on the material *B*. The response obtained with the model is similar to the one classically obtained experimentally [4].

At the end of the driving process, the tip reaches a final position corresponding to a residual penetration distance s_{res} . We can notice that there is a difference between the maximal penetration distance s_{max} and the final residual penetration distance s_{res} (Fig.5). However, the mechanical work of the tip force between these two positions is negligible due to the value of the tip force between these two positions. Consequently, the dynamic tip resistance R_d of the granular material for one impact was calculated as the average tip force F_d for penetration distance between 0 and s_{max} :

$$R_d = \frac{1}{s_{max}} \int_{t=0}^{t_{s_{max}}} F_d(t) ds(t) \quad (1)$$

with: t the time; $t_{s_{max}}$ the time when penetration distance is maximal and equal to s_{max} . Then, $\langle R_d \rangle$ is the average value of dynamic tip resistances obtained for the five impacts and for the three samples.

3.2. Frequency analysis using Discrete Fourier Transform

Each load-penetration curve presents variations - i.e. oscillations, peaks - observed between the time of the impact and the time when the system stabilizes again (Fig.5). As the properties of the granular material change, the shape and size of these variations change too. Consequently, the load-penetration curve can provide not only the tip resistance of granular media but also information on the granular material properties.

Fourier transformation provides a powerful way for study discrete data acquisition in the frequency domain. It allows to decompose a signal into the frequencies that make it up. Discrete Fourier Transform (DFT) changes the N “temporal” points $y_n(x)$ in to N “frequency” points Y_k and inverse DFT the other way around by using the following equations:

$$Y_k = \sum_{n=0}^{N-1} y_n e^{-2\pi i n k / N}$$

$$y_n = \sum_{k=0}^{N-1} Y_k e^{2\pi i n k / N} \quad (2)$$

with: y_n the original function, Y_k the transformed function and N -points DFT.

The *DFT* bins (f_k) represent frequencies in the discrete Fourier transform that are spaced at intervals of $\Delta f_k = F_s / N$, where F_s is the sample rate equal to $1/\Delta x$, with Δx the recording interval. All of load-penetration curve have been analyzed in frequency domain with $F_s = 10^5 [m^{-1}]$ and frequency resolution $\Delta f_k = F_s / N = 0.1$. The equation of inverse *DFT* can be computed by the following formula:

$$y_n = \sum_{k=0}^{N-1} A_k \cos(2\pi f_k x + \varphi) \quad (3)$$

142 with: f_k the k^{th} frequency, A_k the associated amplitude and φ the phase of Y_k with

$$\varphi = \tan^{-1}(\text{Im}(Y_k)/\text{Re}(Y_k)) \quad (4)$$

143 In order to obtain a stabilized and accurate amplitude spectrum, it is necessary to ensure that
 144 the number of DFT points is sufficient. Thus, the original signal of tip force versus penetration
 145 distance is padded with trailing zeros to increase its length, before computing the DFT.

146 Figure 6 presents one example of the amplitude spectrum when the N -points of DFT is equal to
 147 1, 4 and 16 times respectively the number of data of the signal detected between $s = 0$ and
 148 $s = s_{max}$ for one impact in the material A. We found that the amplitude spectrum becomes stable
 149 when N -points DFT increases.

150 Figure 7 presents two examples of amplitude spectrum related to the materials A and C
 151 corresponding respectively to maximal and minimal average particle diameters. The first part
 152 of the spectrum i.e. $f_k < 100 [m^{-1}]$ corresponds to a transition zone where amplitude spectrum
 153 decreases rapidly. Thus, we introduce one parameter called (f_{trans}) which is the frequency
 154 corresponding to the first local minimum value of the amplitude spectrum (Fig.6).

155 In order to analyze the oscillations of the load-penetration curves, we studied the range of
 156 frequencies that provides the most significant information to rebuild the signal with inverse
 157 DFT and to filter the signal noise. For that purpose, the relative error RE between the
 158 reconstructed signal of the k first components (y_k) based on Eq. 3 and the original signal (y)
 159 described by the following equation has been computed.

$$RE = \frac{\sum_1^N \|y^i - y_{k=0:i}^i\| \times (x^i - x^{i-1})}{\sum_i^N y^i \times (x^i - x^{i-1})} \quad (5)$$

160 Figure 8 presents the relative error (RE) for one impact of the material A. The range of
 161 frequencies $[0, f_{limit}]$ that gives an RE smaller than 10% was chosen for rebuilding the signal
 162 and for the load-penetration curves analysis. Note that, the more RE decreases, the more the
 163 reconstructed signal is accurate in comparison to the raw signal.

164 Figure 9 presents one example of signal reconstruction for the material A. We found that the
 165 signal reconstructed with the frequency range $[0, f_{trans}]$ provides the general trend (baseline) of
 166 the load-penetration curve. The signal reconstructed with the frequency range $[0, f_{limit}]$ provides
 167 a reliable reconstruction of the raw signal without noise. Thus, we define the band-pass of

frequency (BF range) from f_{trans} to f_{limit} , for obtaining the full oscillation information of load-penetration curve. The reconstructed signal with $[f_{trans}, f_{limit}]$ frequency range presents the major oscillations of load-penetration curve.

4. Effect of PSD variation

The effect of PSD on the load-penetration curve in terms of tip resistance $\langle R_d \rangle$ and in frequency domain by using the frequencies detected in band-pass range $[f_{trans}, f_{limit}]$ is presented in this section. The PSD types I and II are studied in this section (Tab.2).

Figure 10 presents the load-penetration curves of 5 impacts for materials A, B and C. These materials have the same ratio $D_{max}/D_{min} = 2$ and D_{50} of respectively 7.02 mm, 3.51 mm and 1.76 mm. Figure 11 presents the load-penetration curves of 5 successive impacts for the materials A, D and E. These materials have a ratio D_{max}/D_{min} of respectively 2, 5 and 10, and the same maximal diameter D_{max} of 7.02 mm. We found that the final penetration distance and the signals oscillations amplitude increases as D_{50} decreases and D_{max}/D_{min} ratio increases.

Concerning the macroscopic response, Figure 12 shows $\langle R_d \rangle$ as function of D_{50} for the 5 different psd A to E. In general, $\langle R_d \rangle$ increases when D_{50} increases and the standard deviation decreases for smaller particles sizes. Thus, the response is more variable for coarser material. In addition, as D_{max}/D_{min} increases, we found that $\langle R_d \rangle$ slightly decreases and that the standard deviation decreases. Thus, it seems that $\langle R_d \rangle$ decreases faster as function of D_{50} than for the effect of spreading. As the quantity of smaller particles increases, the response given by the load-penetration curve is more repeatable.

The oscillations of the load-penetration curve vary as function of the combination of their frequencies f_k and the associated amplitudes A_k . We can observe on the load-penetration curves of Fig.10 and 11 that the amplitudes of oscillations decrease and the frequency increases as the material becomes finer. It is then more difficult to detect the frequency features for finer materials i.e C or E.

In order to quantify the oscillations of the load-penetration curve for each material and in order to compare them to each other, we defined the coefficient Af as the average value of the product of the frequency f_k and the associated amplitude A_k detected in the band-pass range $[f_{trans}, f_{limit}]$.

$$Af = \frac{\sum_{k=1}^n A_k \times f_k}{n} \quad (5)$$

with n the number of frequencies detected in band-pass range $[f_{trans}, f_{limit}]$.

Figure 13 presents the coefficient A_f averaged on 15 impacts for each material A to E as function of D_{50} and of PSD spreading. We found that $\langle A_f \rangle$ and its standard deviation decrease as the average diameter D_{50} decreases. The coefficient $\langle A_f \rangle$ was also found to decrease as the spreading of PSD increases. It means that the oscillations of load-penetration curve, quantified by a coefficient $\langle A_f \rangle$, are dependent on the PSD of the material tested.

5. Conclusions

In this paper, we presented a method to analyze the dynamic penetration test results, based on the Discrete Fourier Transform. This method was used on results of dynamic penetration test of Panda modelled in 2D with DEM. The method was applied to the evaluation of the variation of particle size distribution of a coarse granular material, on and more particularly the influence of average particle diameter and particle size distribution span. Five different materials were simulated under dynamic penetration test.

The discrete Fourier transform was applied on the load vs. penetration curves so that:

- the oscillations of the penetration curve can be reconstructed
- a band-pass range that characterizes the material in terms of particle size distribution can be identified
- influence of mean diameter D_{50} on the both global response and signal oscillations can be quantified with a scalar called here amplitude coefficient $\langle A_f \rangle$ calculated from the frequencies and associated amplitudes in the characteristic band-pass range. This coefficient captures only the nature of the oscillations and is influenced by particle size distribution of the material.

Concerning the macroscopic response, we observed that

- average tip resistance decreases when the content of smaller particles increases: when D_{50} decreases and when the spreading of the particle size distribution increases
- the DFT applied on signal obtained with finer granular materials shows a distribution of frequencies and associated amplitude that is more flat, in the characteristic band-pass range, making it more difficult to detect the characteristic frequency and amplitude of the oscillations for such materials.

The method presented in this paper based on spectral analysis will be useful to extract more information from the penetrometer test results, in terms of physical properties of the material, and beyond the classical tip resistance. Further investigations using three-dimensional modeling

228 and experimental validation will have to be performed in order to confirm and extend the
229 benefits of this method.

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318 Table 1. Parameters of the model.

<i>Parameter</i>	<i>Symbol</i>	<i>Value</i>	<i>Unit</i>
Width box	L	0.60	m
Height box	H	0.45	m
Particle density	ρ	2 700	kg.m ⁻³
Normal contact stiffness	k_n	1.25 x 10 ⁸	N.m ⁻¹
Tangential contact stiffness	k_s	9.375 x 10 ⁷	N.m ⁻¹
Rod friction coefficient	μ_{rod}	0.0	–
Tip friction coefficient	μ_{tip}	0.3	–

320 Table 2. Material characteristics used in penetration tests with different particle size
 321 distribution.

Ref	Particle number N _p	ϕ _{max} [-]	D _{max} [mm]	D ₅₀ [mm]	D _{max} /D _{min} [-]	Type
A	10 000	0.844	7.02	5.80	2	I;II
B	40 000	0.843	3.51	2.91	2	I
C	160 000	0.843	1.76	1.45	2	I
D	30 000	0.856	7.02	3.98	5	II
E	97 831	0.869	7.02	2.61	10	II

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Figure 11. Tip force as a function of penetration distance for 5 successive dynamic penetration tests for materials A, D and E

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Figure 13. (*Left*) $\langle Af \rangle$ as fonction of D_{50} for five particle size distributions A to E. (*Right*) $\langle Af \rangle$ as function of psd shape for three particle size distributions A, D and E (height of vertical bars represent twice the standard deviation of $\langle Af \rangle$)

Fig.01

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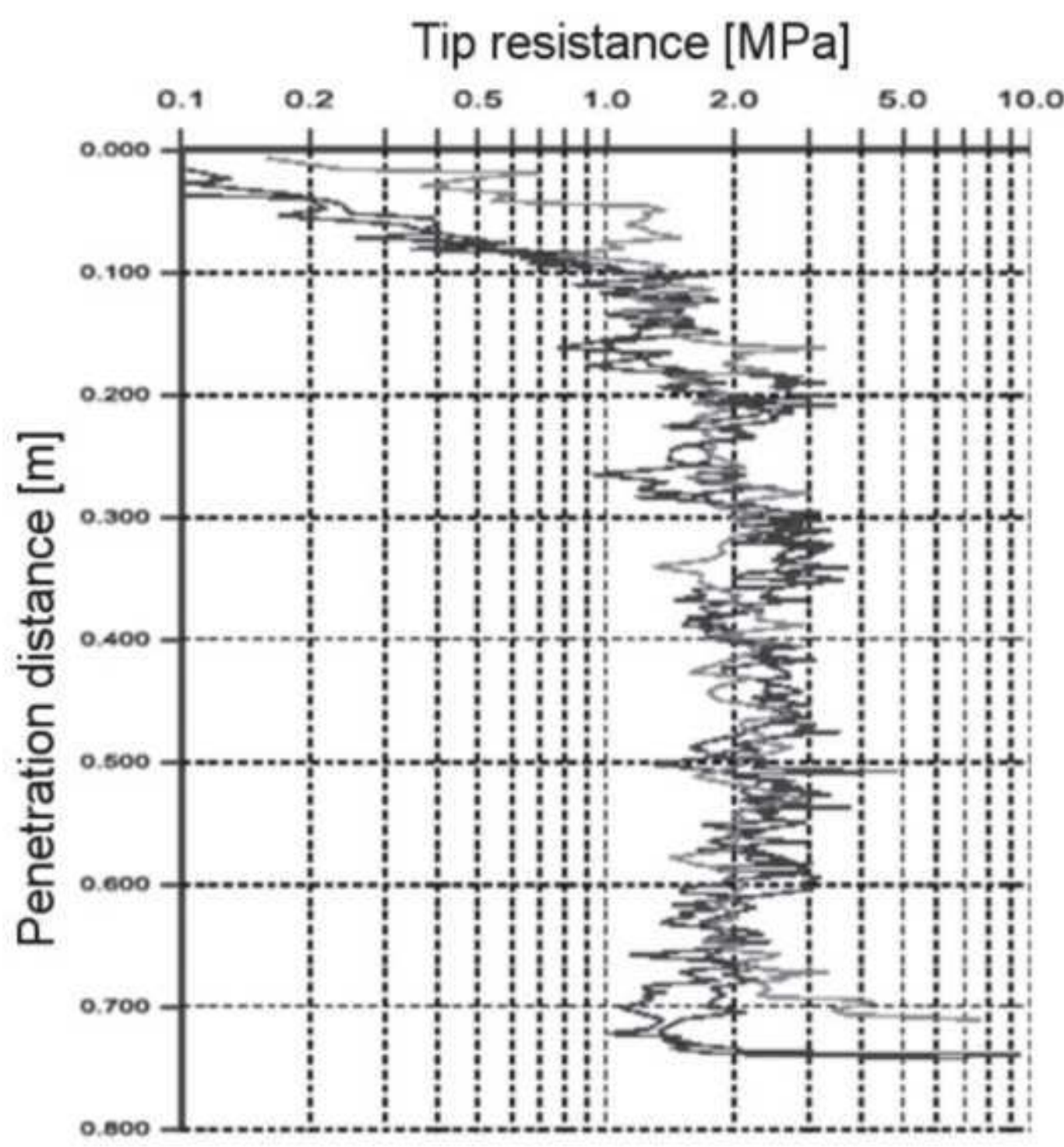
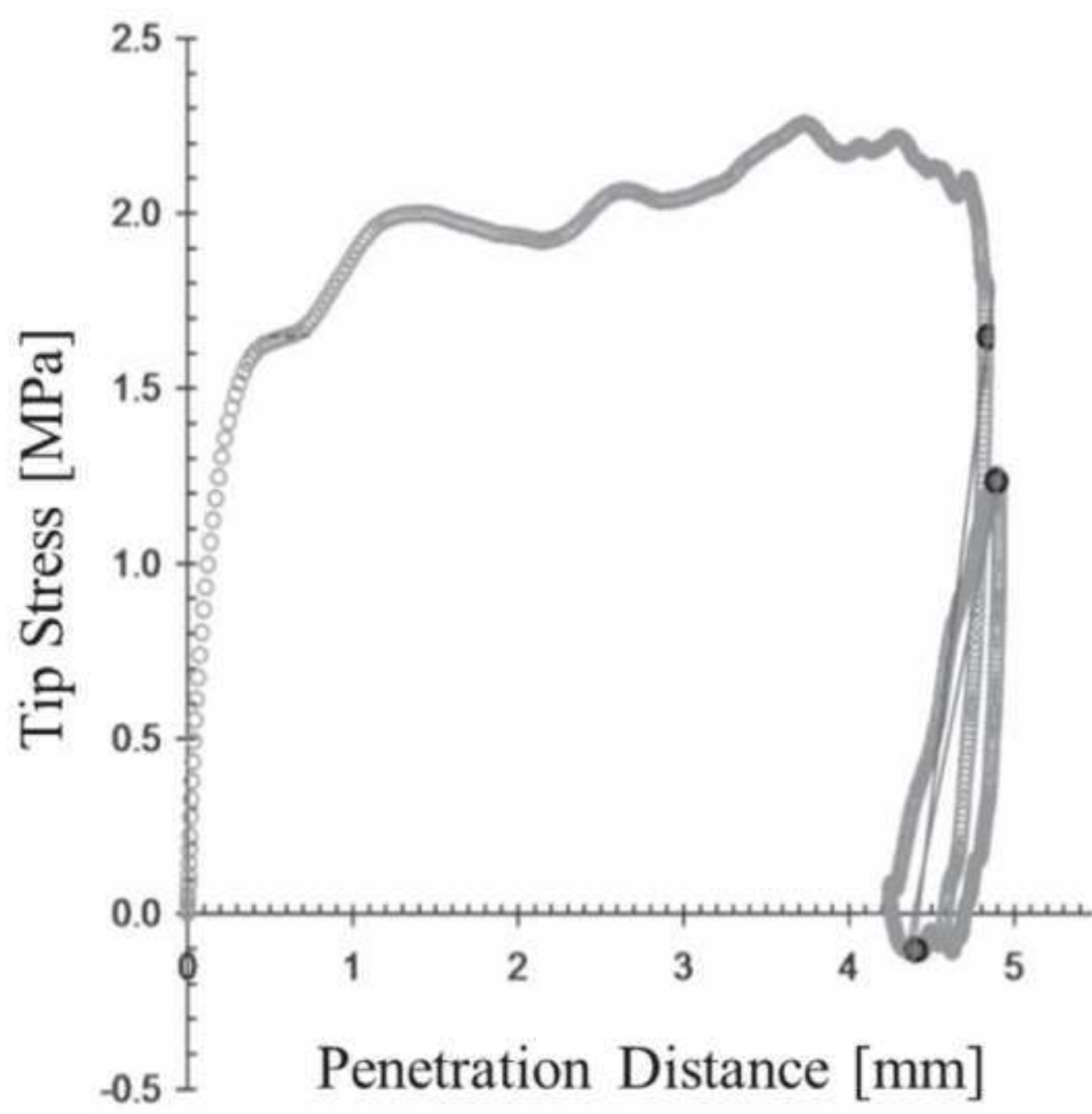
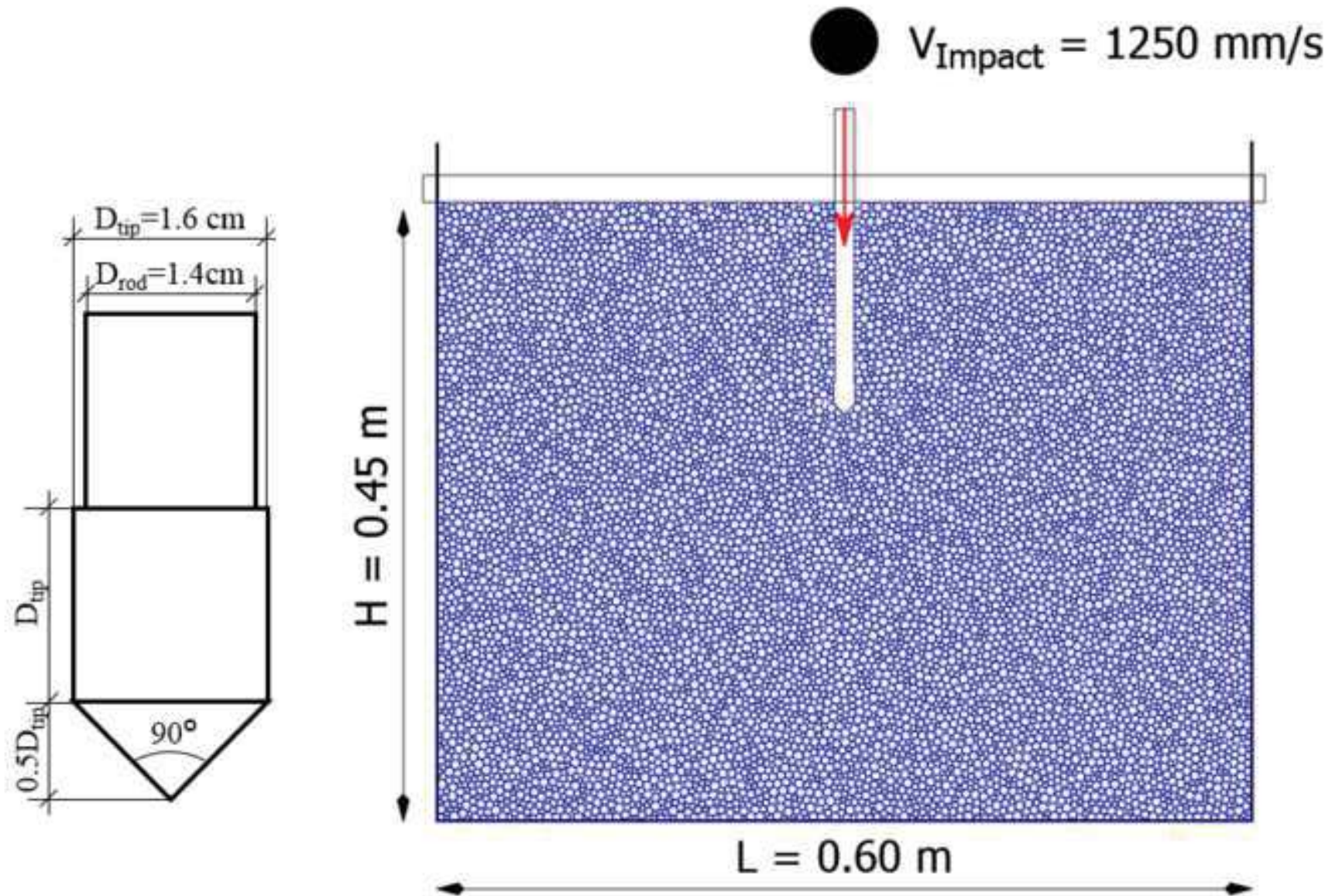
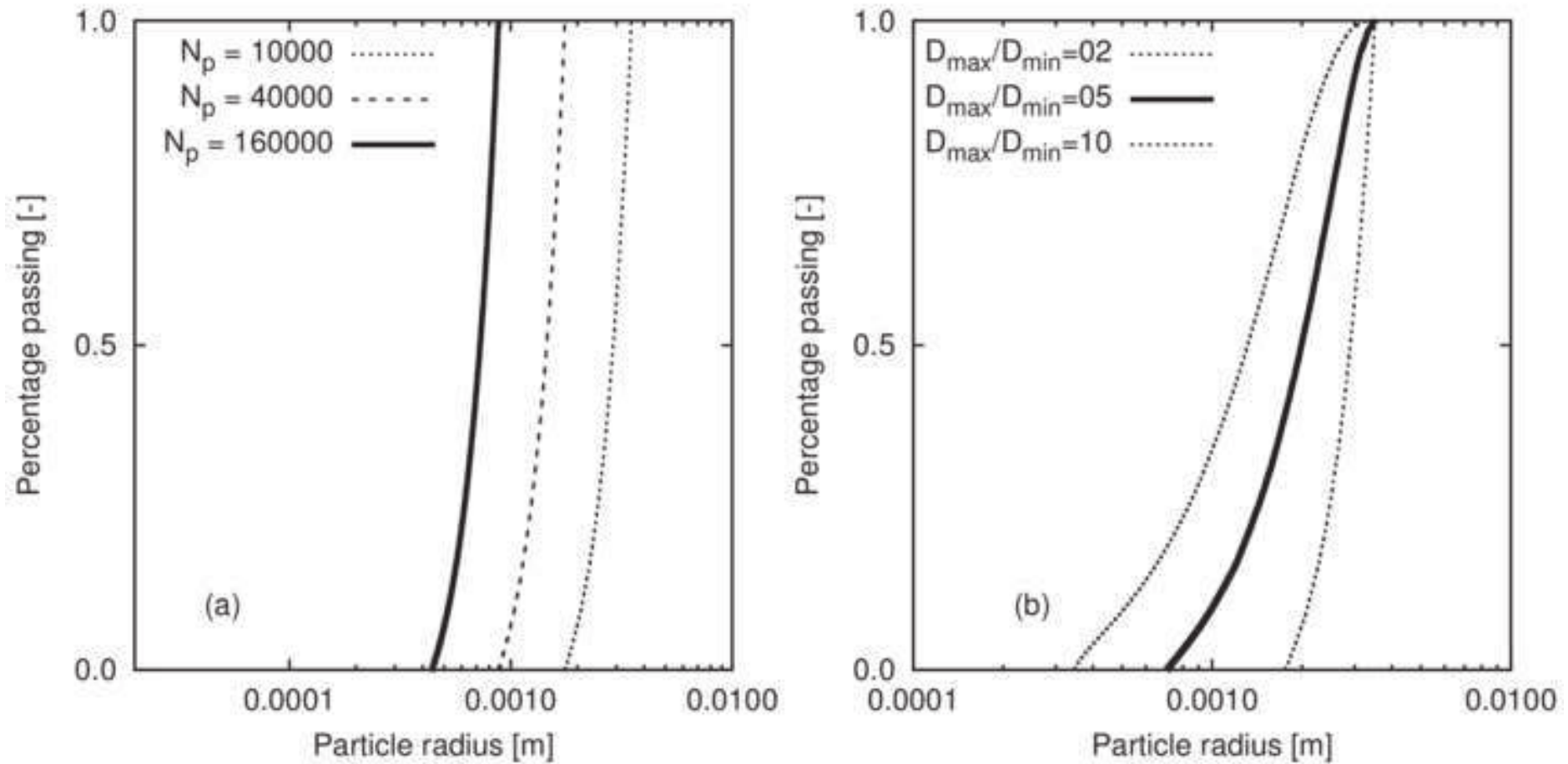


Fig.02

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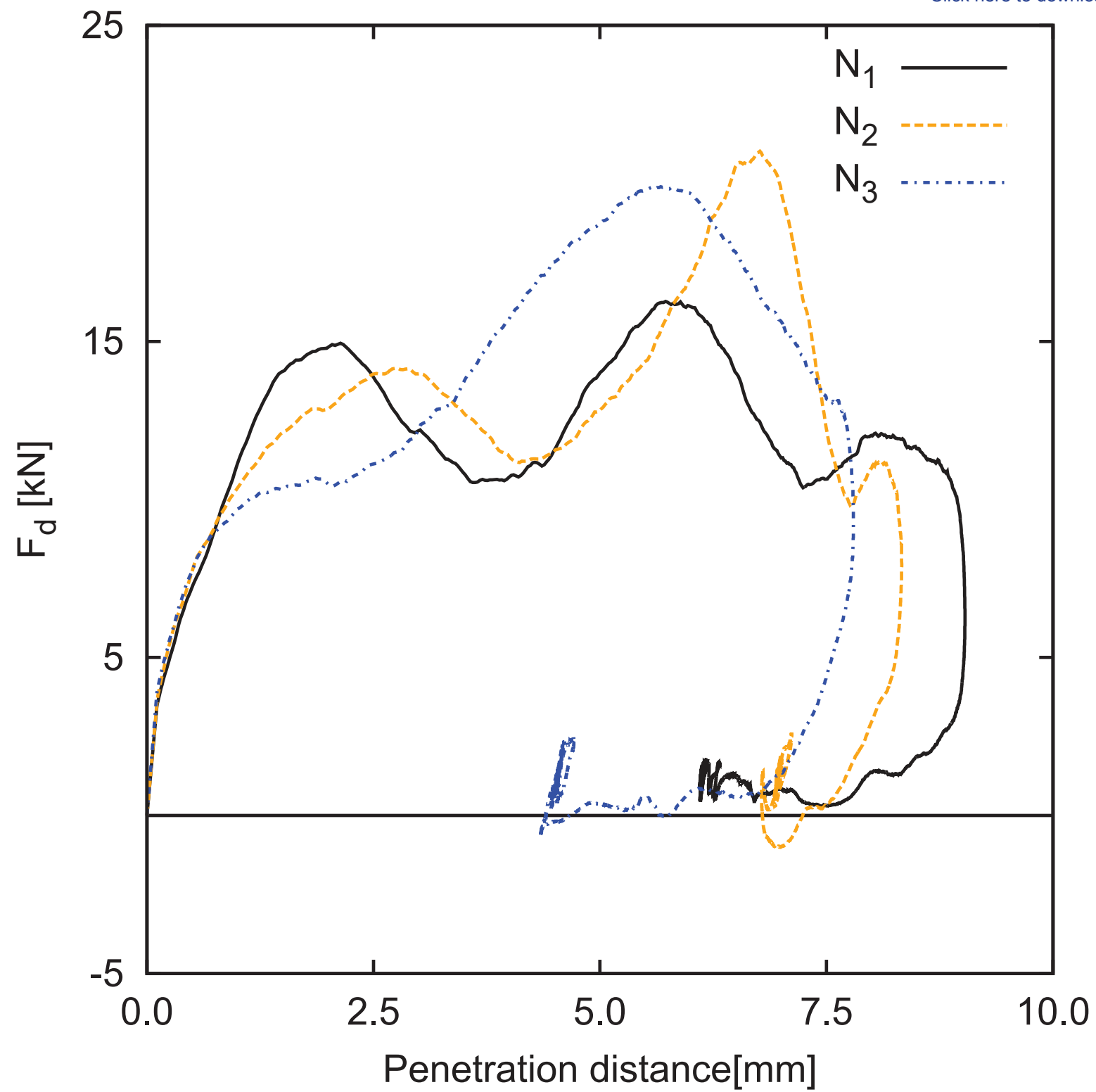
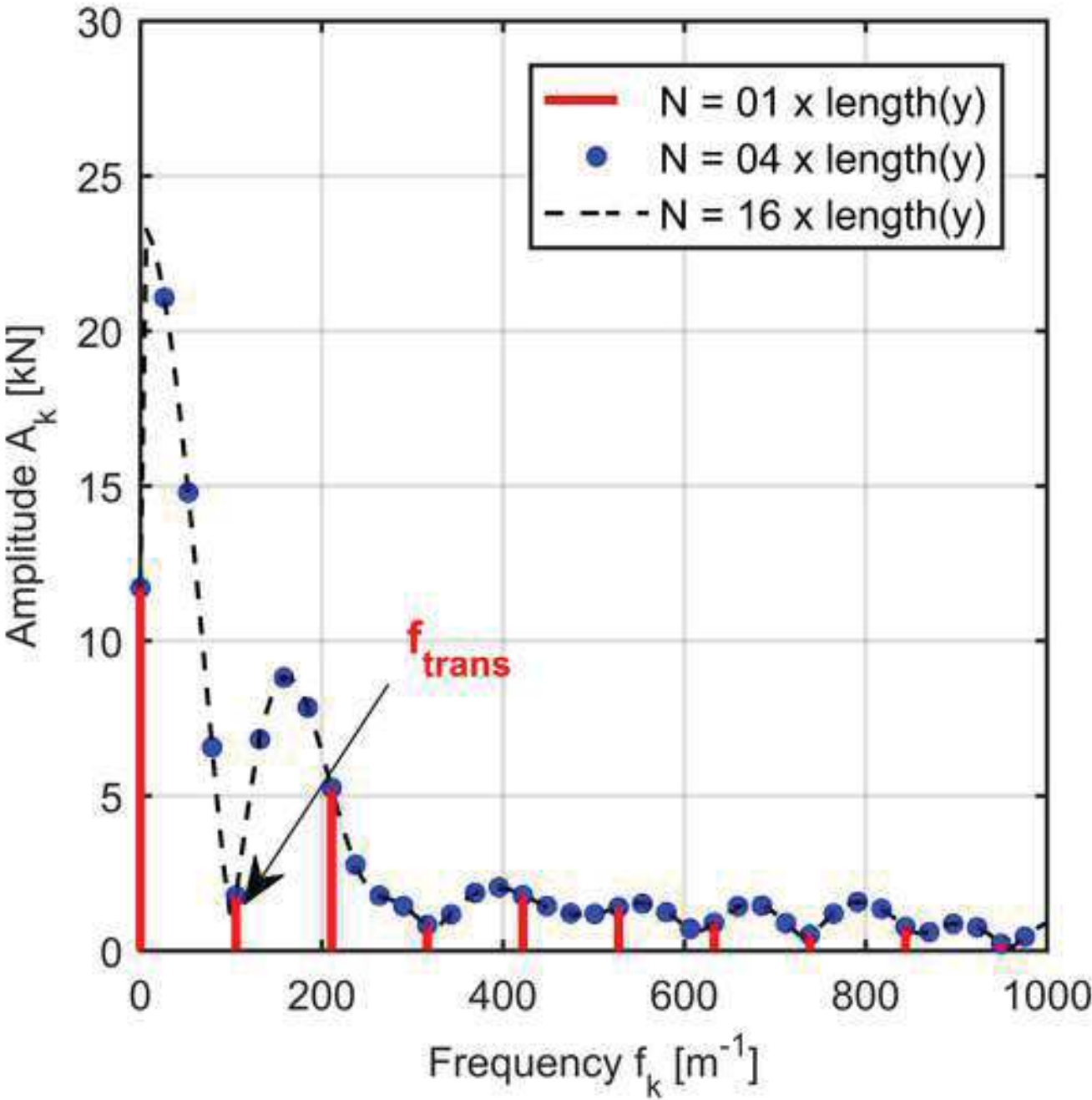


Fig.06



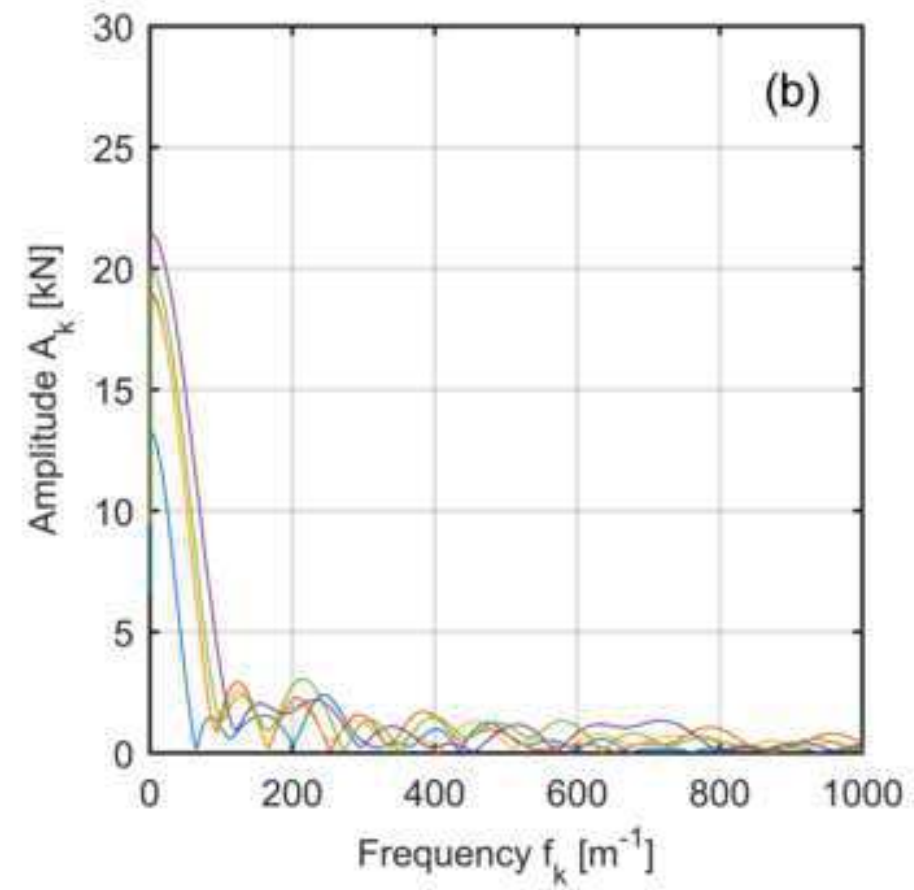
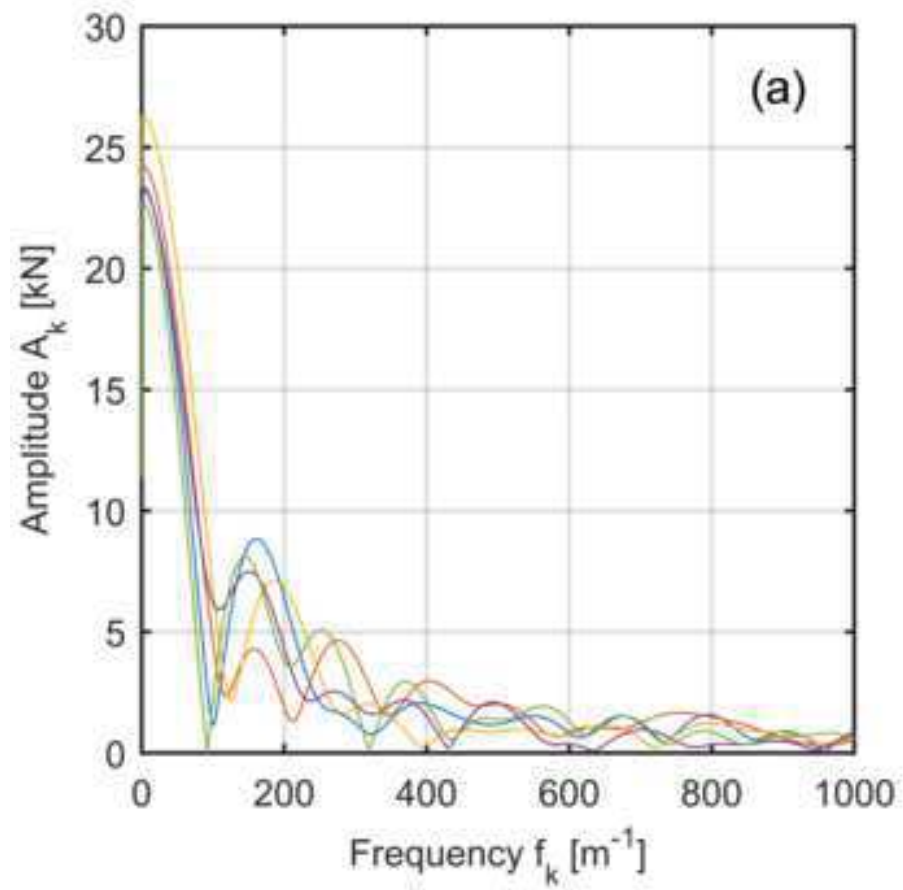
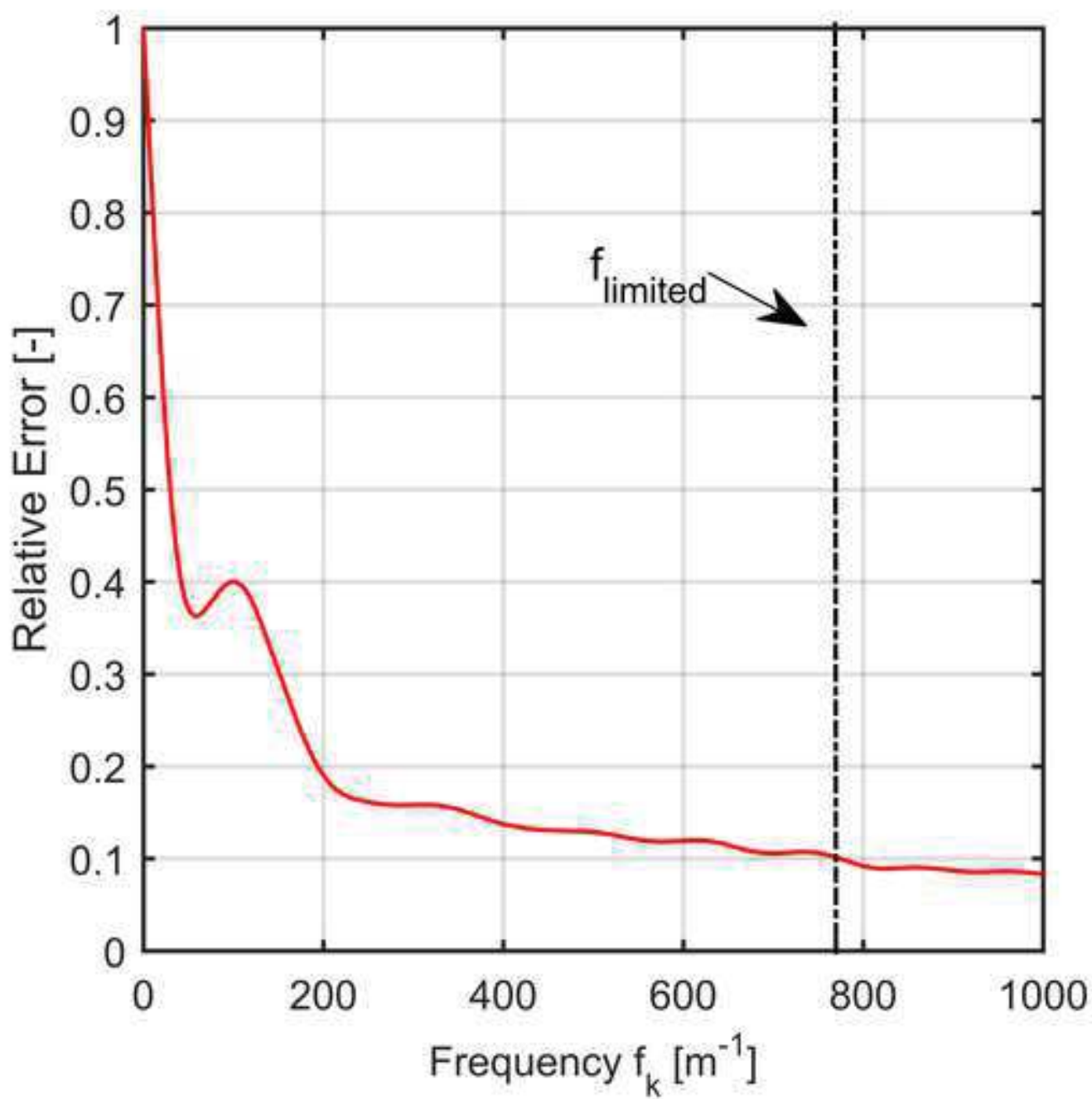


Fig.08



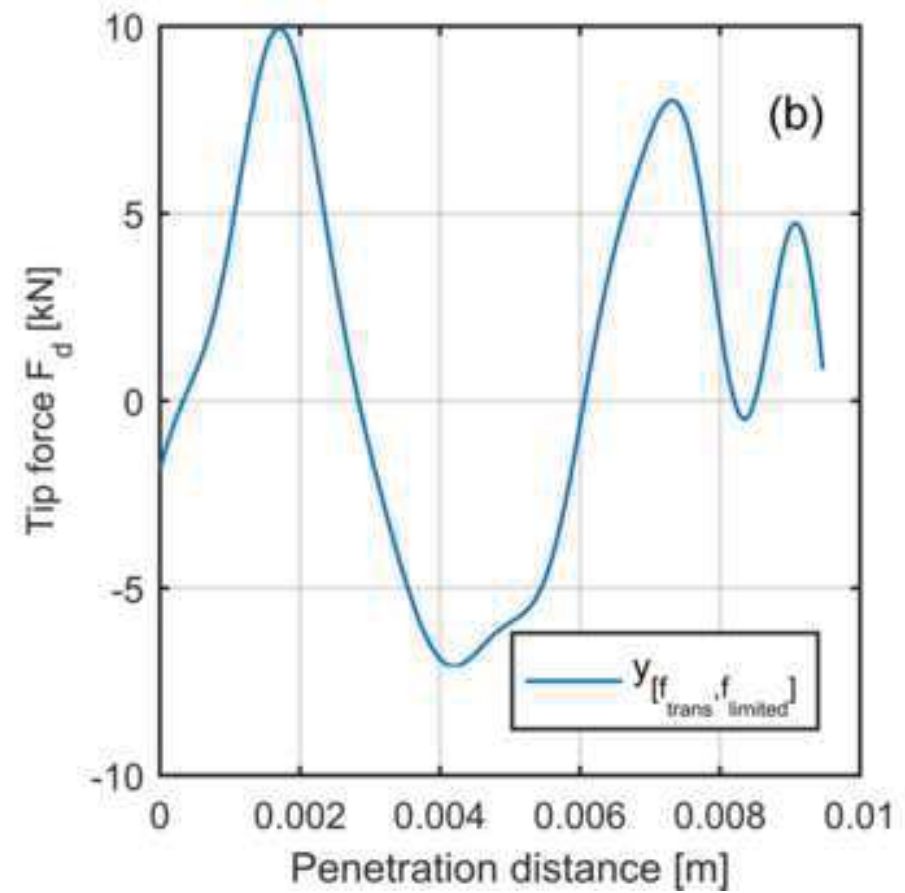
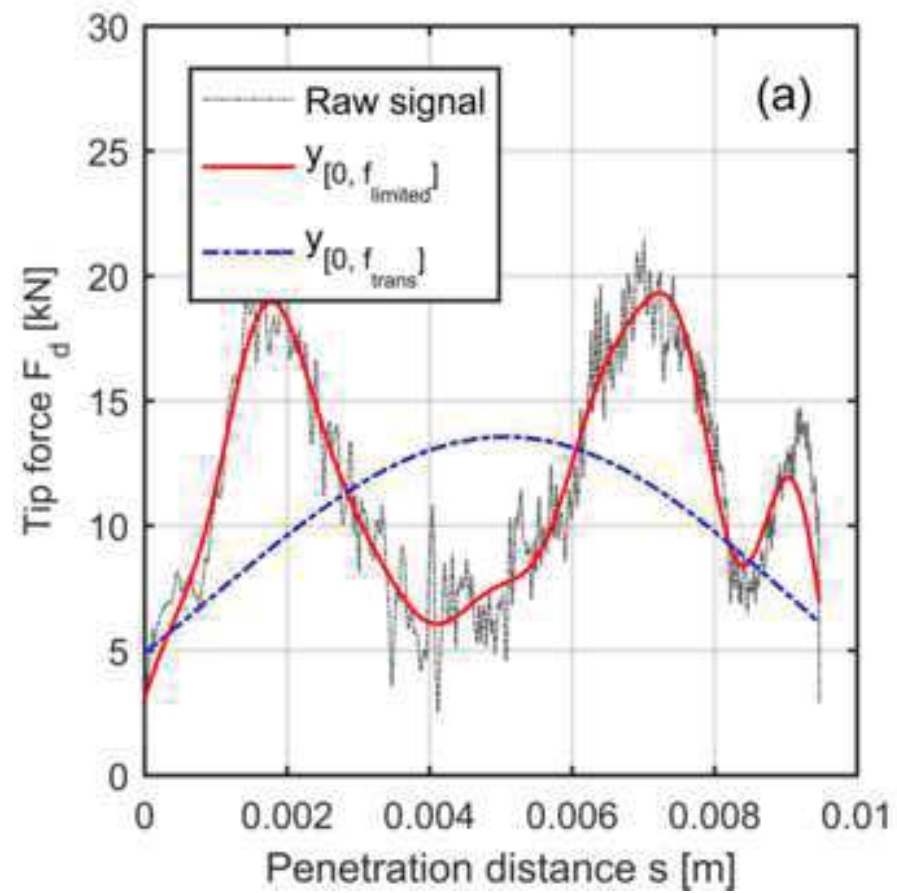


Fig.10

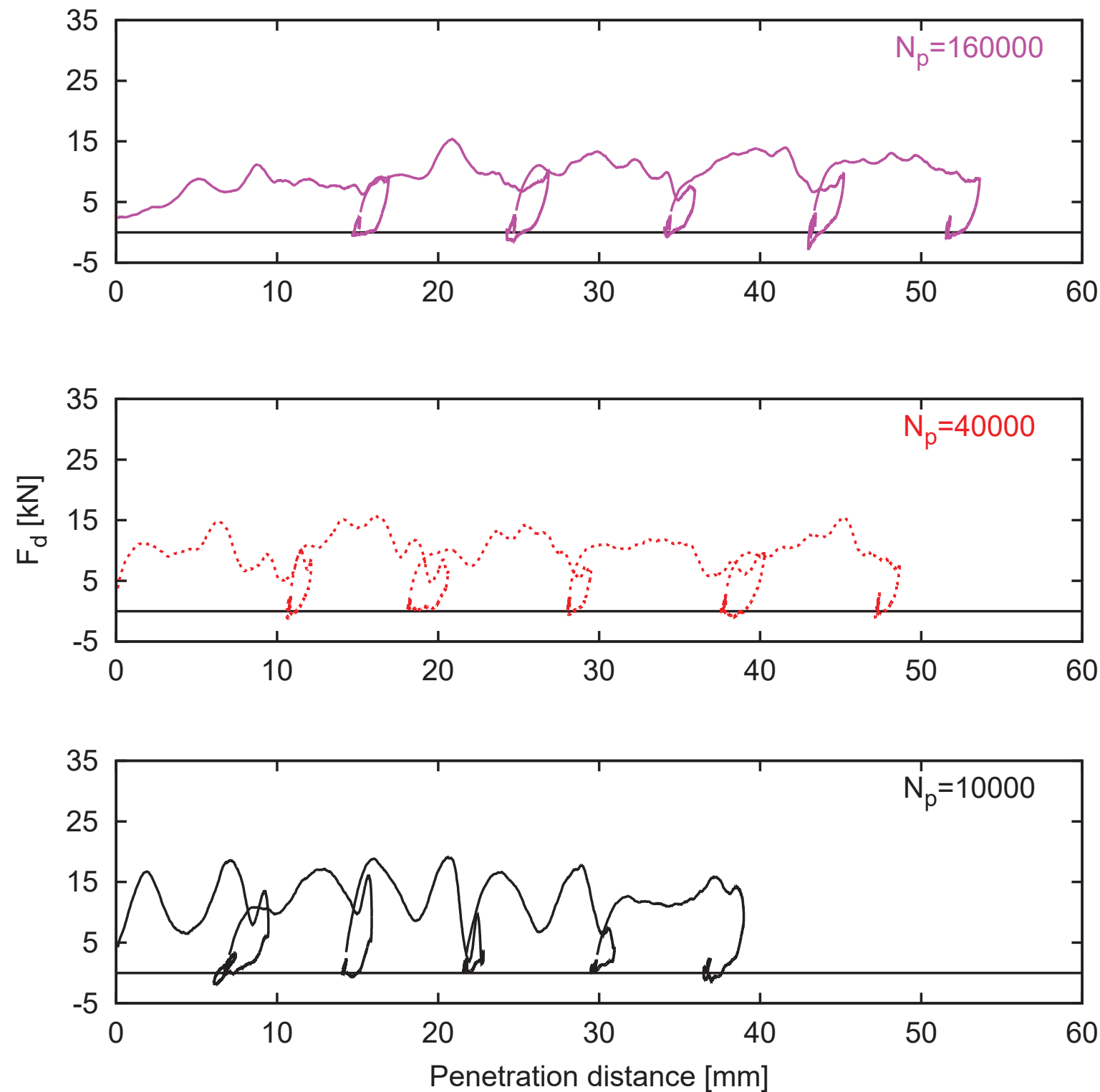


Fig.11

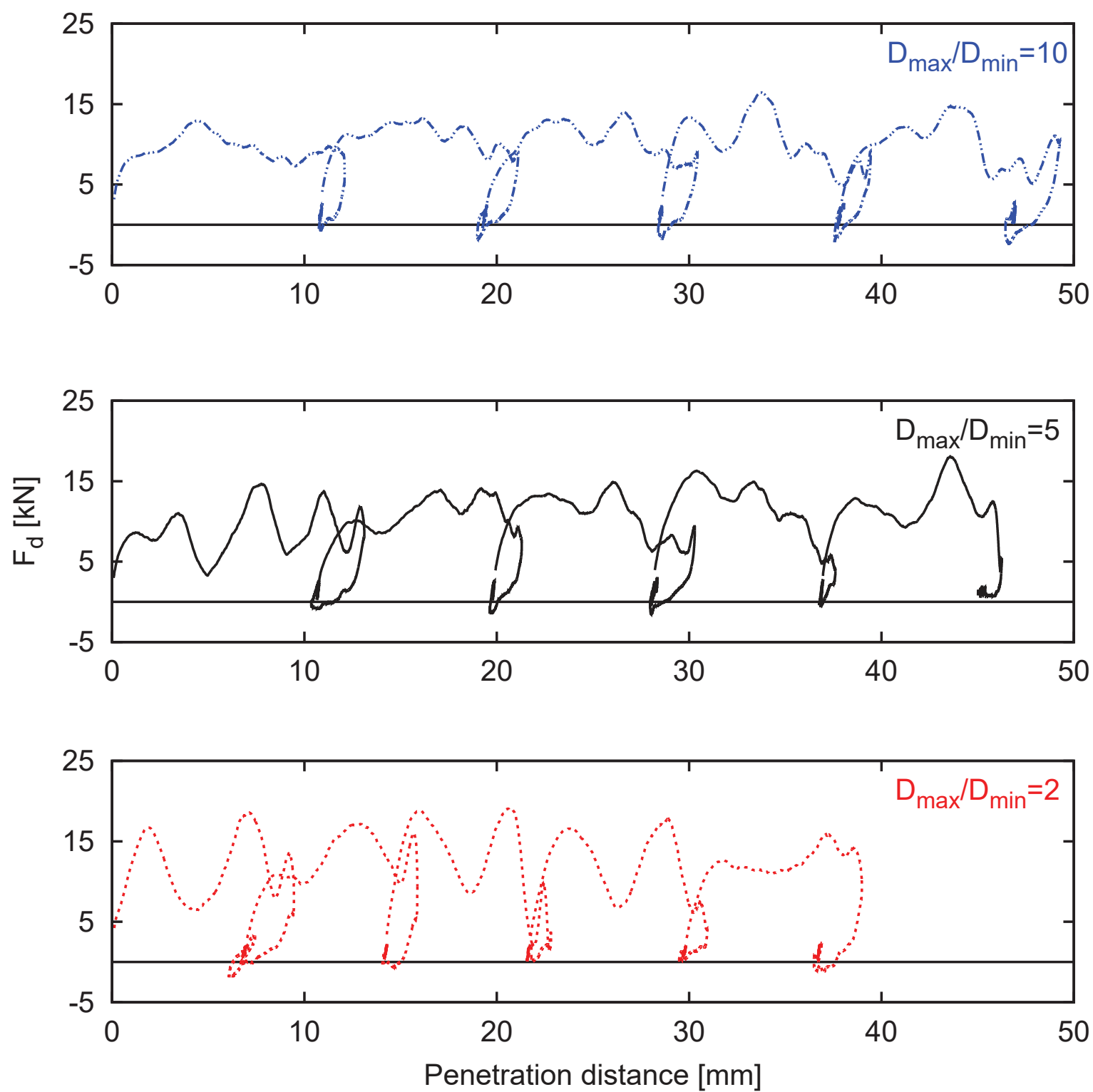


Fig.12

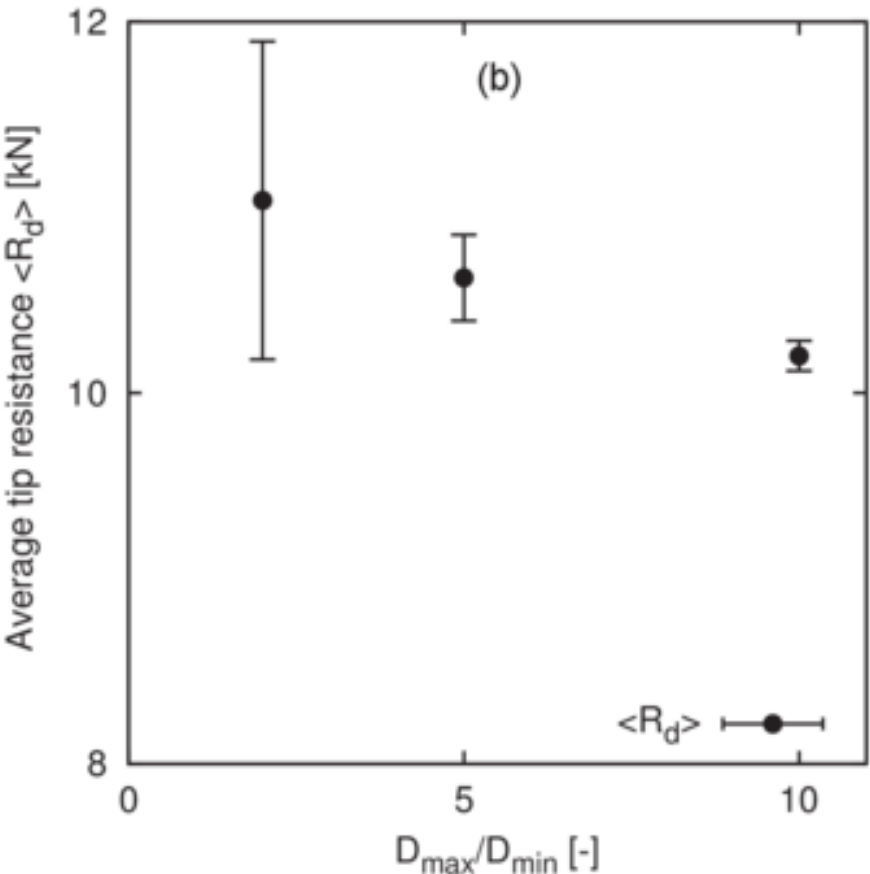
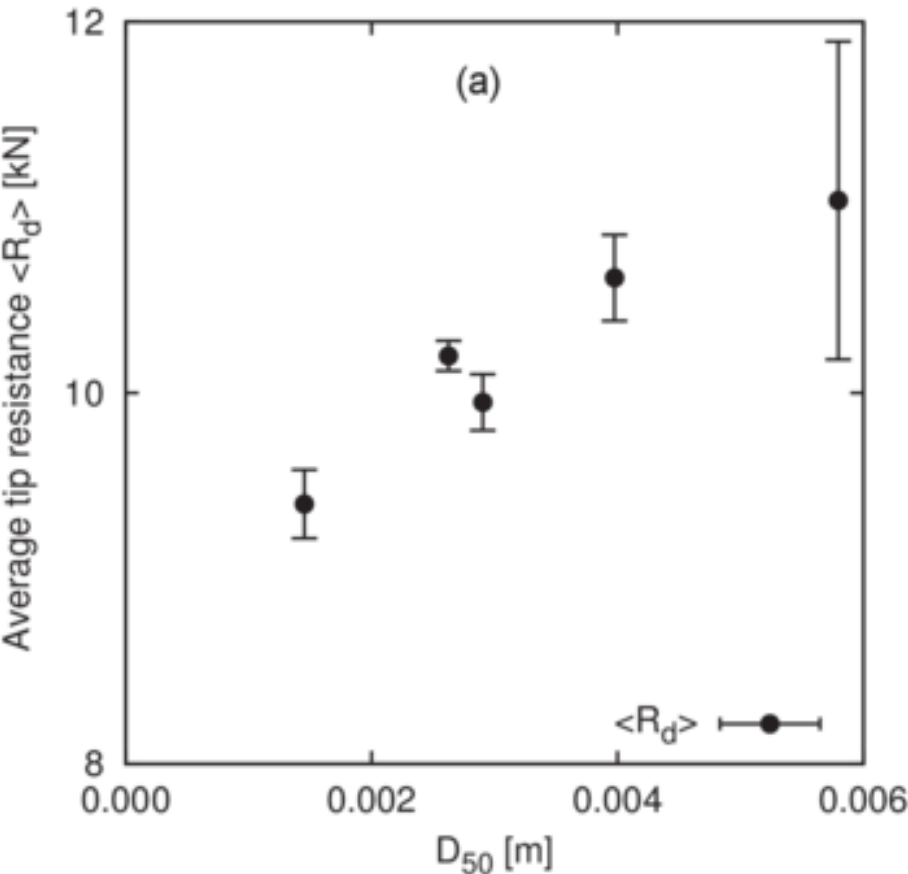


Fig.13

